

Binary Neutron Stars II: multi-messenger emission

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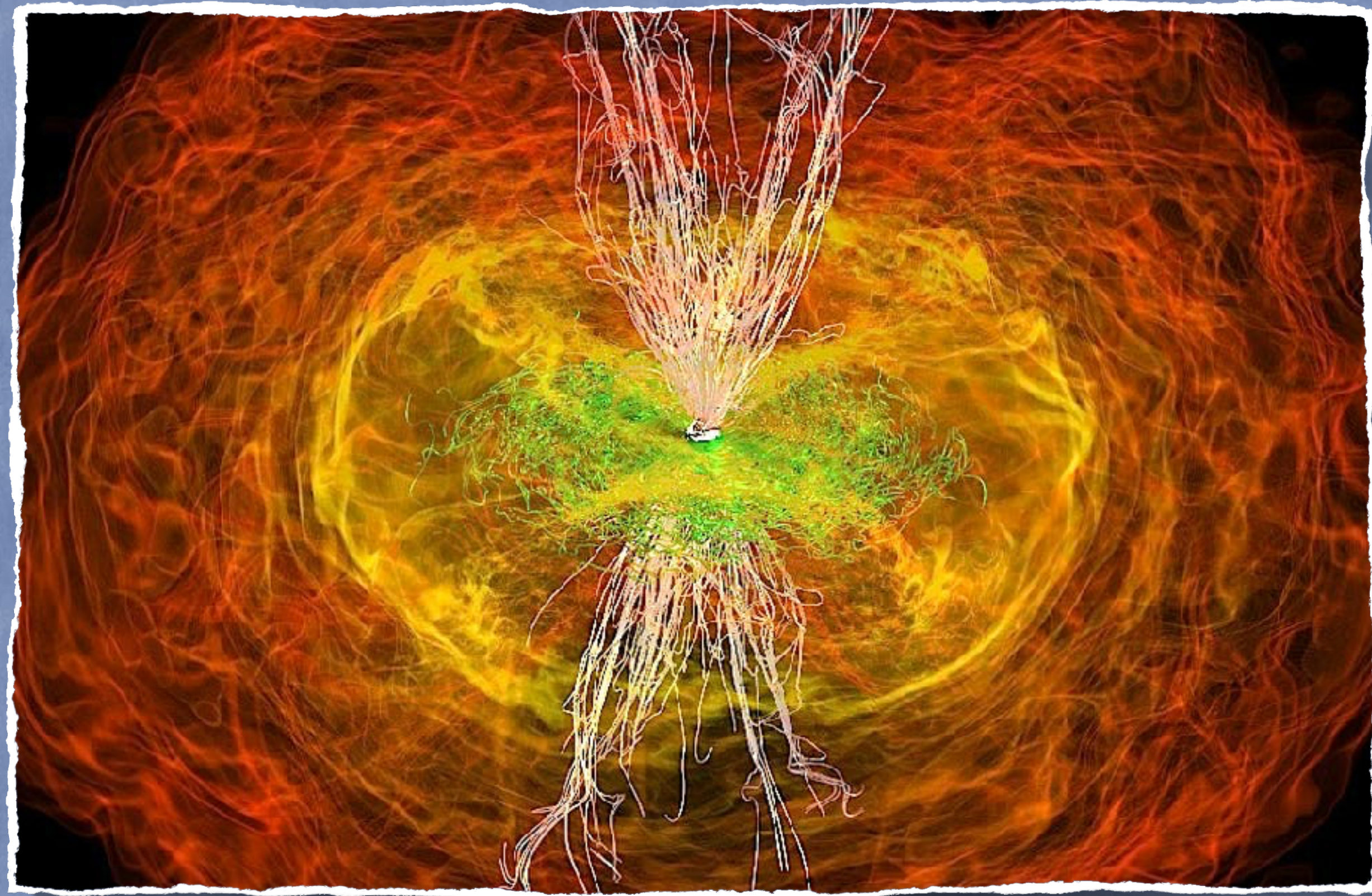
Timisoara, May 27 2026

Blended Intensive Programme (BIP):

Relativistic Fluid Dynamics

Plan of the talk II

- Electromagnetic counterparts and jet formation
- Magnetic field amplification at merger KHI
- Role of B-field topology and NS spin
- Neutrino emission and magnetar jets
- *r*-process nucleosynthesis of heavy elements

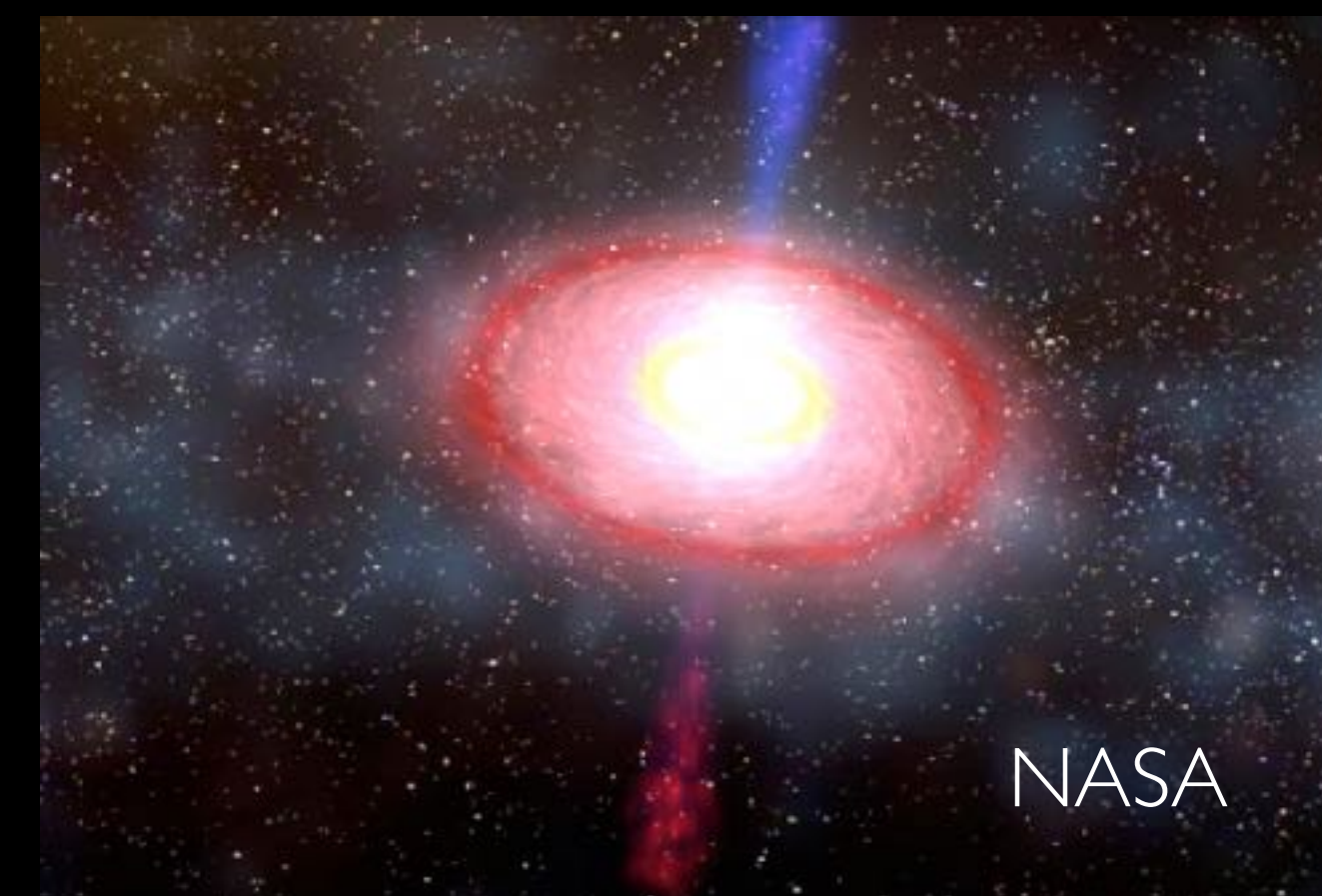


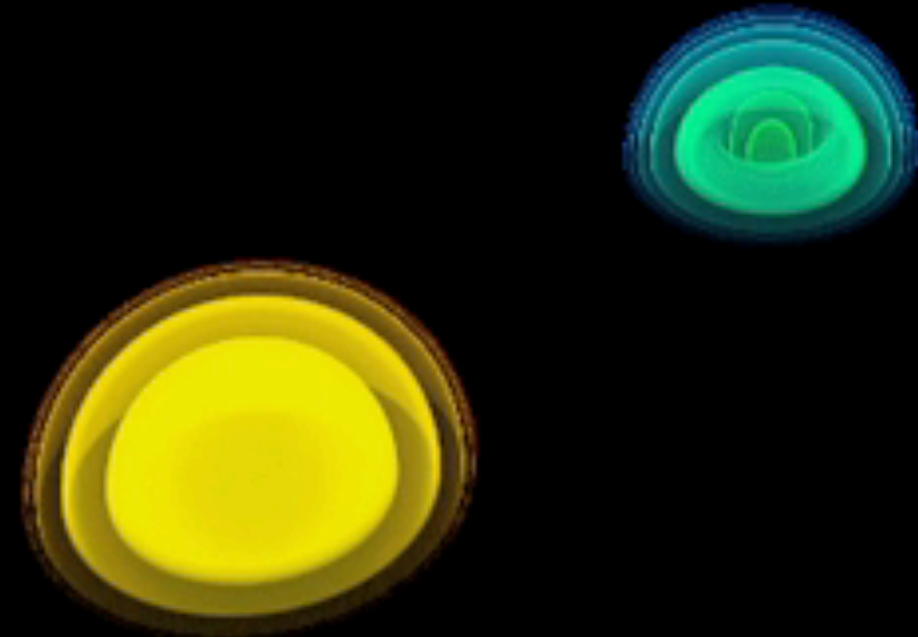
Electromagnetic counterparts and jet formation

Electromagnetic counterparts

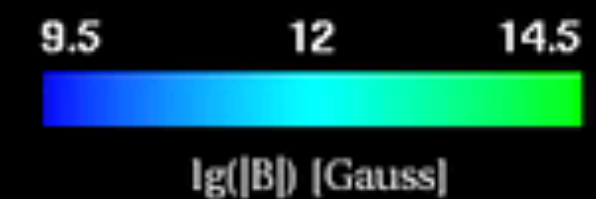
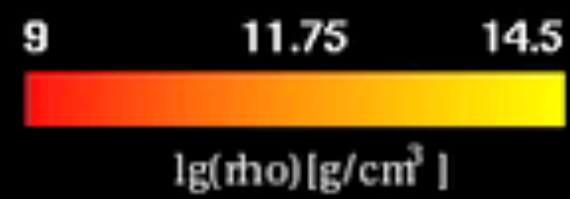
- Since 70's observed flashes of gamma rays observed with energies 10^{50-53} erg: **gamma-ray bursts (GRBs)**
- Two families of GRBs: "**long**" and "**short**"
- **Long**: last 10-100 s; likely due to the collapse of very massive stars.
Short: last 1-10 s; we know they are due to NS mergers (GW170817)
- All GRBs show **jets** but how is a jet produced from a binary merger?

Need to solve equations of GRMHD in addition to the Einstein equations



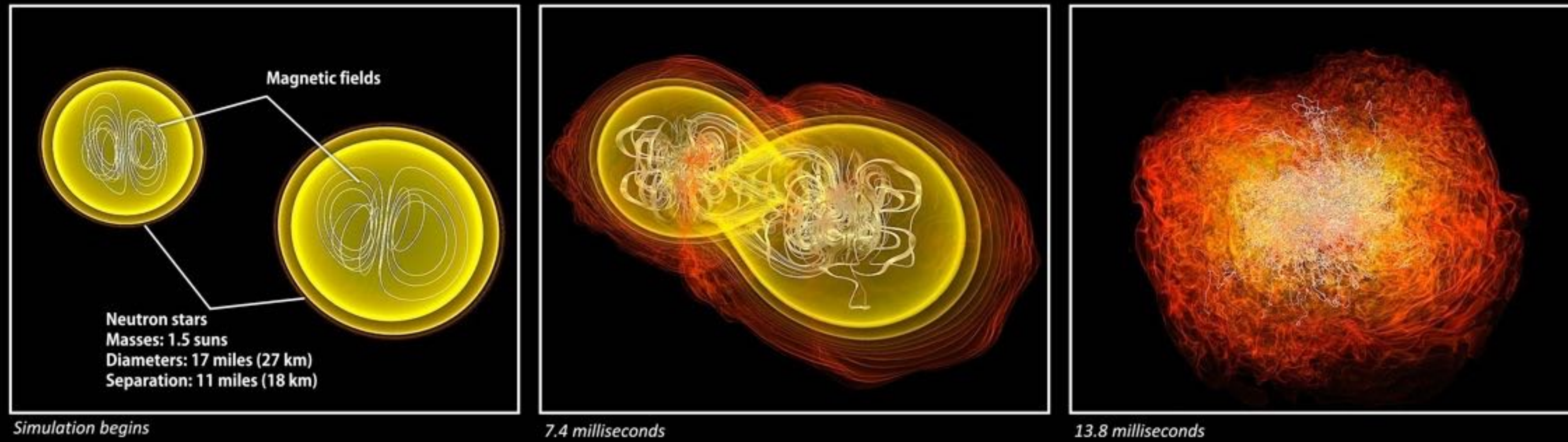


$$M = 1.5 M_{\odot}, B_0 = 10^{12} \text{ G}$$

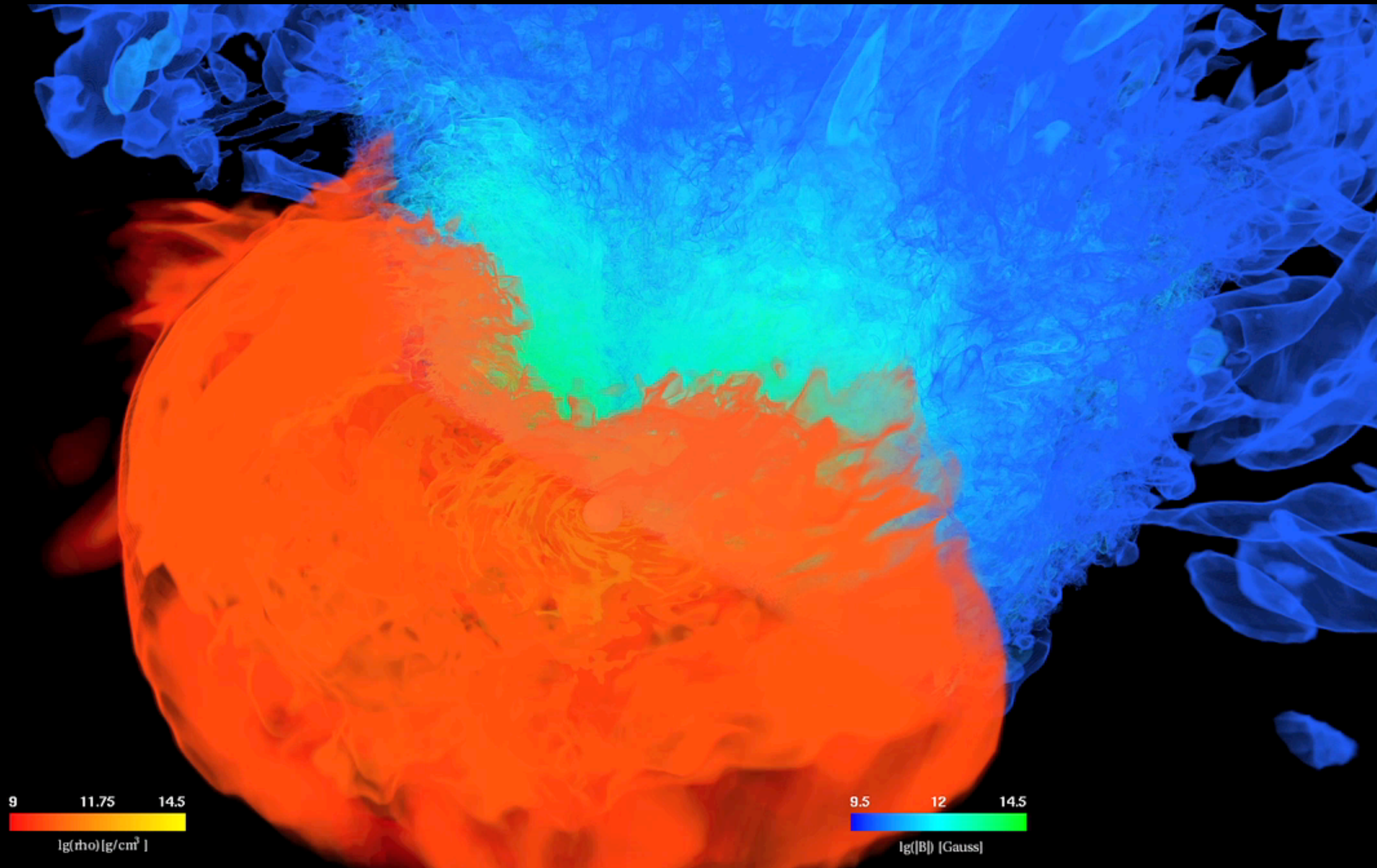


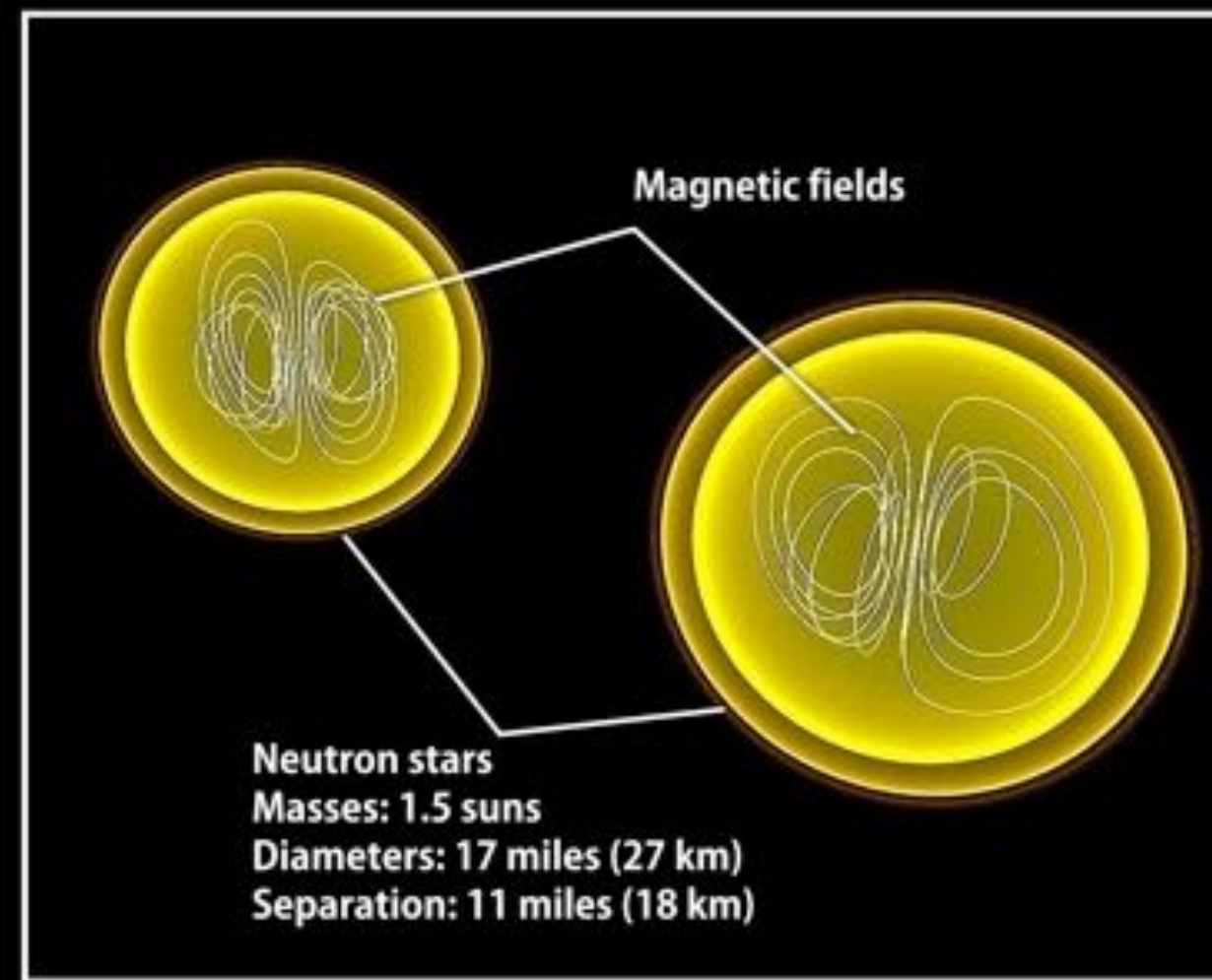
Animations:, LR, Koppitz

What happens when magnetised stars collide?

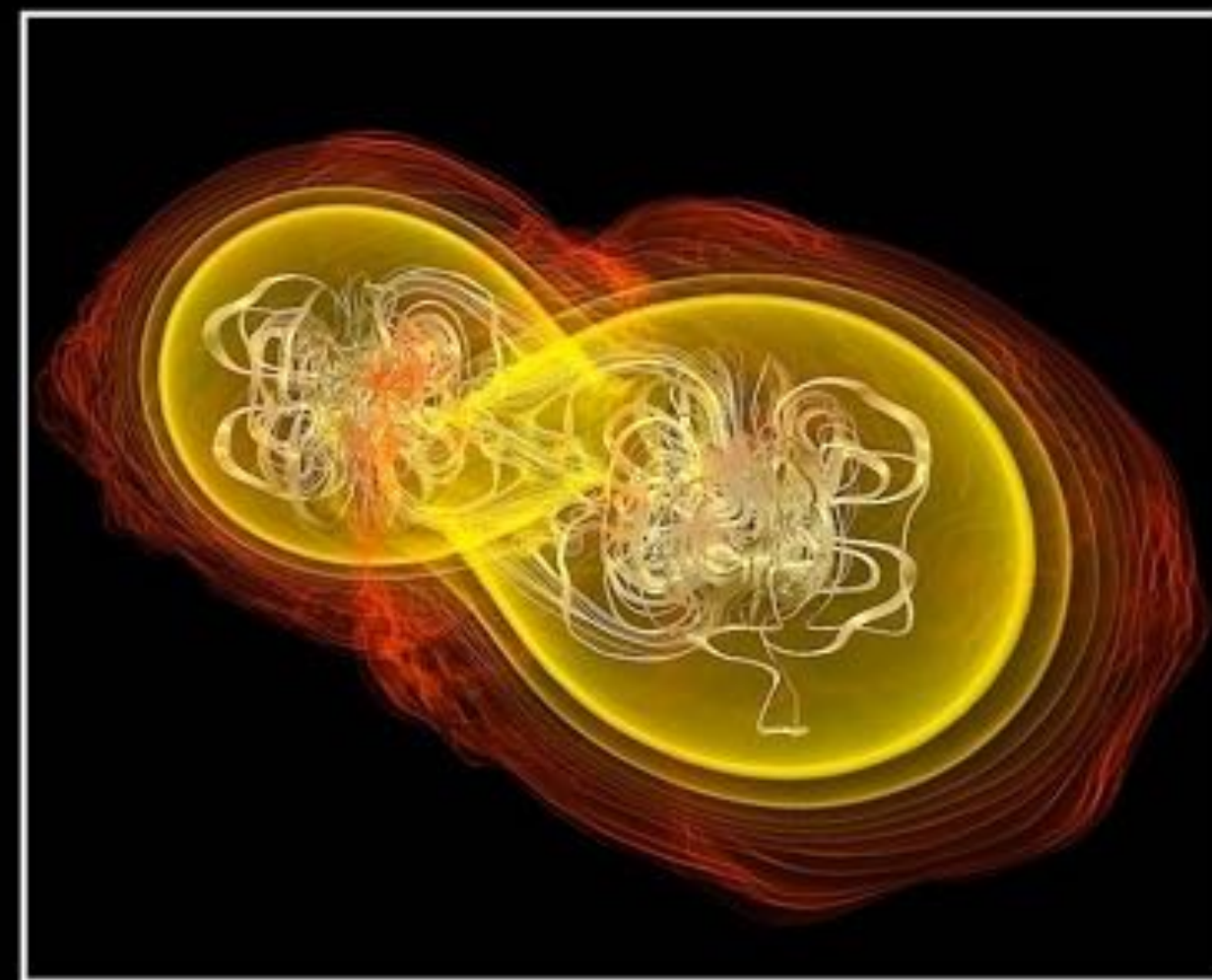


Magnetic fields in the HMNS have complex topology: dipolar fields are destroyed.

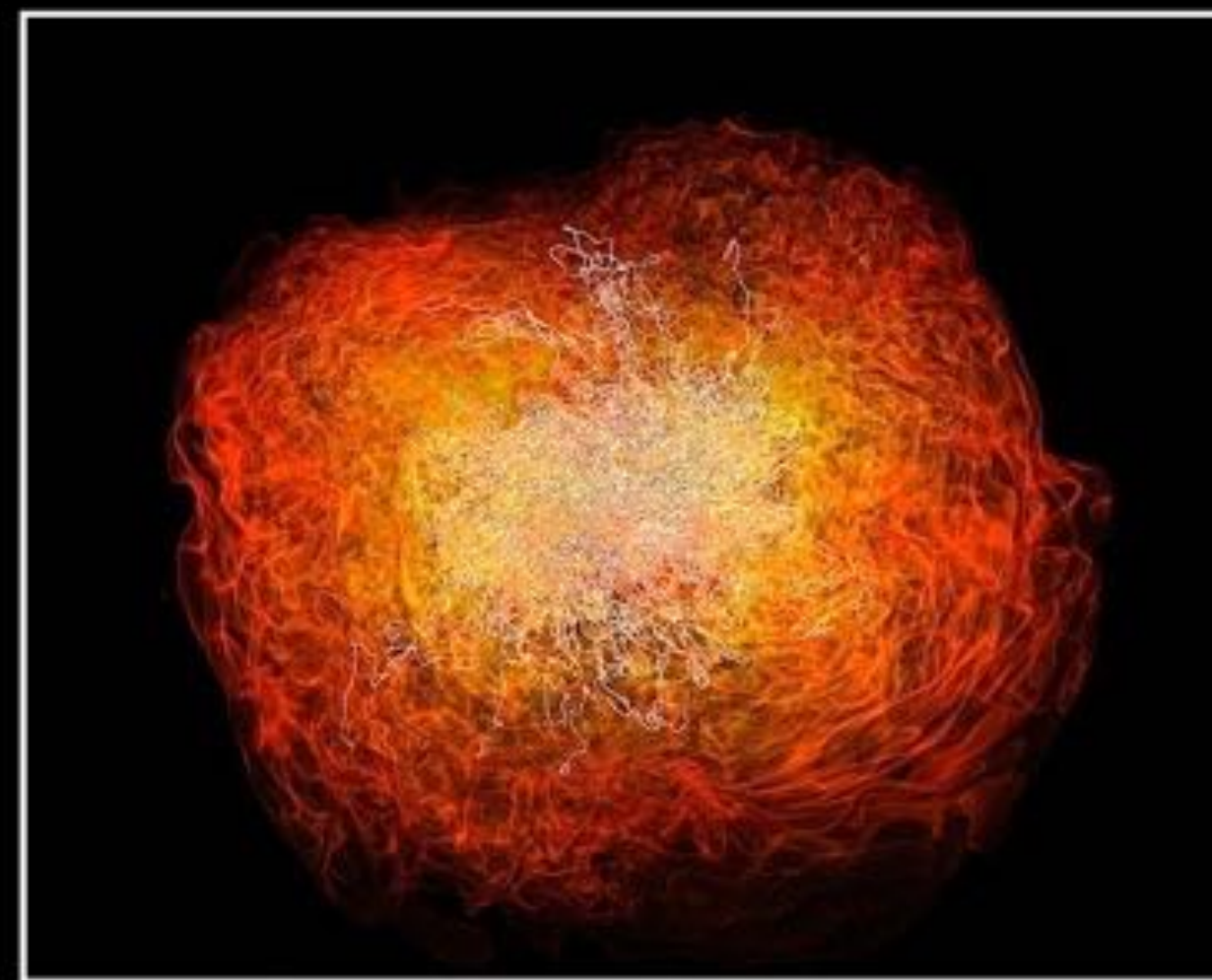




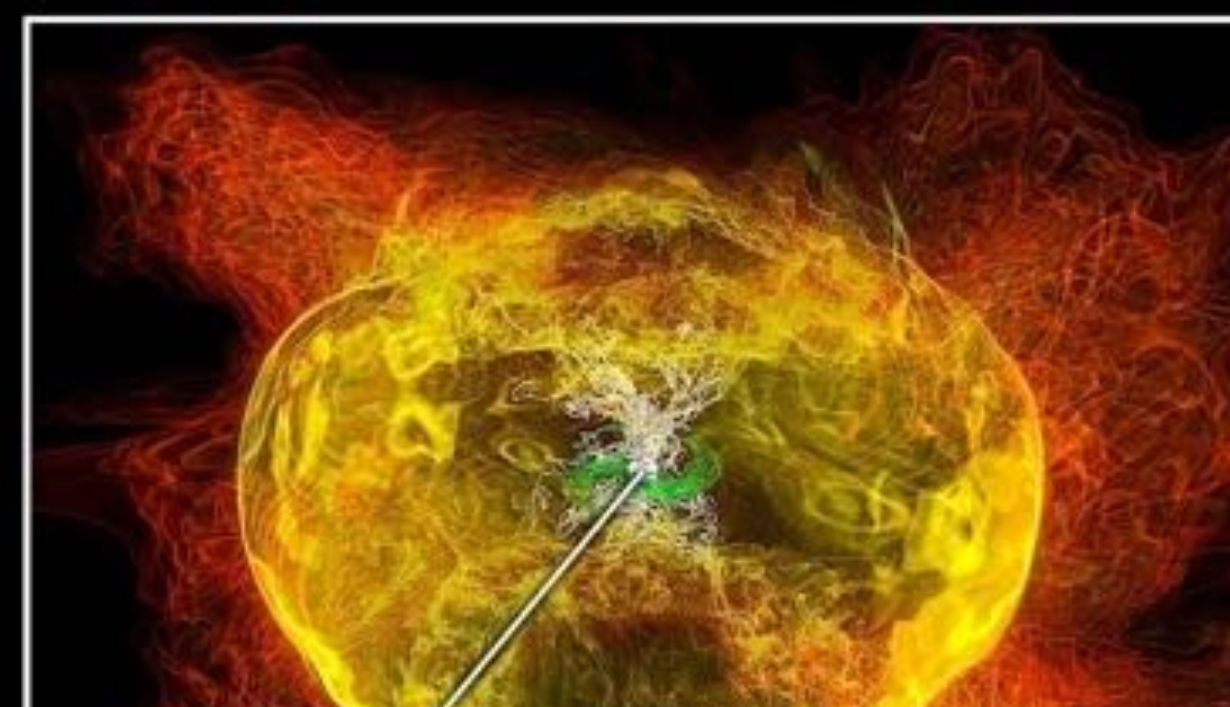
Simulation begins



7.4 milliseconds



13.8 milliseconds



Black hole forms
Mass: 2.9 suns
Horizon diameter: 5.6 miles (9 km)
15.3 milliseconds



21.2 milliseconds



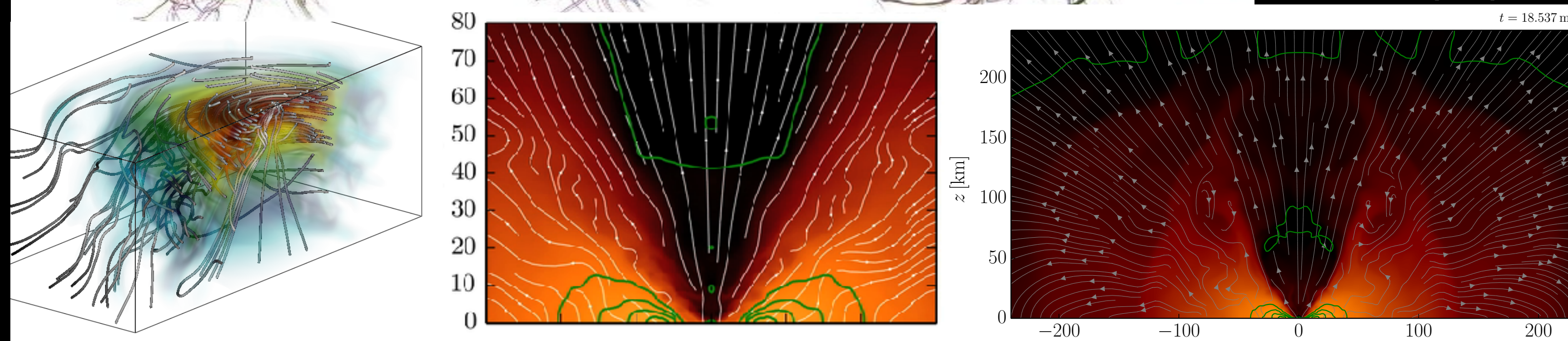
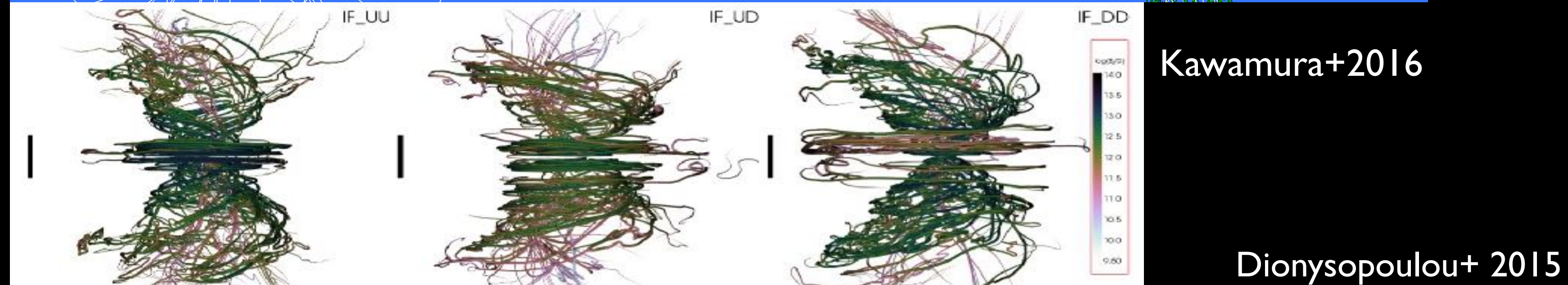
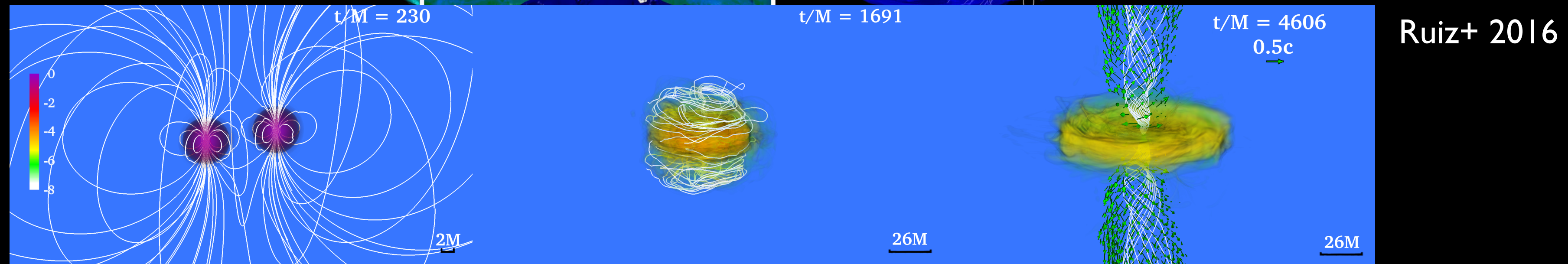
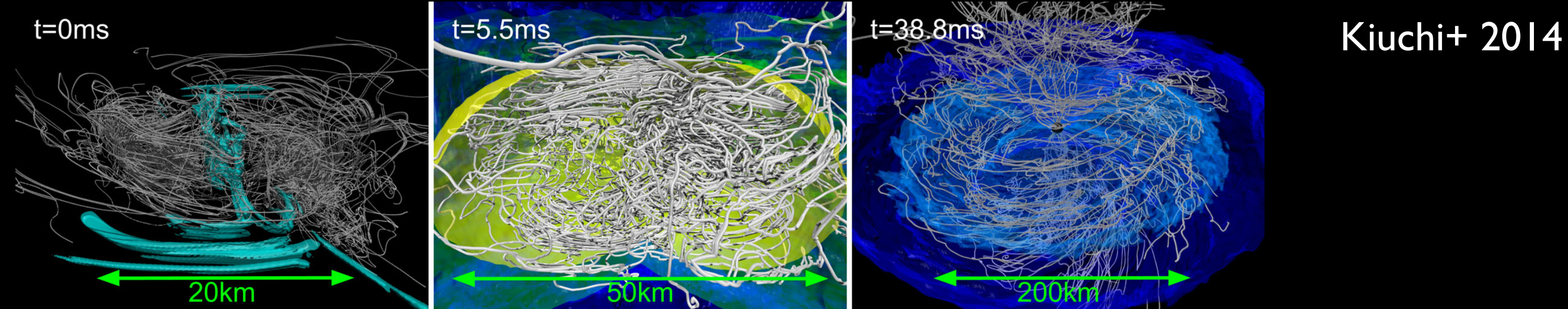
26.5 milliseconds

These simulations have shown that the merger of a magnetised binary has all the basic features behind SGRBs

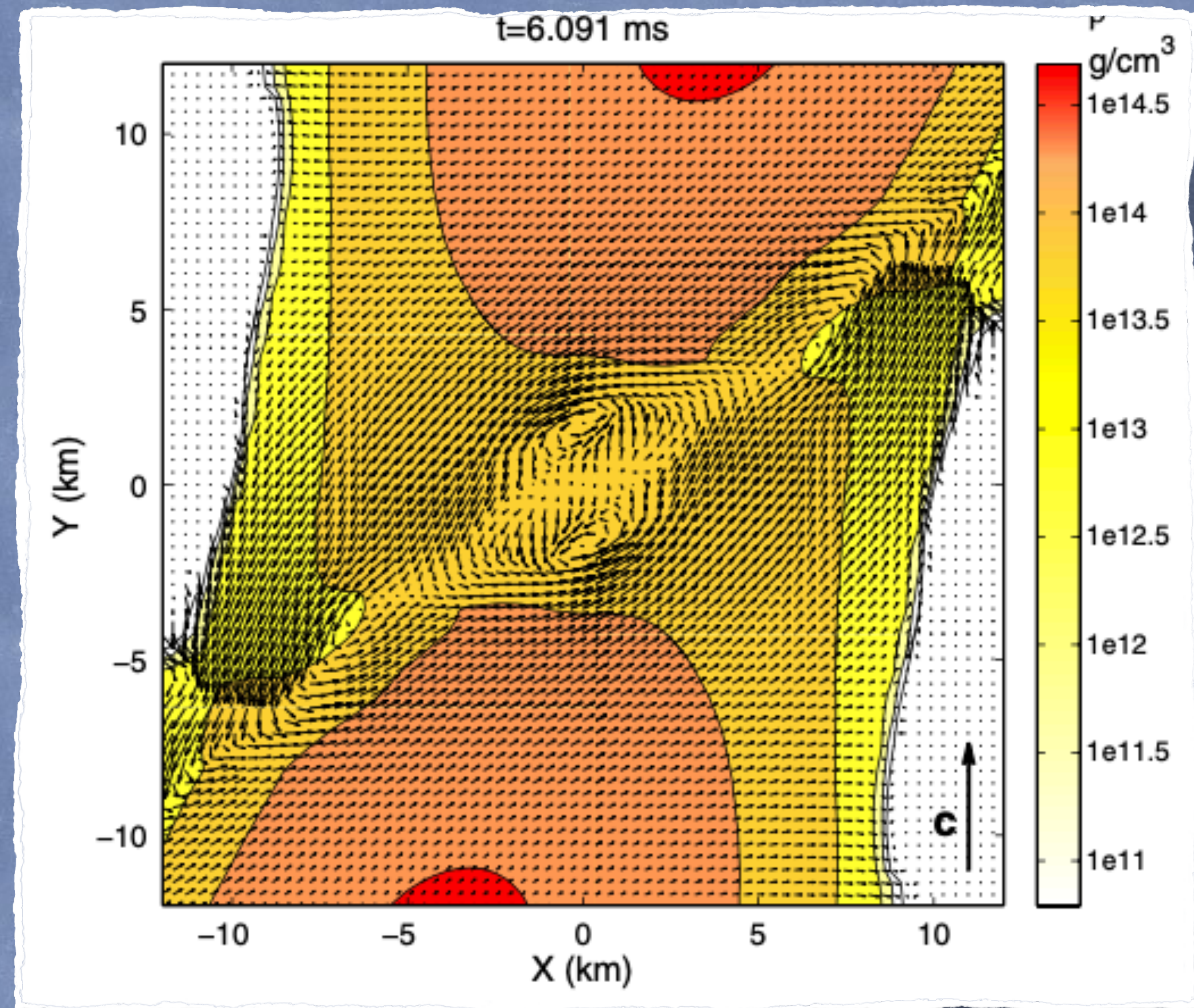
$$J/M^2 = 0.83 \quad M_{\text{tor}} = 0.063 M_{\odot} \quad t_{\text{accr}} \simeq M_{\text{tor}}/\dot{M} \simeq 0.3 \text{ s}$$

Credit: NASA/AEI/ZIB/M. Koppitz and L. Rezzolla

With due differences, other groups confirm this picture



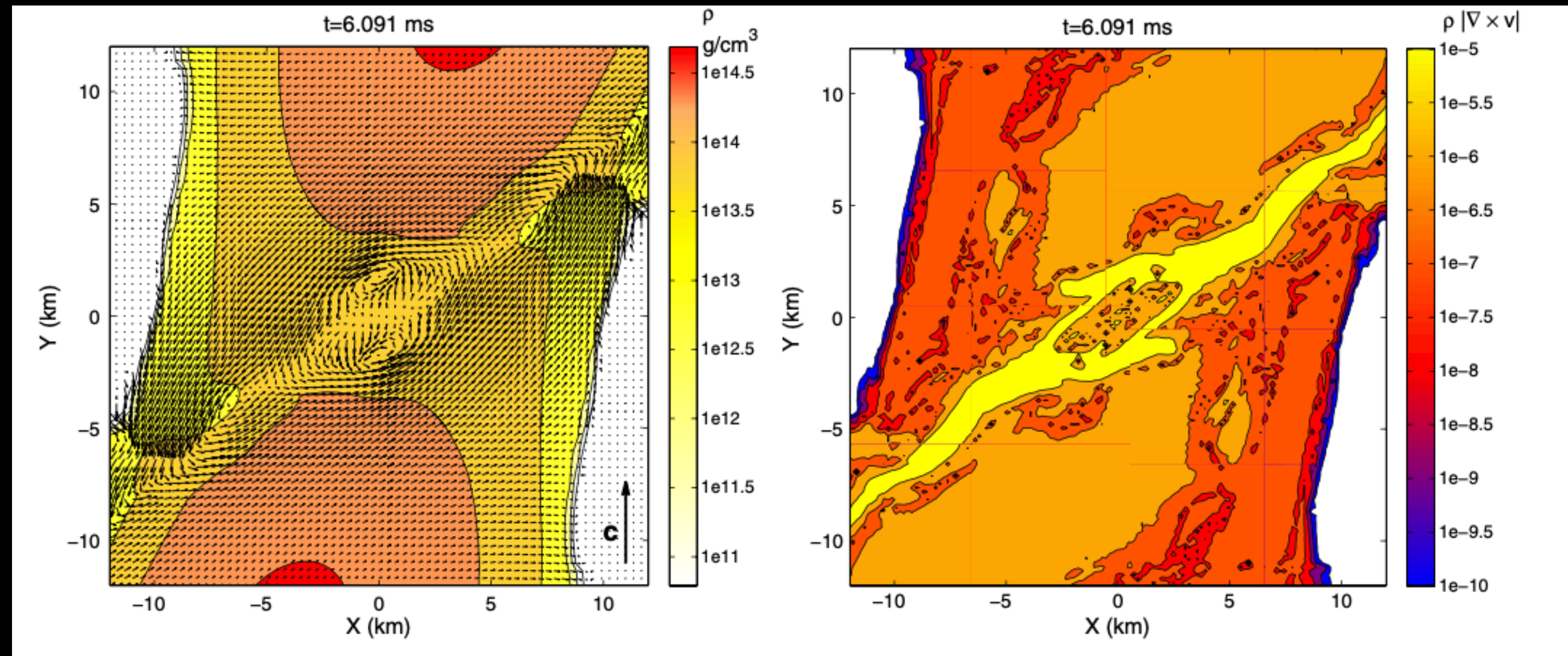
RMHD



Magnetic-field
amplification and
crustal fields

A very powerful instability

- at merger, a strong **tangential discontinuity** is produced by the **shear** between the stellar surfaces.



- this leads to **Kelvin-Helmholtz** instability (KHI) and large vorticity
- in turn this leads to **exponential** growth of **toroidal** magnetic field

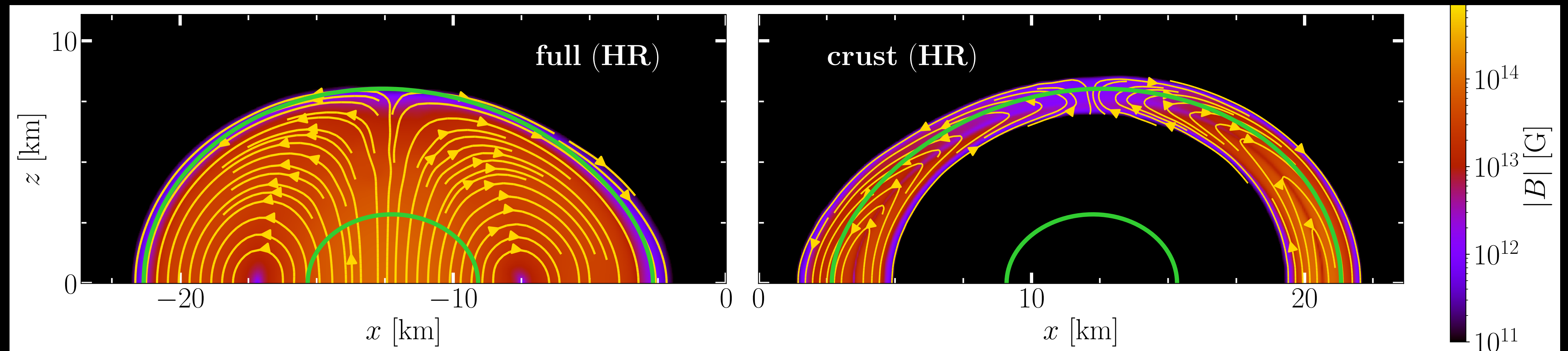
A very powerful instability

- in practice, we **cannot** model this process yet despite simulations at ultra-high resolution and enormous computational costs.
- this is because there is **no minimum wavelength** in the development of KHI
- all we know is that magnetic fields grow **exponentially** till **equipartition** with binding/kinetic energy in the system

$$10^{10} \text{ G} \rightarrow 10^{16} \text{ G} \quad \text{in few ms!}$$

- additional **linear** amplification of the B-field takes place later on because of a **turbulent** magnetorotational (shearing) instability (MRI)

- simple question: does the amplification depend on the **B-field topology**?
- internal magnetic field in NSs is unknown
- a global **poloidal field** is the standard assumption but not only one
- a number of pulsar models postulate the existence of **crustal fields** only



- assuming the **same magnetic energy** can we tell the difference via numerical simulations?

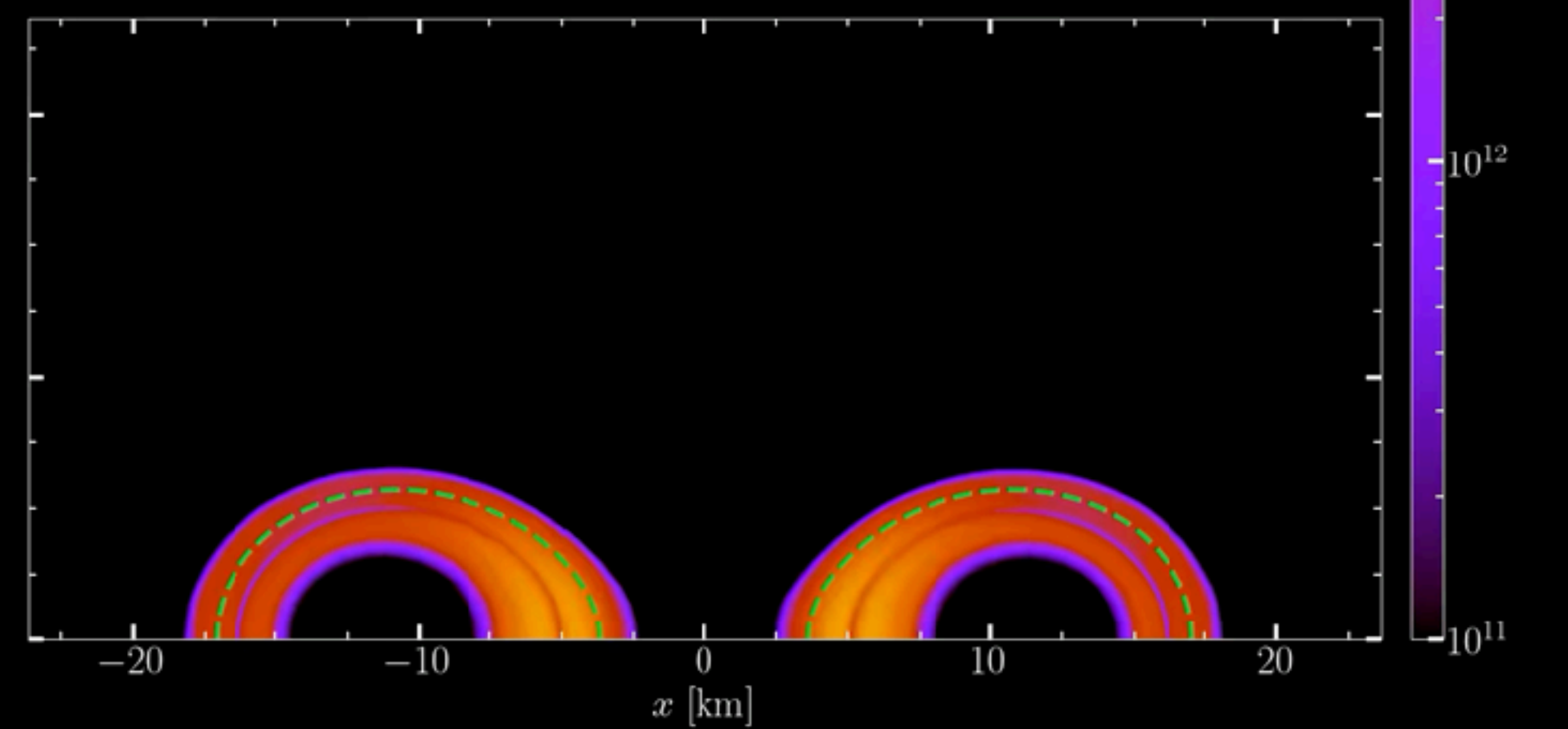
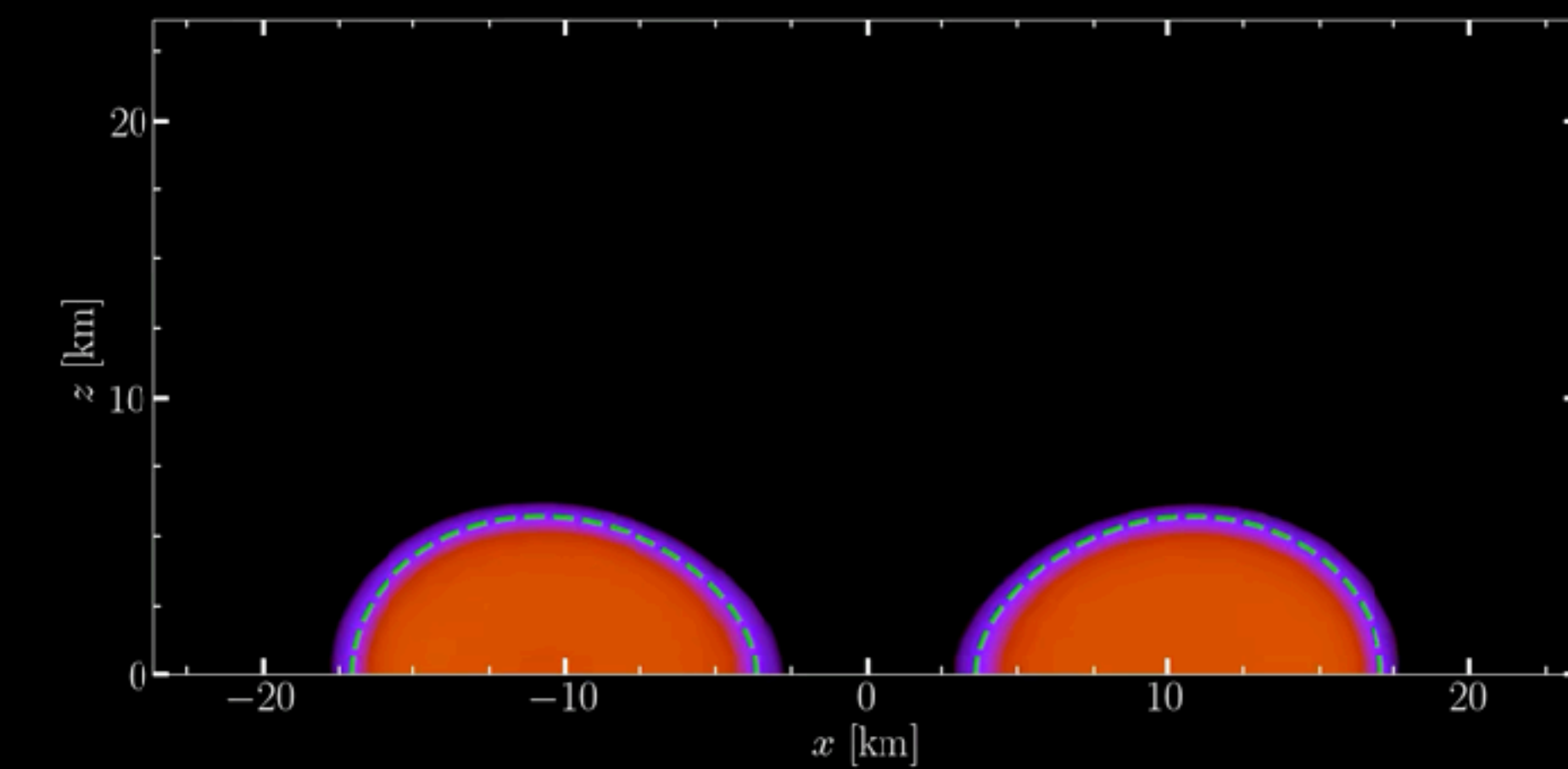
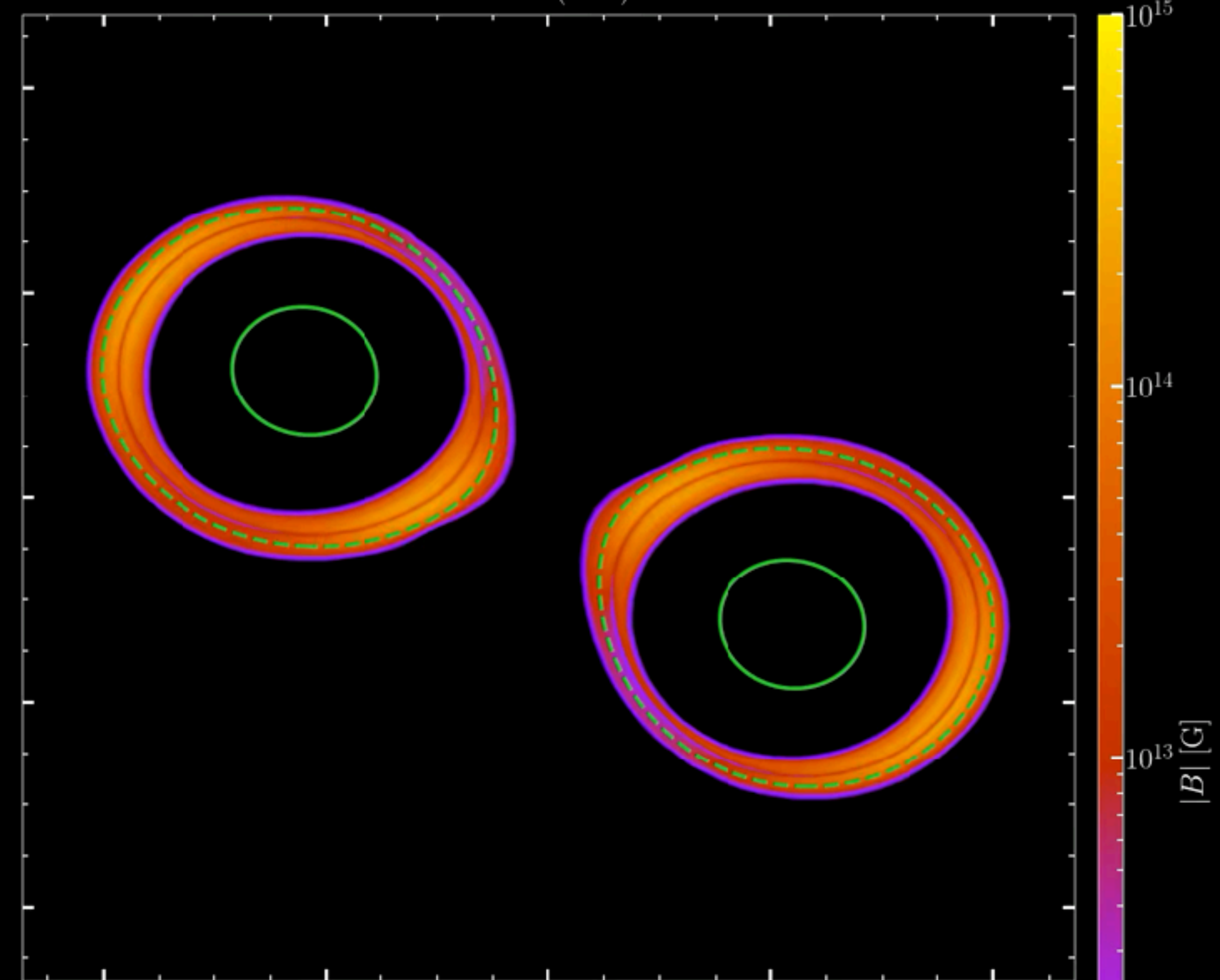
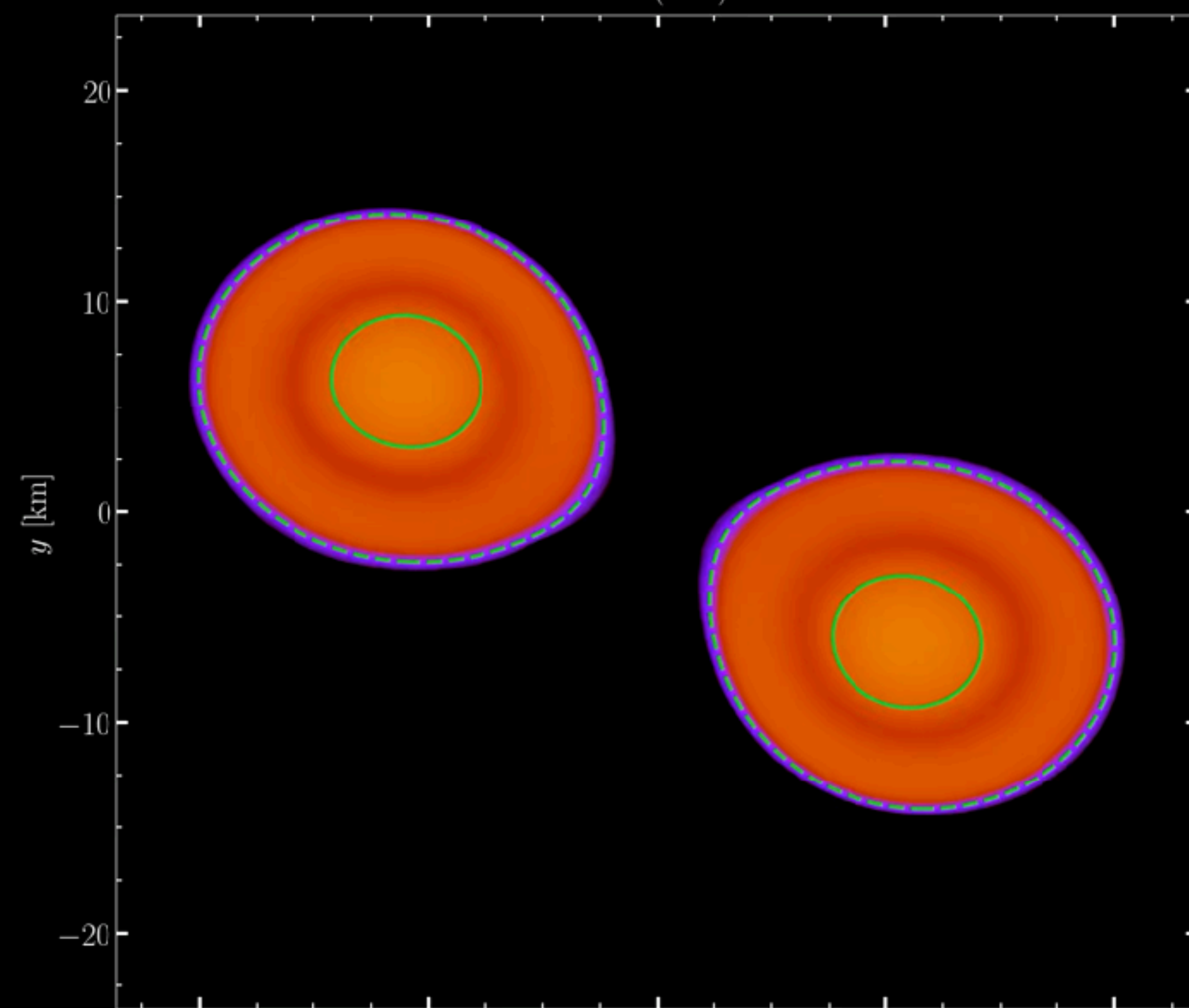
full

Full (HR)

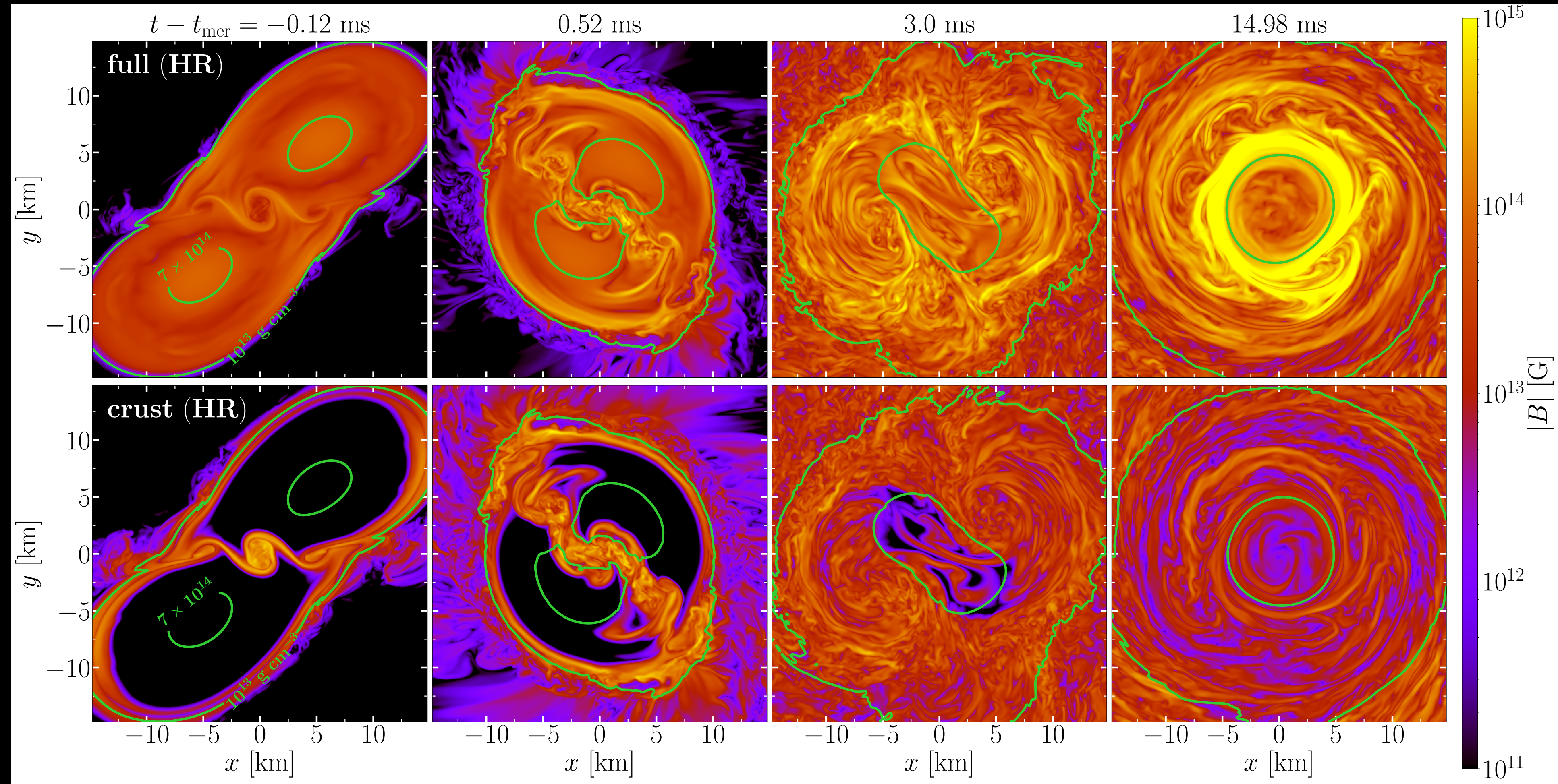
$t - t_{\text{mer}} = -1.142$ ms

crustal

Crust (HR)

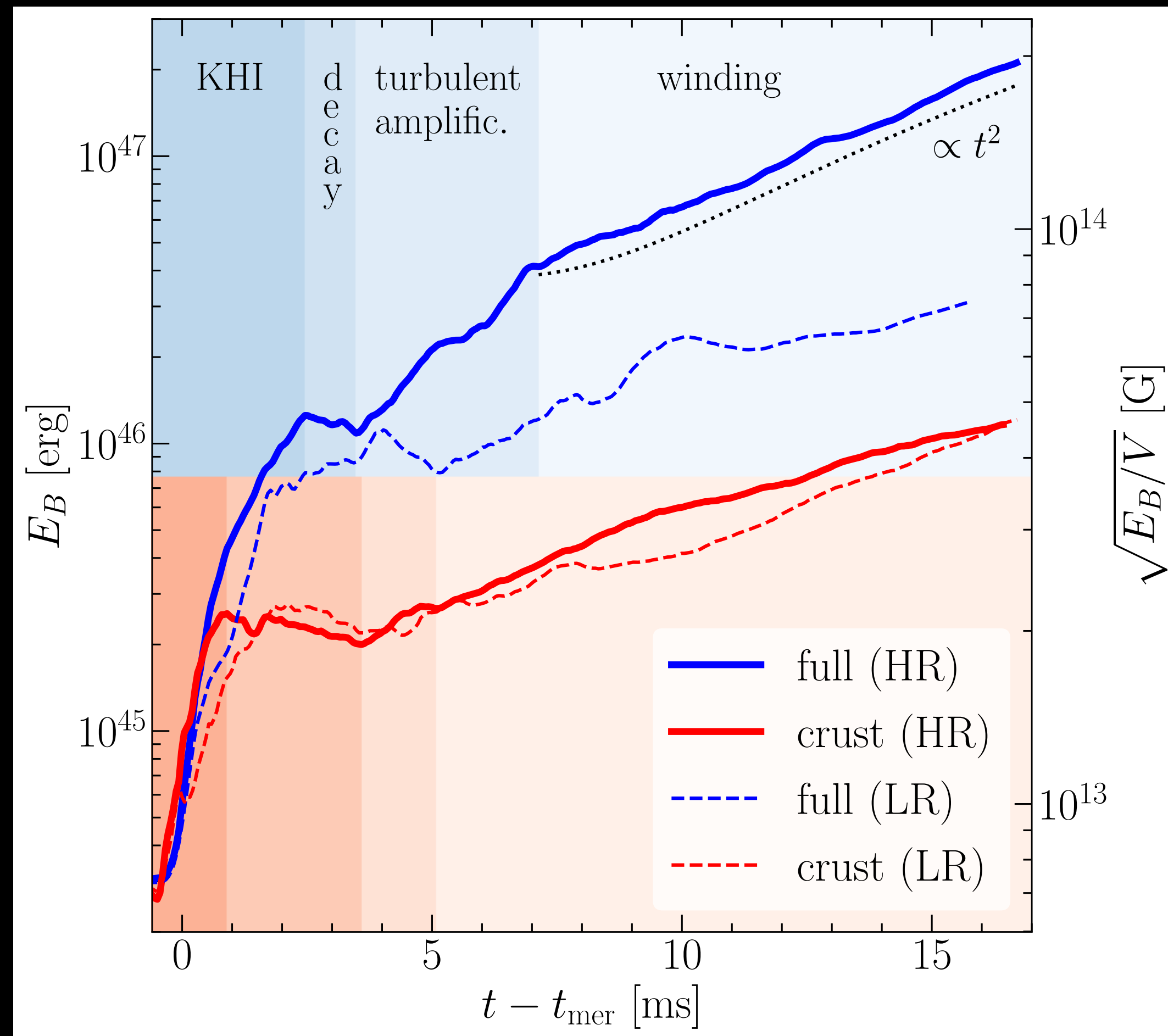


A closer comparison



- significant differences: crustal field is partly lost at the surface and not further amplified by interior turbulence

A more quantitative description

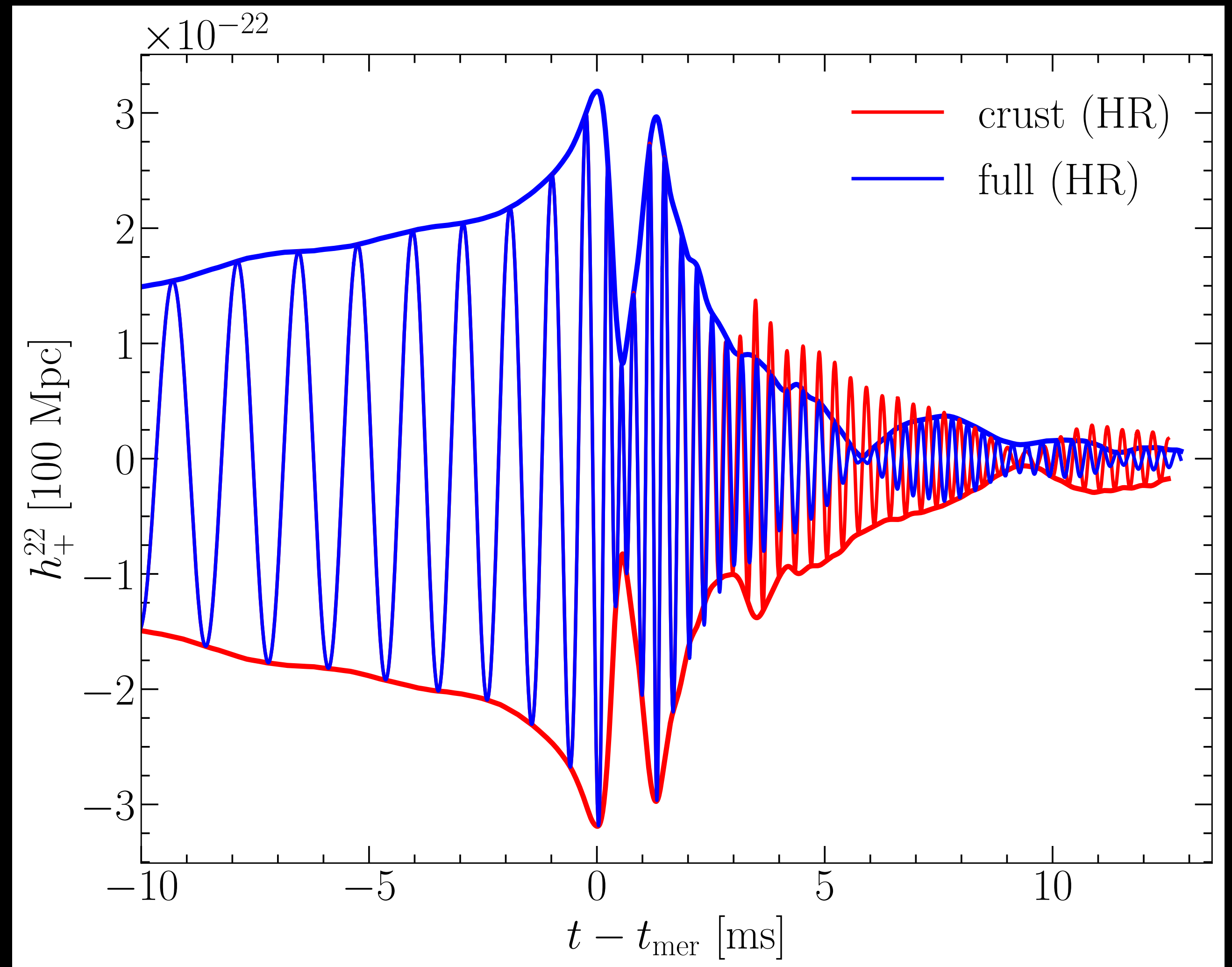


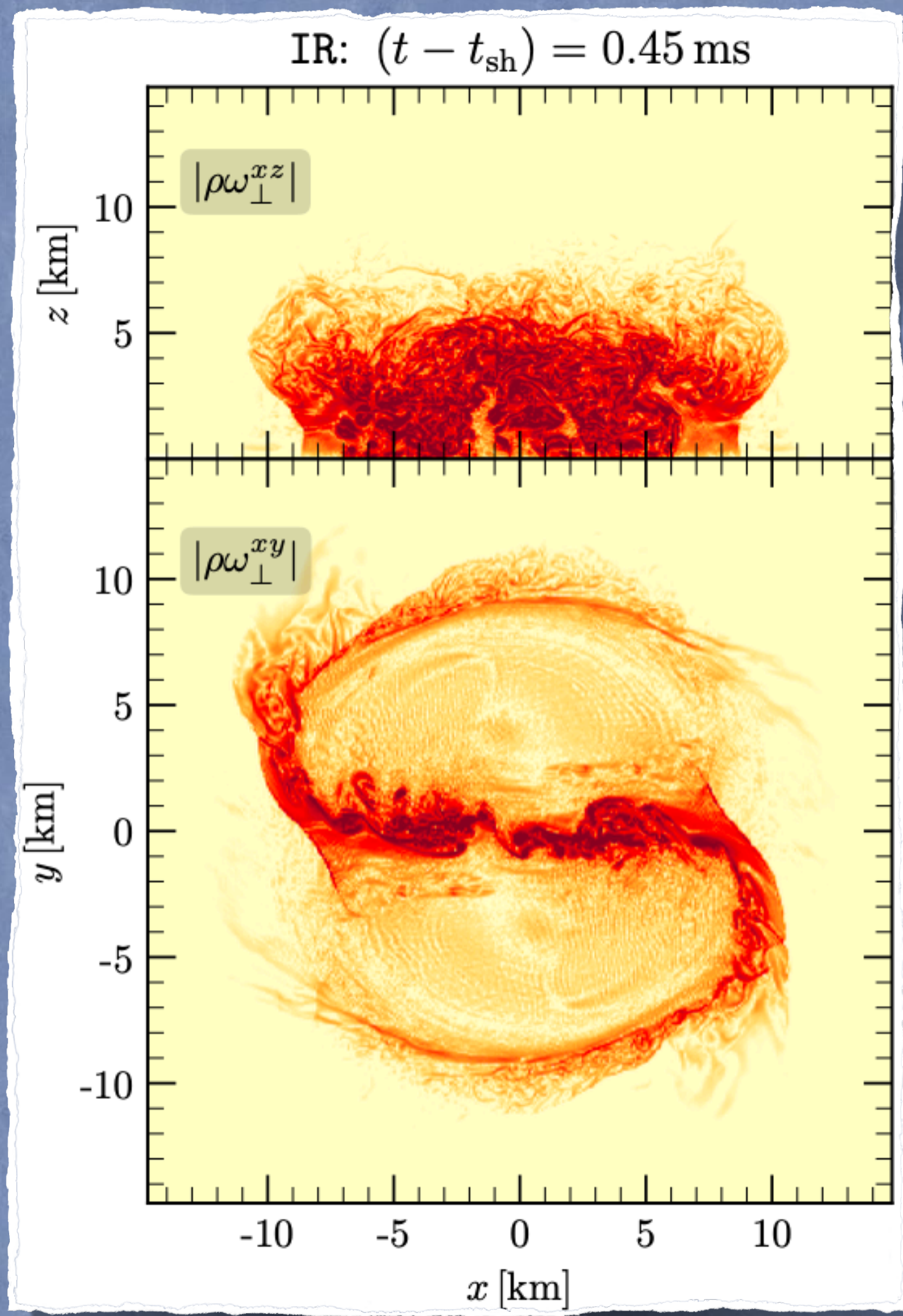
- crustal fields are initially more efficient in amplifying the B-field
- however, their amplification is quickly quenched because of mass loss not present in full fields
- when a shearing amplification is active, i.e., $t - t_{\text{mer}} \gtrsim 5$ ms, crustal fields are one order of magnitude weaker

Bottom line: crustal magnetic fields **do not** lead to large magnetic-field amplifications in BNS mergers

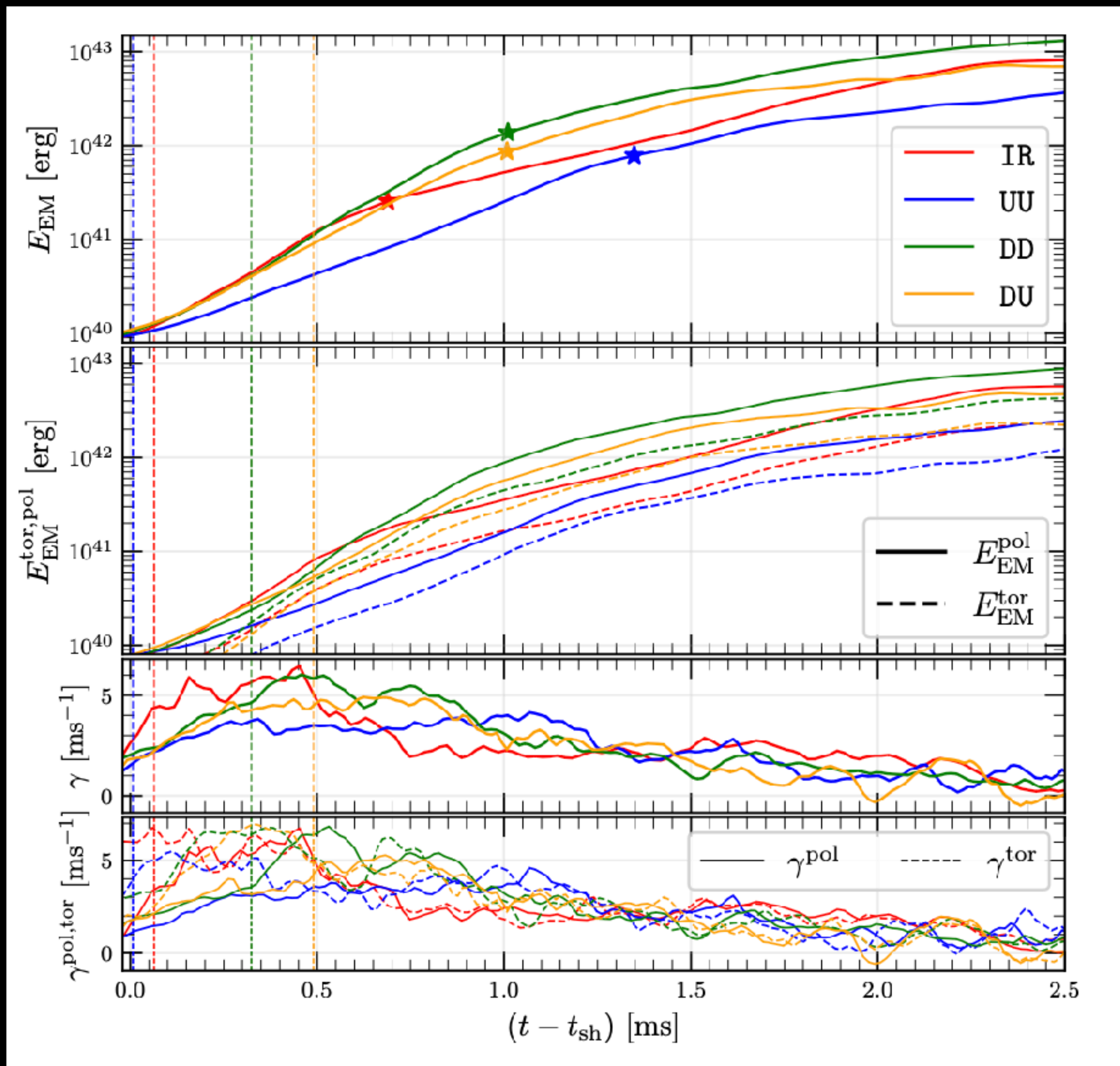
How can we tell the difference?

- different magnetic fields in the remnant will lead to different (weaker) EM emission
- GWs will also be different: weaker for full configuration (more energy into B-field) and smaller $l=2, m=2$ deformations (magnetic tension)



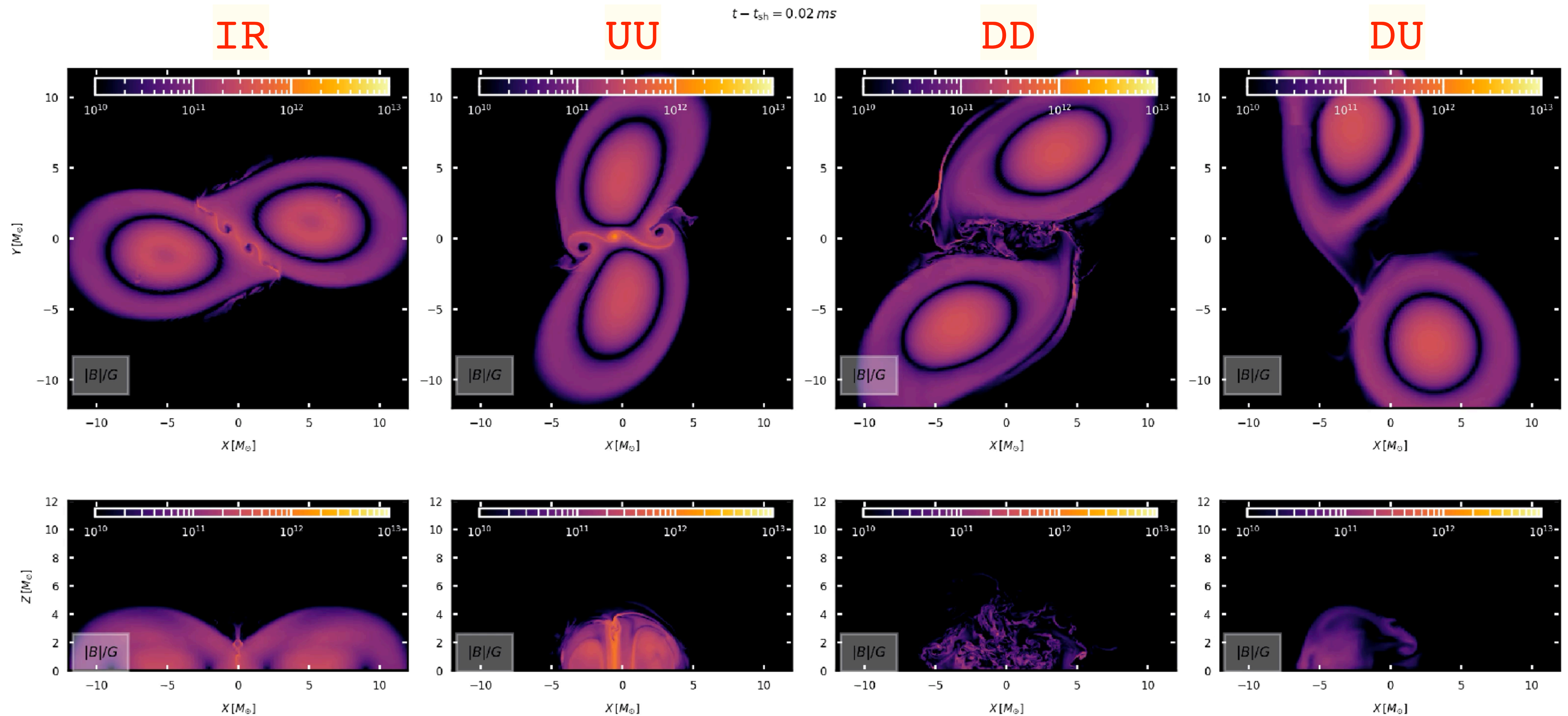


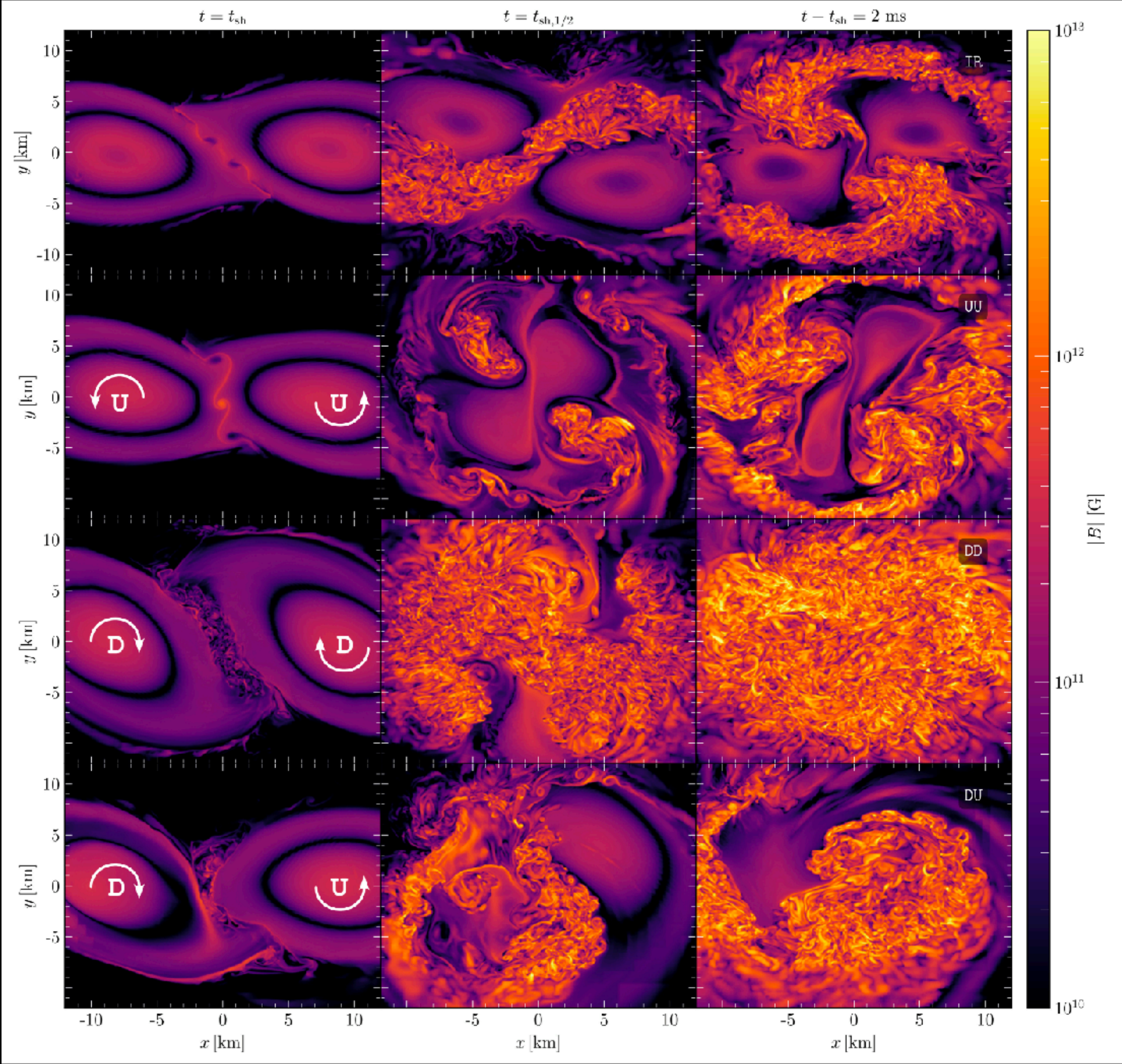
The role of stellar spin in
the B-field amplification



- NSs at merger not expected to have large spins if produced in a binary
- in globular clusters, dynamical capture is potential formation channel
- have considered rapidly spinning stars with aligned/misaligned spins
 - ★ IR (irrot.), UU (↑↑), DD (↓↓), DU (↕↕)
- spin introduces changes also in the inspiral; tidal deformation is different
- Interestingly, both the B-field growth rates and the fields after KHI differ

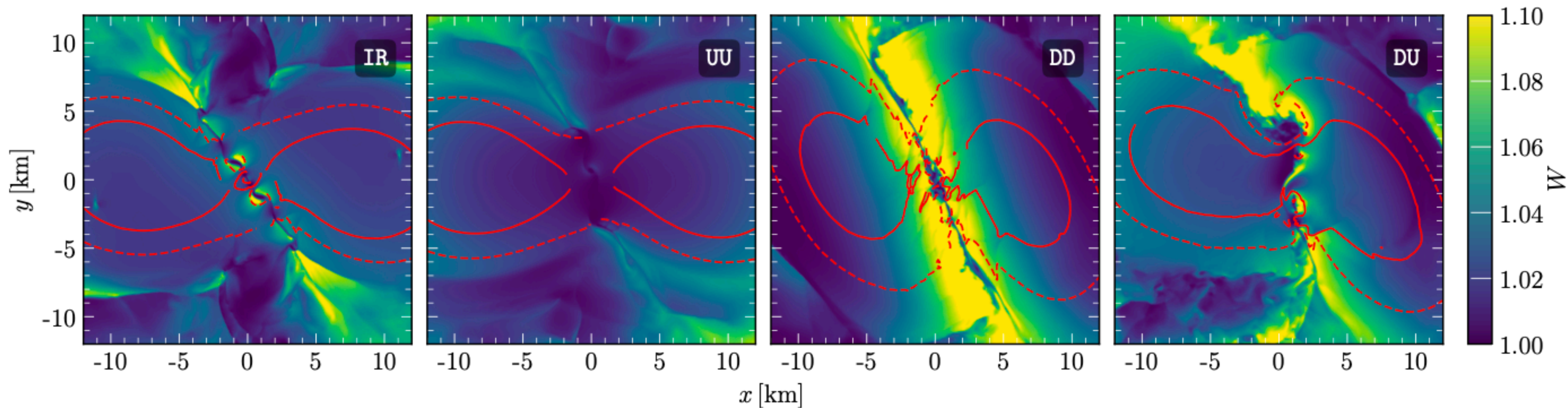
performed ultra-high resolution simulations (35 m)



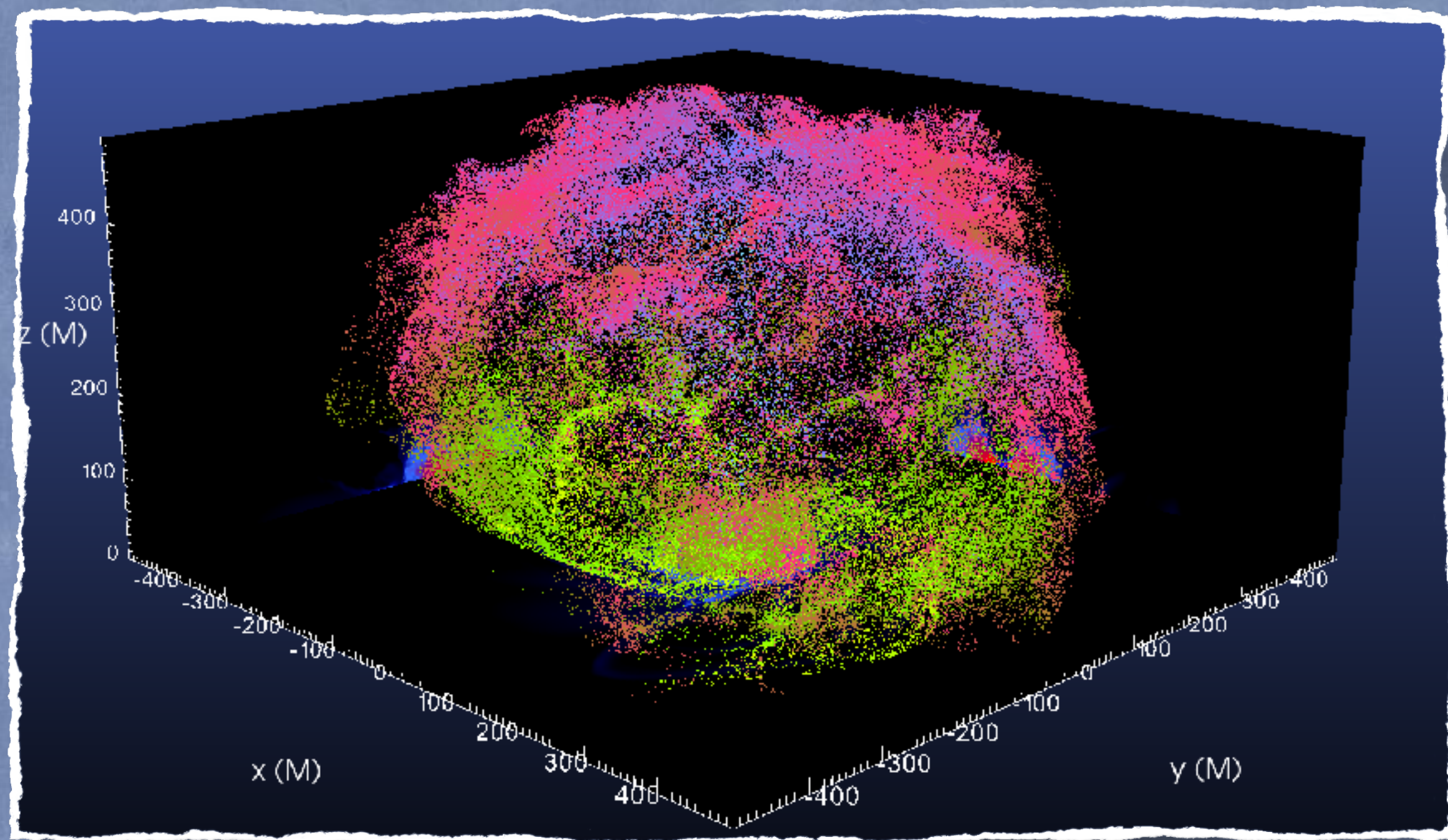


- IR binaries produce considerable vorticity but not the largest
- UU produces smallest vorticity and smallest "final" B-field
- DD produces largest vorticity and largest "final" B-field
- DU produces vorticity only in Ns with misaligned spin

Why this different behaviour?



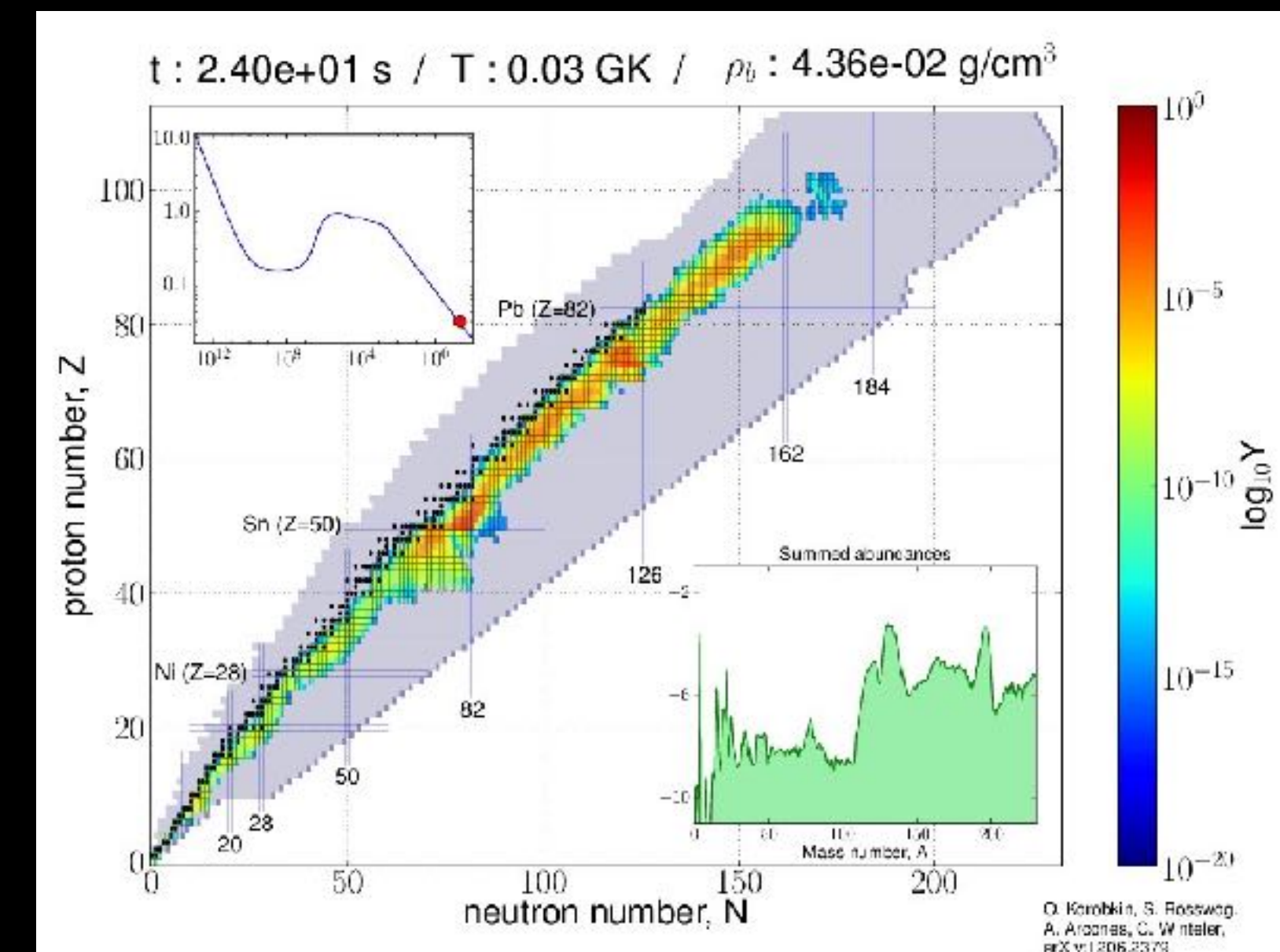
- **intrinsic** tangential discontinuity in UU is large but **contrasted** by **orbital** vorticity
- **intrinsic** tangential discontinuity in DD is also large but **amplified** by **orbital** vorticity
- UU merges with small radial velocity; DD merges with large radial velocity
- larger shocks allow the KHI to shear larger magnetic field with greater magnification



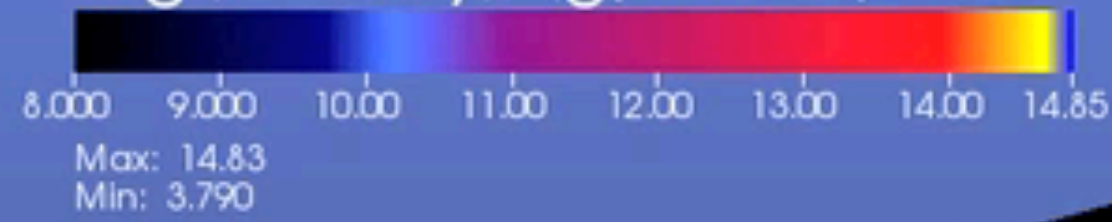
Ejected matter and r-process nucleosynthesis

Heavy-elements nucleosynthesis

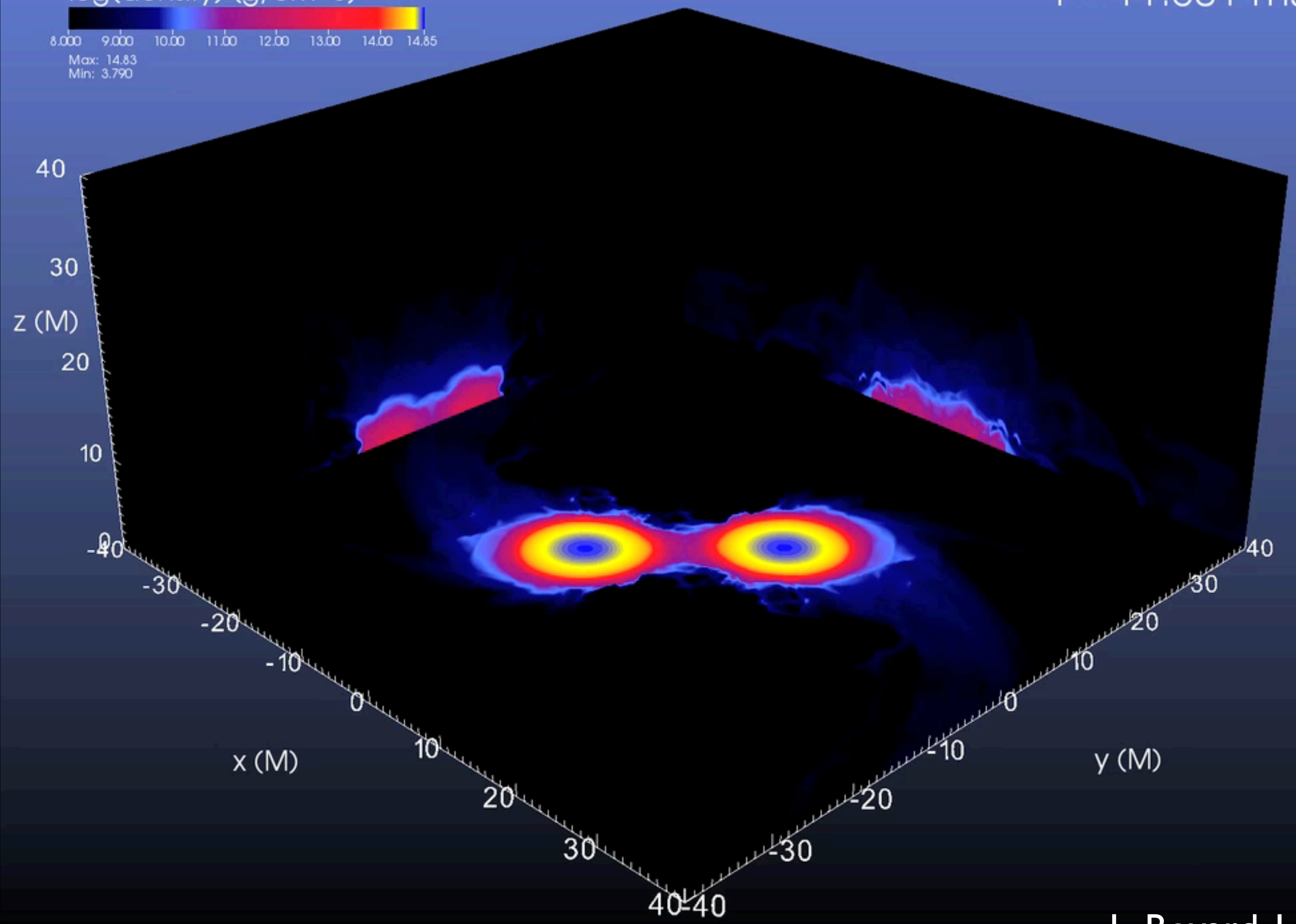
- Already in the 50's, nuclear physicists had tracked the production of **elements** in stars via nuclear fusion.
- **Heavy elements** ($A > 56$) cannot be produced in stellar interiors but can be synthesised during a **supernova**.
- SN simulations have shown that temperatures/energies not enough to produce **“very heavy” elements** ($A > 120$).
- To produce such elements very high temperatures and **“neutron-rich”** material is needed.
- Physical conditions in **neutron-star mergers** are perfect candidates for this process!



log(density) (g/cm³)

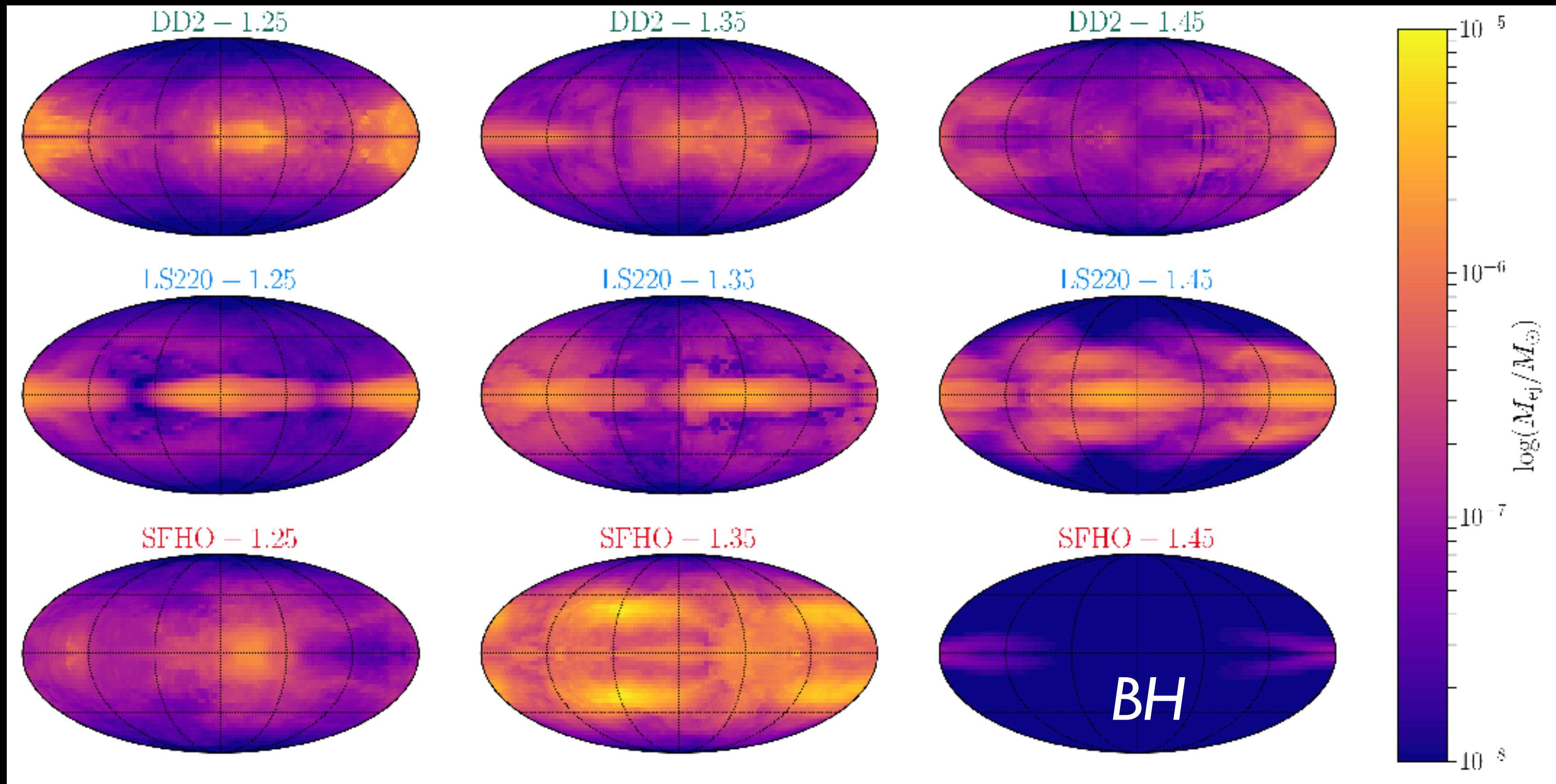


t = 11.801 ms



L. Bovard, LR

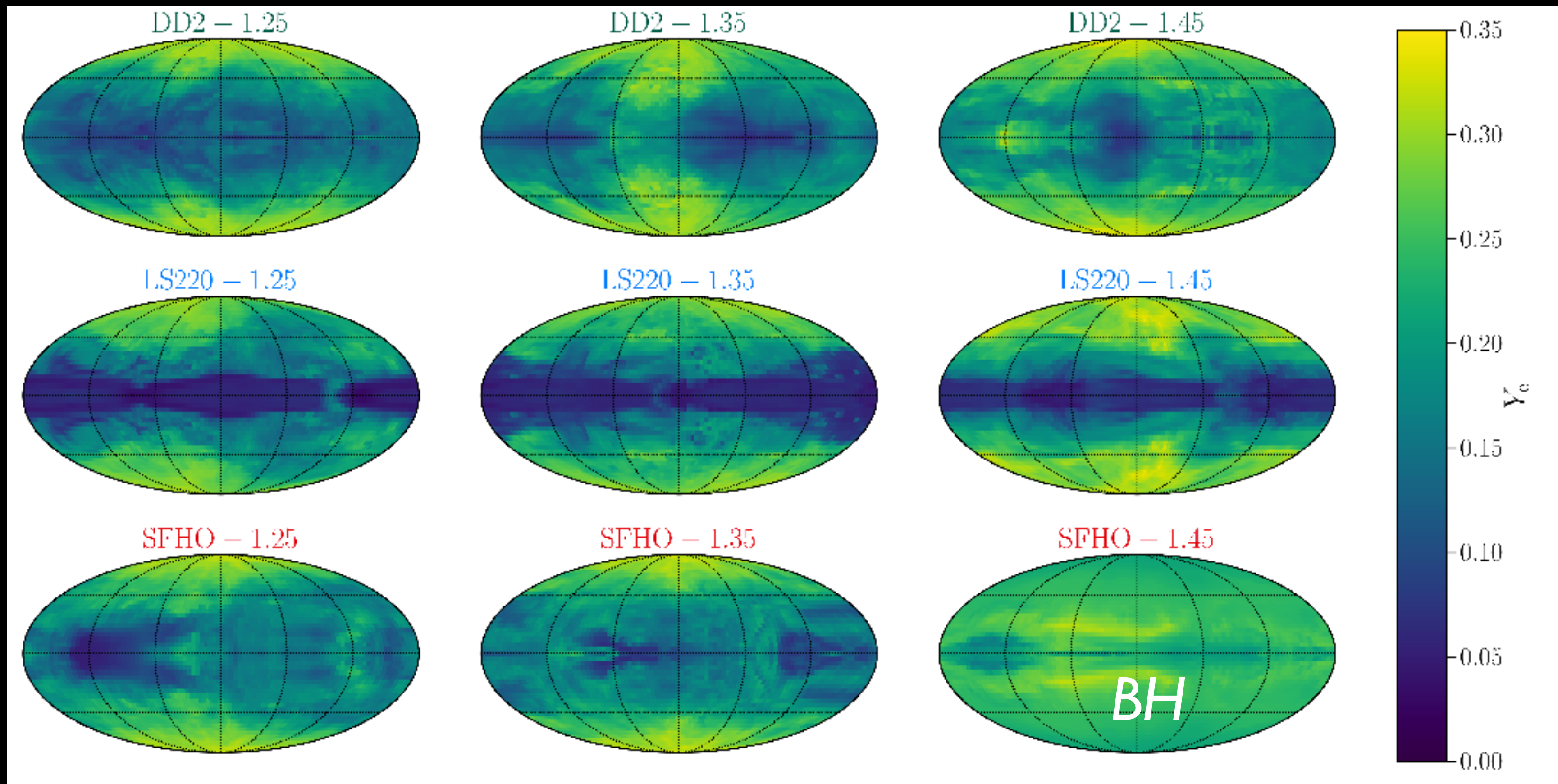
Spatial distributions: M_{ej}



Spatial distribution of M_{ej} impacts detectability of EM counterpart:

- ★ most of M_{ej} lost at low latitudes;
- ★ depending on EOS/mass, contamination also in polar regions

Spatial distributions: Y_e

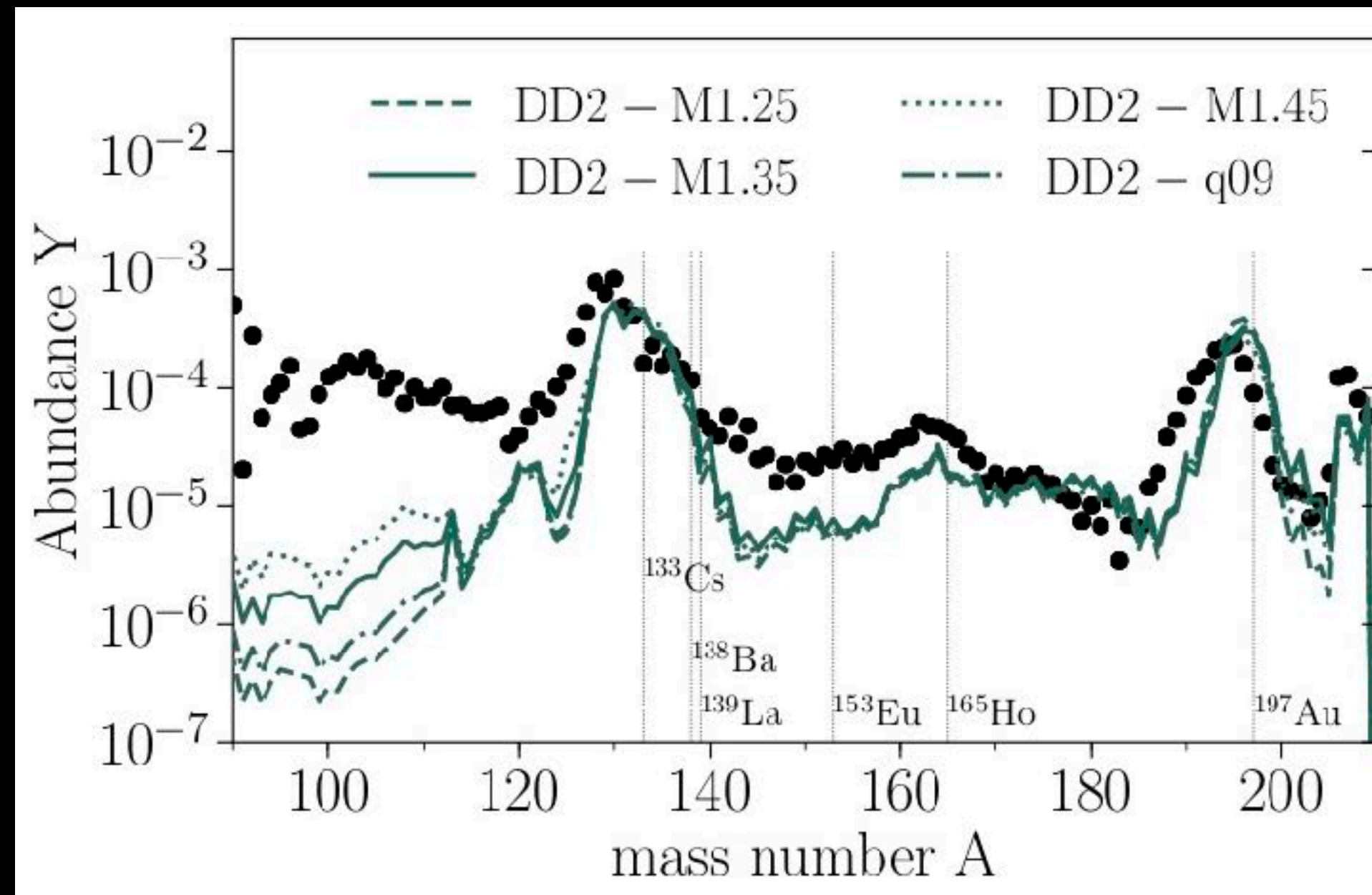


Spatial distribution of Y_e impacts detectability of EM counterpart:

- ★ high Y_e in polar regions: blue (optical) macronova
- ★ low Y_e in equatorial regions: red (FIR) macronova

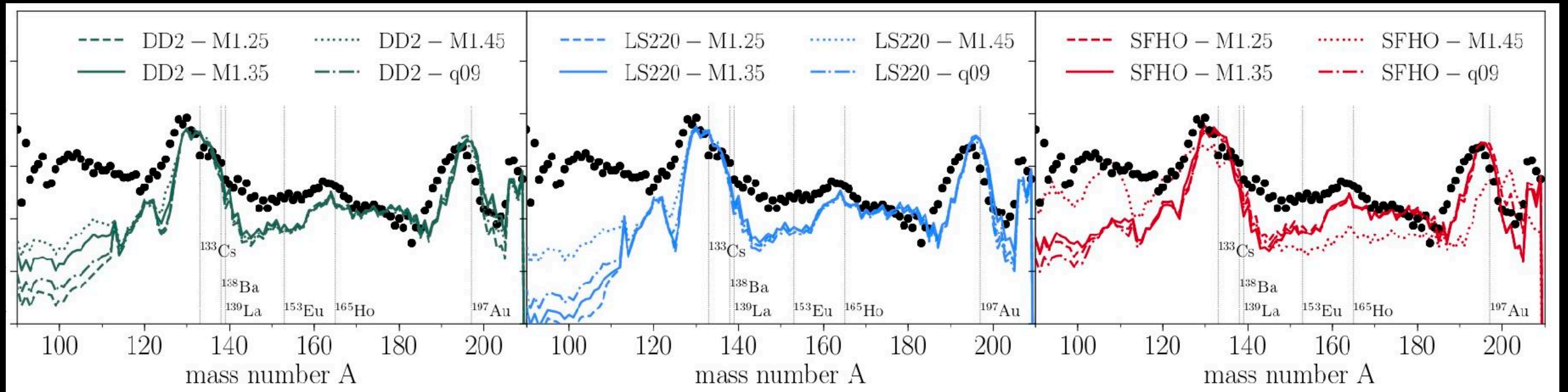
Relative abundances

- Mass ejection can either be **dynamical** (shocks; 100 ms) or **secular** (magnetic or neutrino-driven winds; 1-10 s).
- Even **tiny amounts** of ejected matter ($0.01 M_{\odot}$) sufficient to explain observed abundances.
- Abundances for $A > 120$ good agreement with solar. **robust** for different **EOSs, NS masses, and mass ratios**



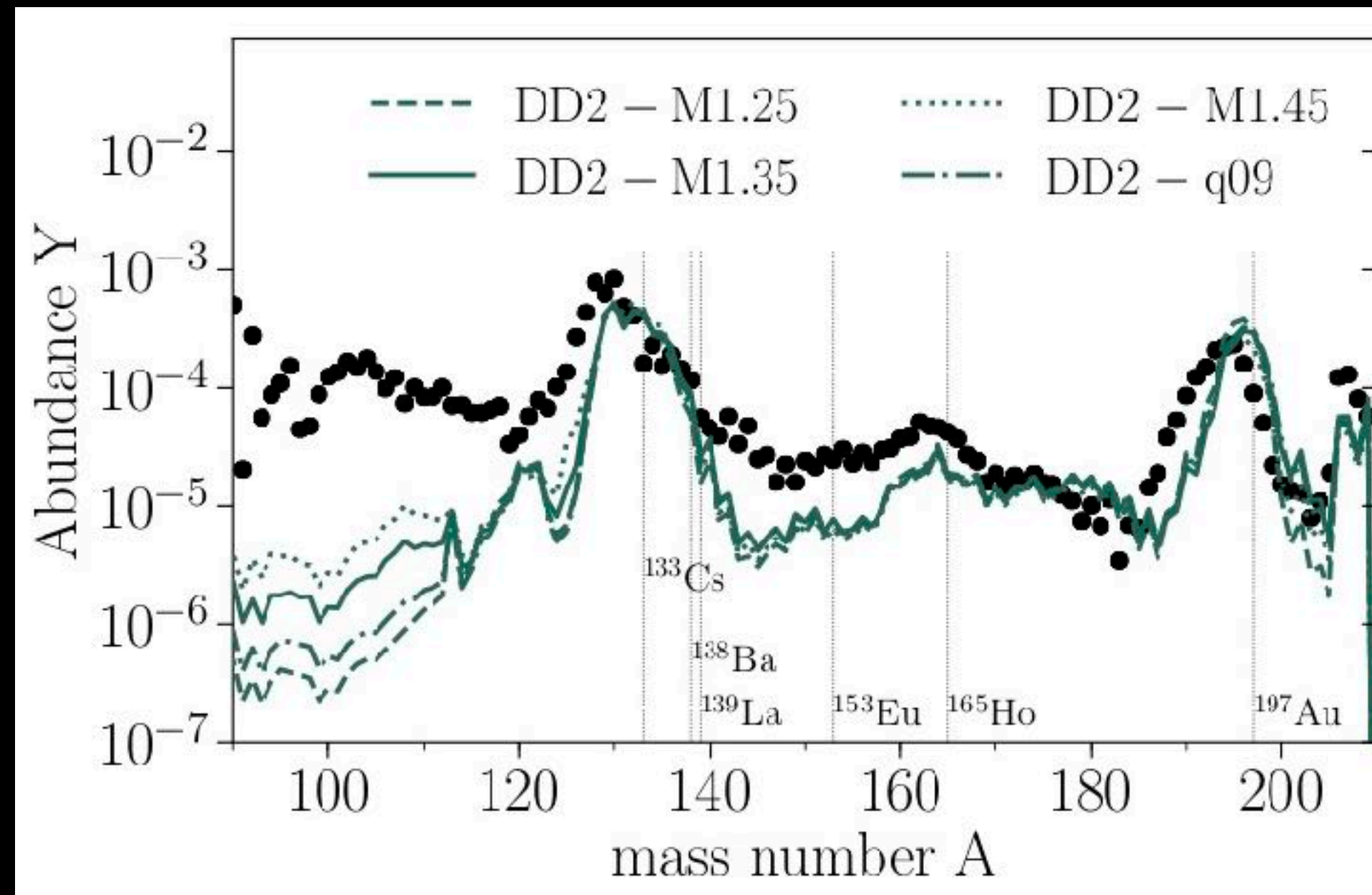
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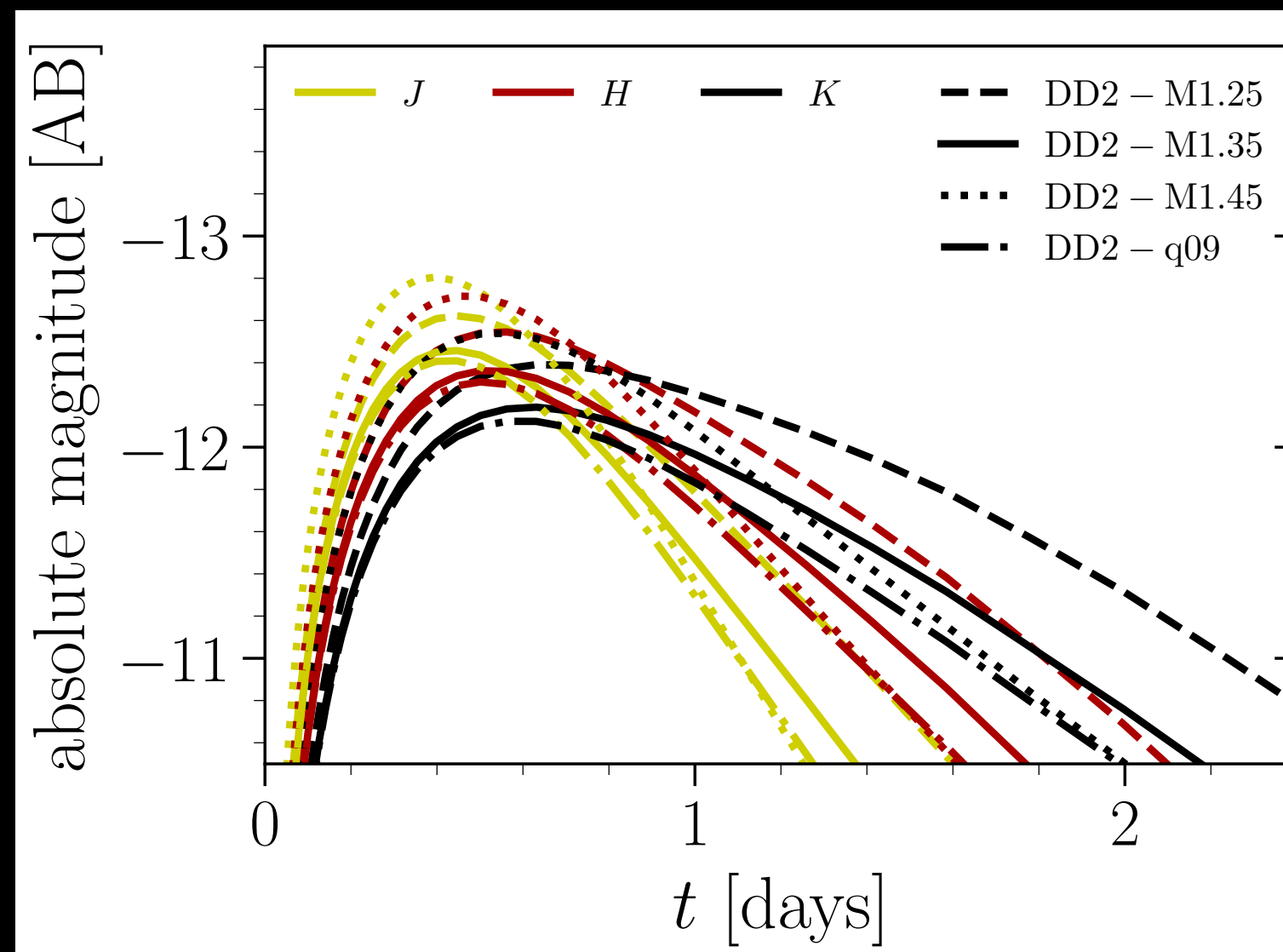
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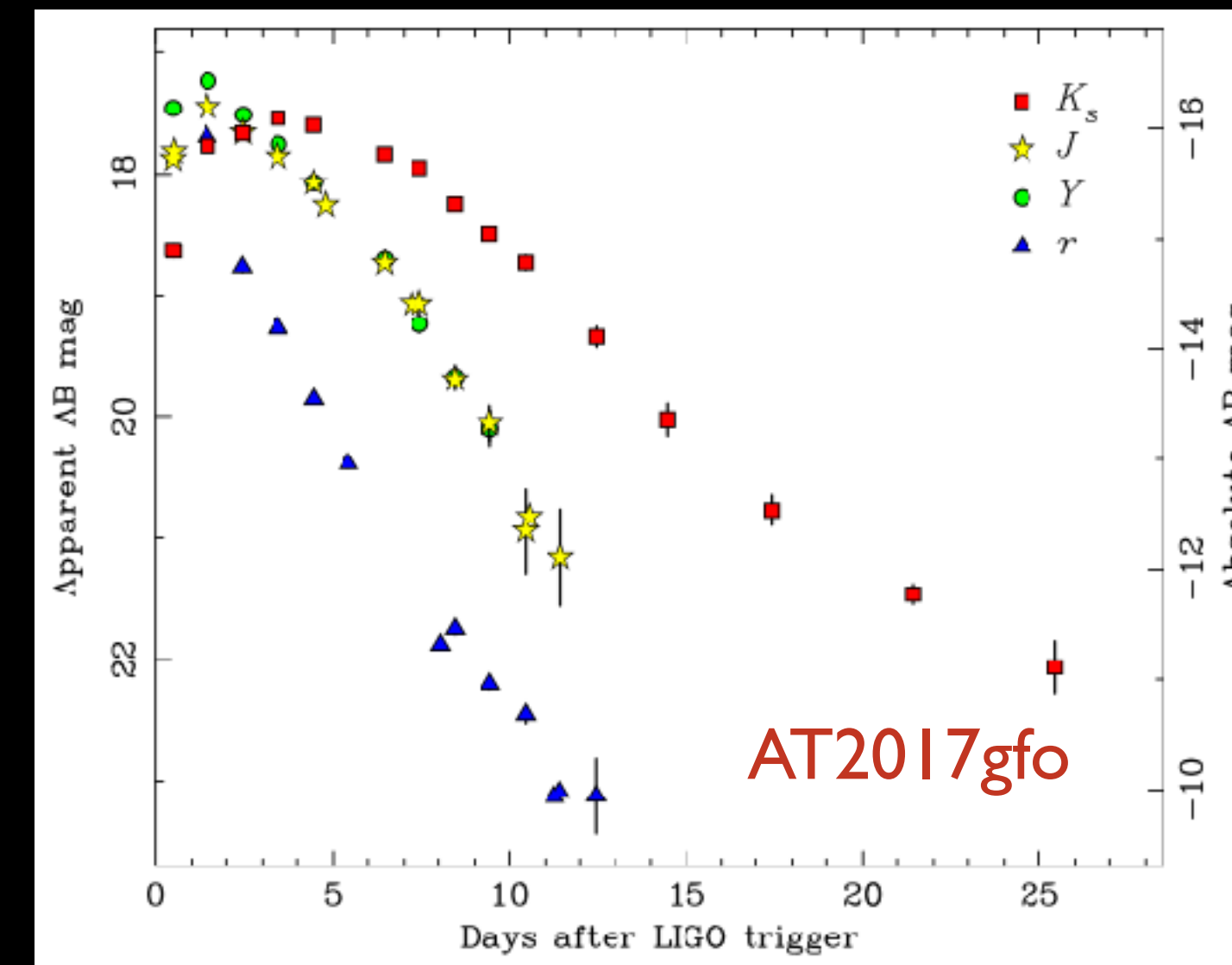
GW170817 produced total of **16,000** times the mass of the Earth in heavy elements (**10** Earth masses in **gold/platinum**)

Kilonova emission

- Besides nucleosynthesis, the ejected matter also provides important EM information.
- When critical densities and temperatures are reached, matter undergoes radioactive decay emitting light (optical/infrared): **kilonova/macronova** (Li & Paczynski '98).



simulations



observations (Tanvir+2017)

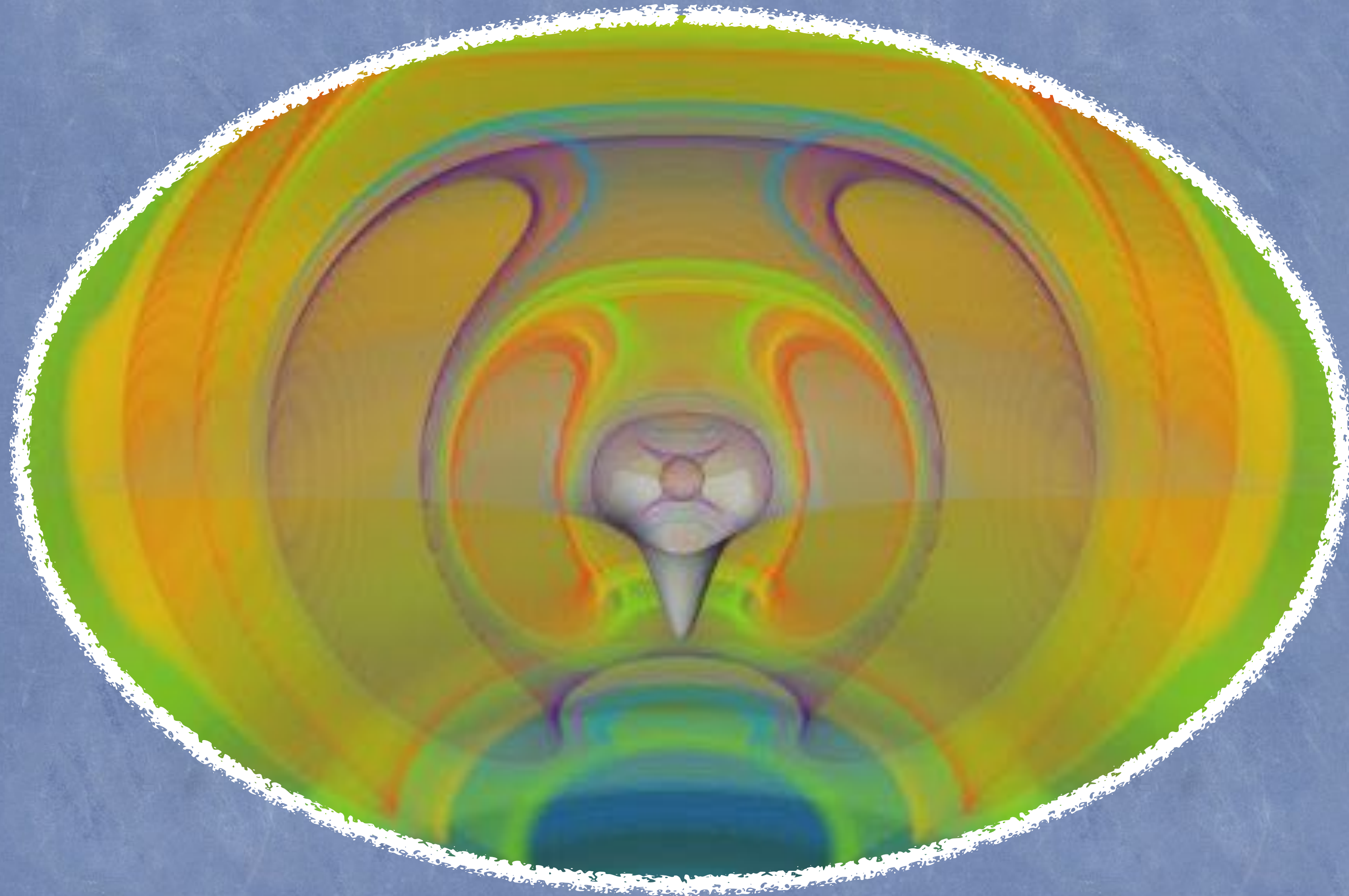
- **AT2017gfo** is kilonova measured with GW170817, showing it was a BNS merger.
- Using simulations, it is possible to reproduce qualitatively the **AT2017gfo** signal

Conclusions

- Inclusion of B-fields and the collapse to a BH, naturally leads to the formation of a **large-scale jet** structure; outflow only mildly relativistic
- **KHI** represents efficient way of **amplifying** B-fields from small pulsar-scale values (10^{10} G) to magnetar values (10^{15} G)
- **crustal** magnetic fields **do not** lead to large amplification: precious B-field is ejected at merger
- **spins** impact KHI; larger B-fields amplifications for **anti-aligned** spins
- r-process nucleosynthesis is **robust** and matches well the **observations**

EXTRAS

On the maximum compactness



How compact can a **realistic** neutron star be?

This is a very old question and we have a very important limit in general relativity (Buchdahl Theorem)

$$\frac{M}{R} \leq \frac{4}{9} \simeq 0.444$$

We could ask this question for the 10^6 **EOSs** we have constructed

However, compactness can change as a function of mass and a criterion is needed to compare the maximum compactness

How compact can a **realistic** neutron star be?

To address this question we formulate the following **conjecture**

$$\mathcal{C}_{\max} = \mathcal{C}_{\text{TOV}}$$

In other words the **maximum compactness** is attained by the star with the **maximum mass**.

This condition can be shown to be true for a large number of possible EOSs and a simple theorem can be proven.

More in general, however, it is hard to prove.

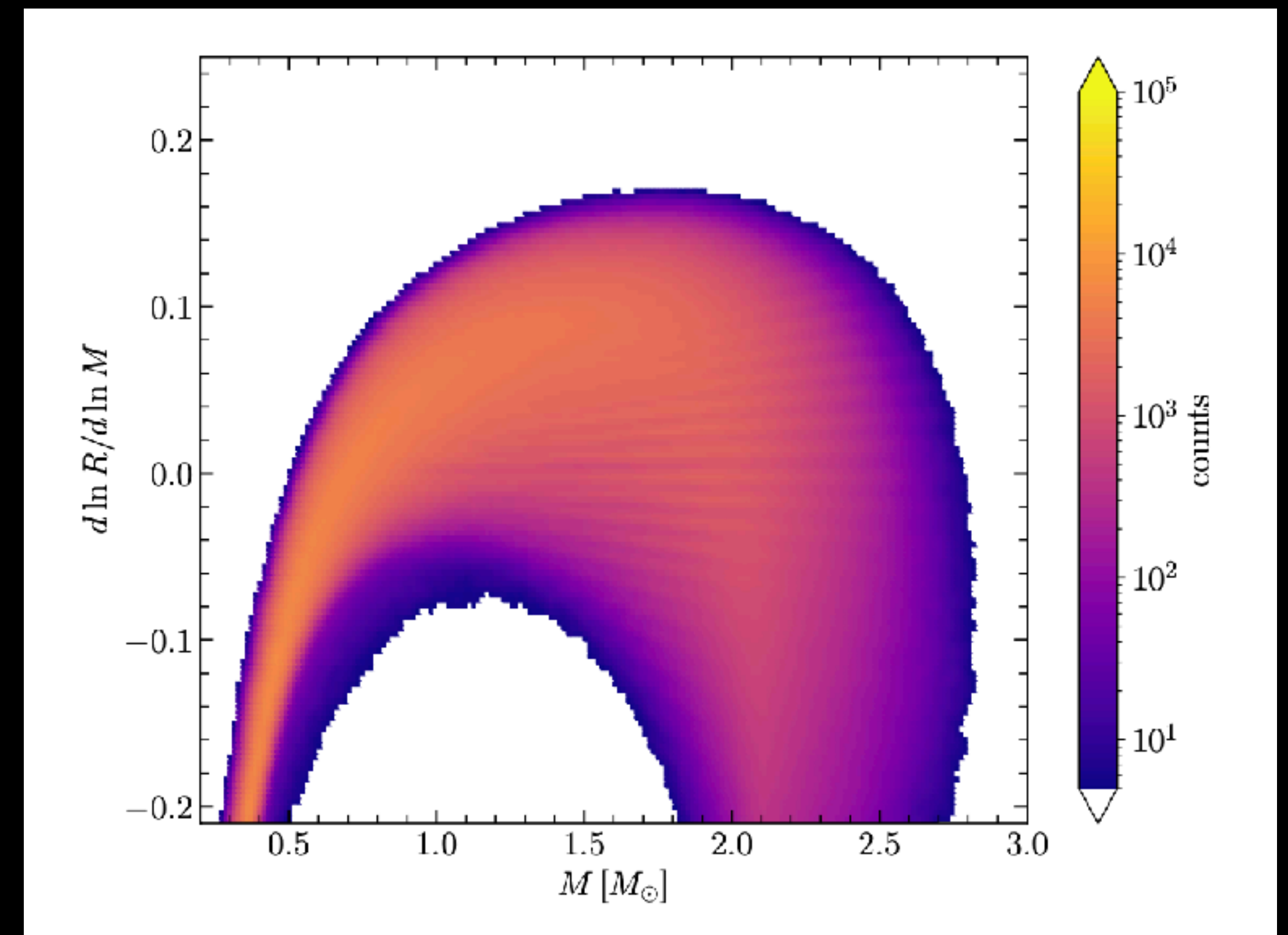
How compact can a realistic neutron star be?

Is the conjecture true for realistic EOSs? The conjecture can be cast as

$$\mathcal{C}_{\max} = \mathcal{C}_{\text{TOV}} \iff \frac{d\mathcal{C}(M)}{dM} = \frac{1}{R(M)} \left(1 - \frac{d \ln R}{d \ln M} \right) \geq 0.$$

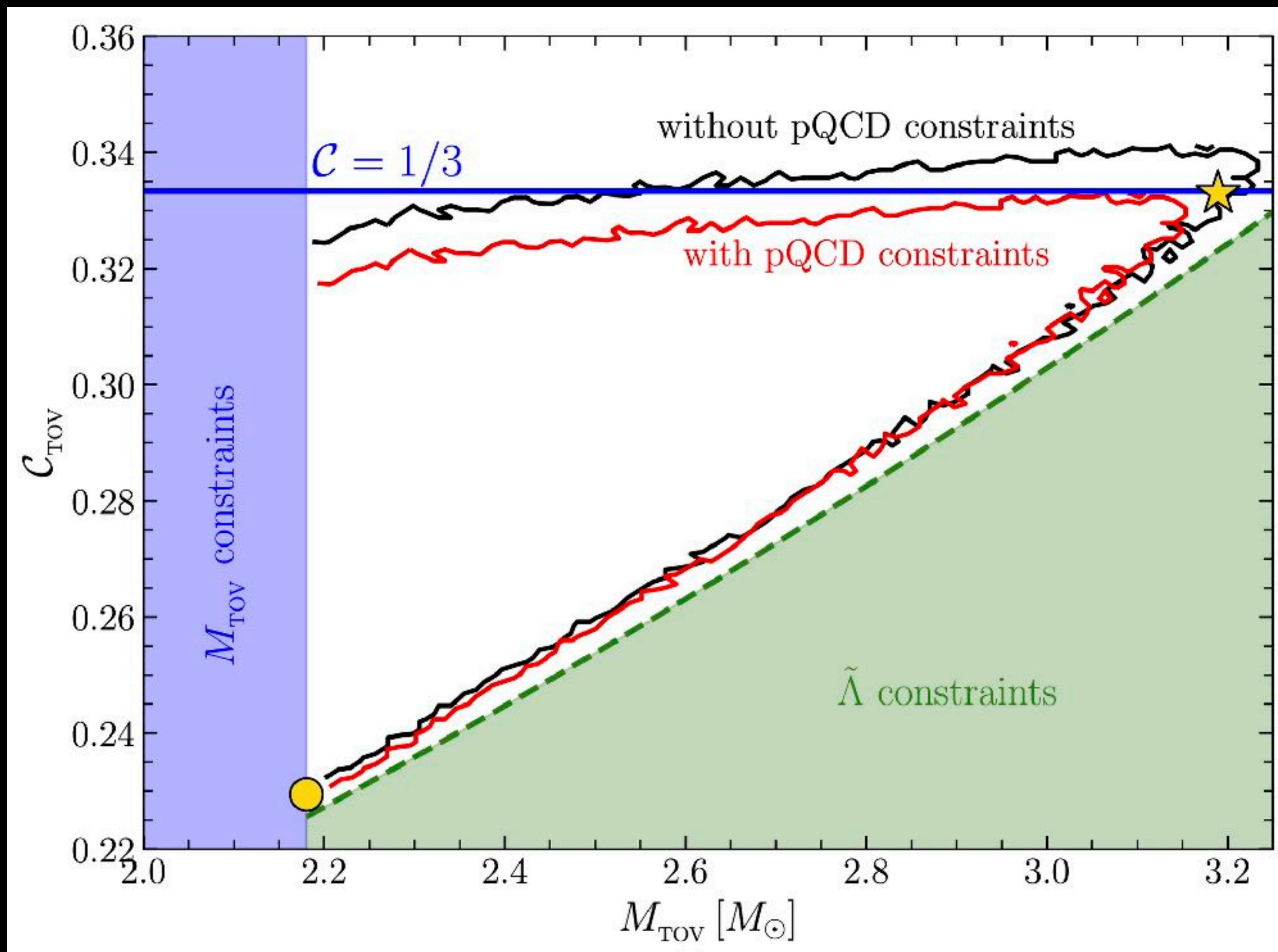
All we need to check is whether the term in the round brackets is validated by all our stellar models.

Hence, the conjecture is far more solid than a conjecture...



How compact can a realistic neutron star be?

We can finally answer the question

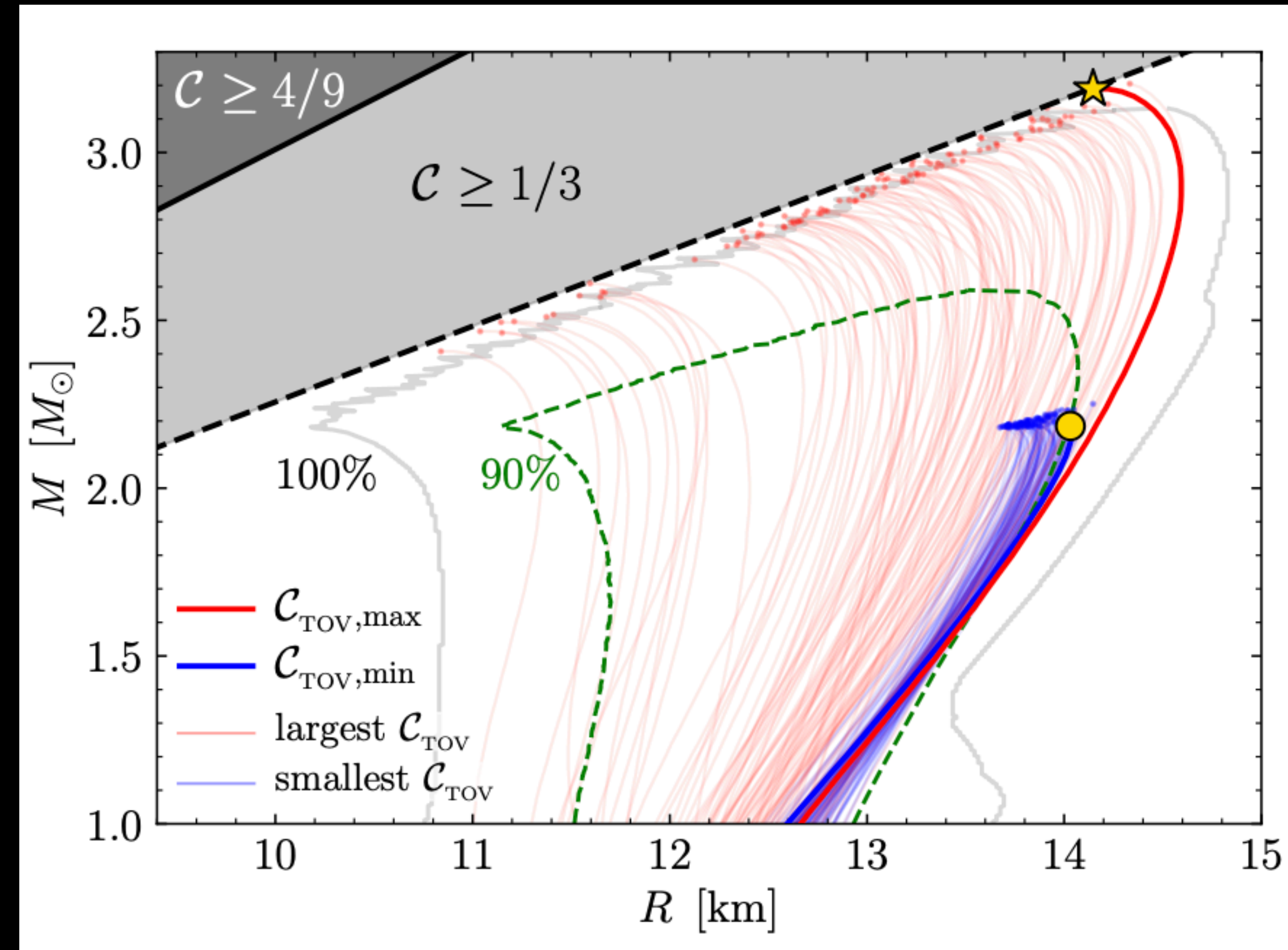
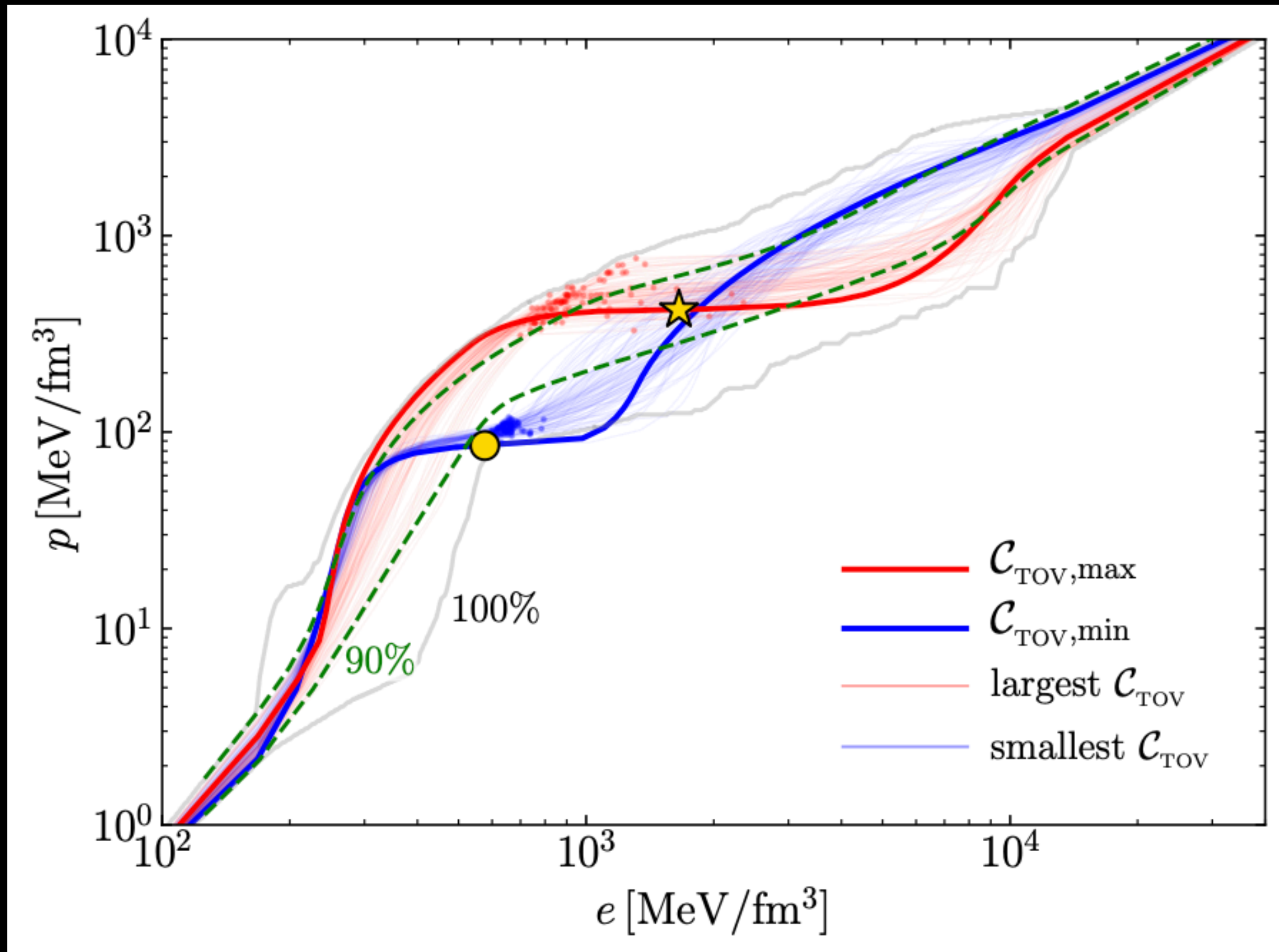


If the pQCD constraint is imposed, the evidence is that

$$c \leq 1/3$$

Violation of this bound would provide important information: anomalous QCD behaviour at largest densities

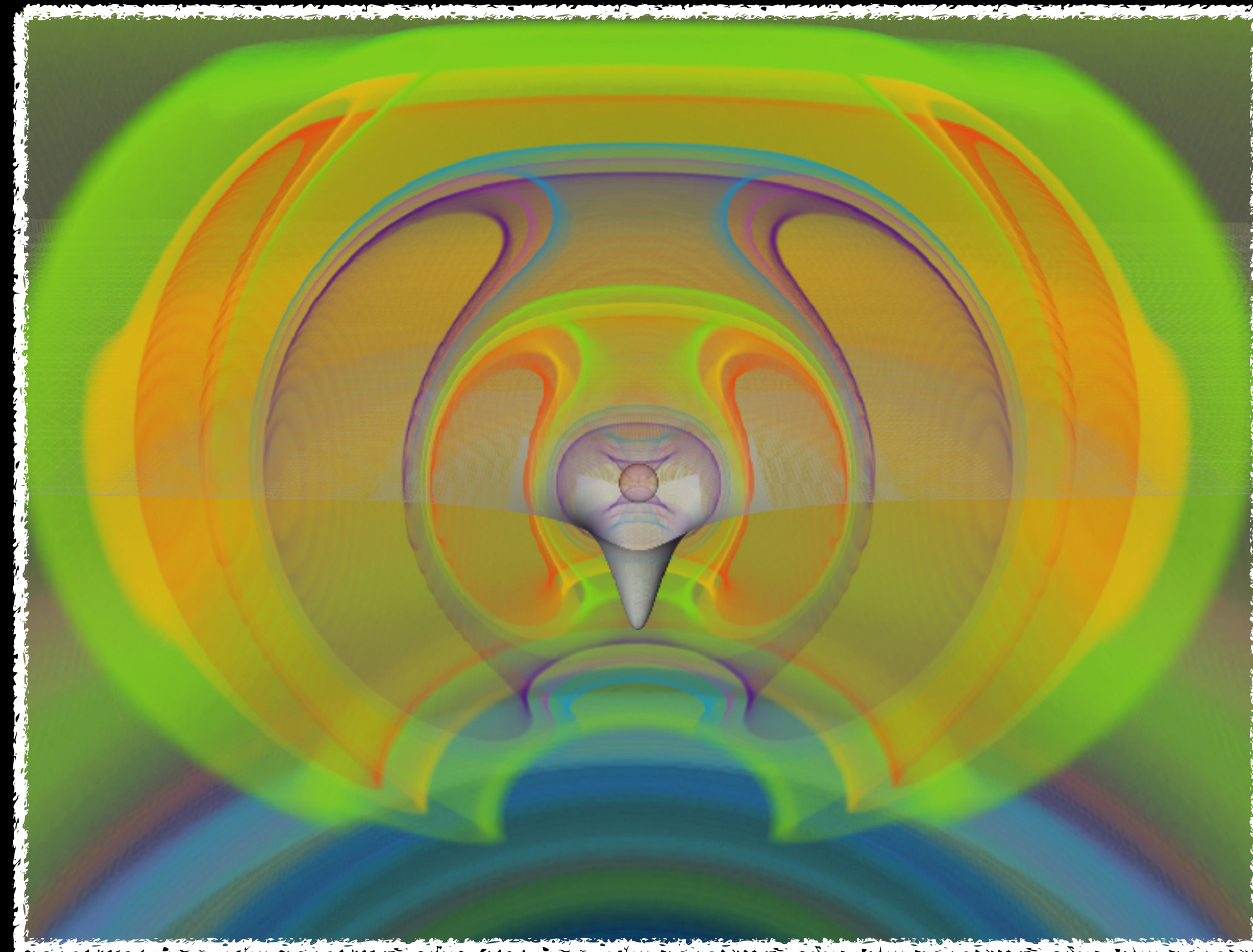
How compact can a realistic neutron star be?



Conclusions

- Spectra of post-merger shows peaks, some "quasi-universal".
- When used together with tens of observations, they will set tight constraints on EOS: radius known with ~ 1 km precision.
- A **phase transition** after a BNS merger leaves GW **signatures** and opens a gate to access quark matter beyond accelerators.
- The sound speed is likely to be **super-conformal** in a NS and its maximum value is reached at the centre/interior for light/heavy stars.
- Long ringdown, is **new tool** to constrain NS properties relating slope and EOS at highest densities and pressures.
- pQCD imprints intriguing upper bound on stellar compactness: $\mathcal{C} \leq 1/3$.

Threshold Mass to prompt collapse

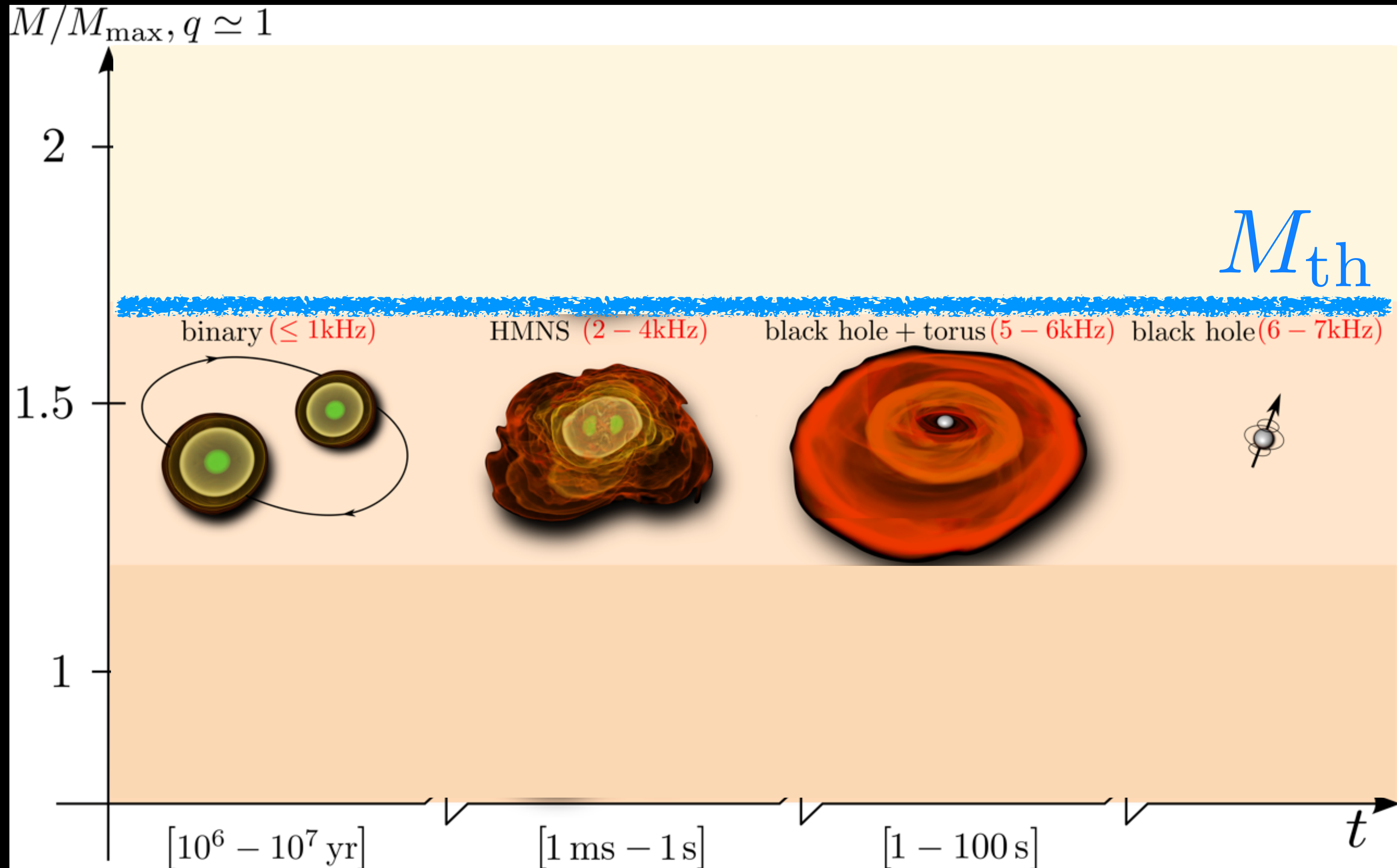


Köppel, Bovard, LR, ApJL (2019)
Tootle, Papenfort, Most, LR ApJL (2021)

A universal behaviour ?

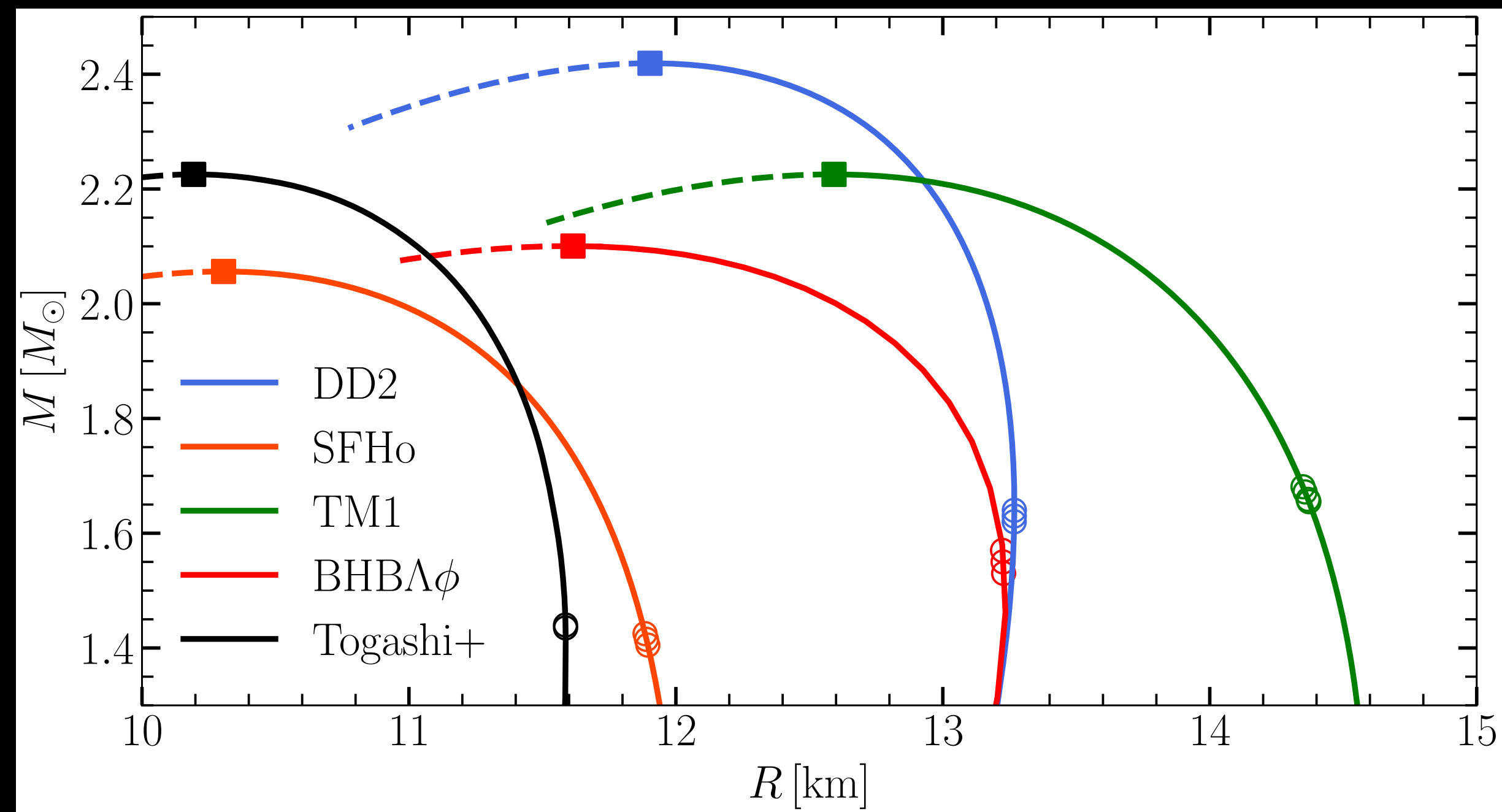
- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal?**

Threshold mass



A universal behaviour?

- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal**?
- 1. Select useful EOSs that self-consistently incorporate **finite-temperature effects**.



A universal behaviour ?

- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal**?
- 2. Determine rigorous definition of **“prompt”** collapse and produce dimensionless quantity

$$t_{\text{coll}} := t_{\text{BH}} - t_{\text{merg}}$$

$$t_{\text{merg}} : \quad \min(\alpha) = \alpha_{\text{merg}} := 0.35 ,$$

$$t_{\text{BH}} : \quad \min(\alpha) = \alpha_{\text{BH}} := 0.2 .$$

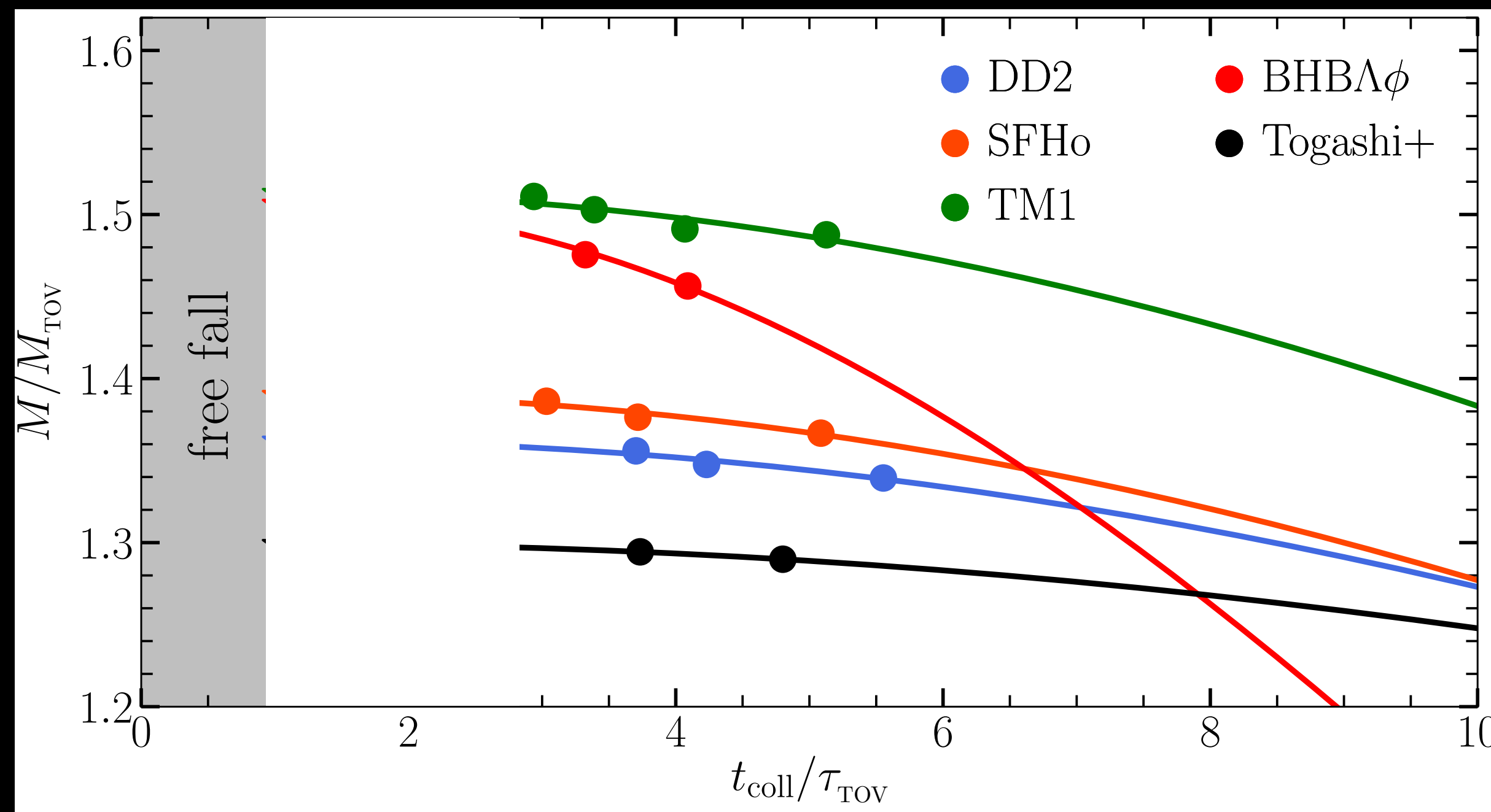
extremely robust and EOS
independent

$$\tau_{\text{ff}}(M, R) := \frac{\pi}{2} \sqrt{\frac{R^3}{2M}} .$$

free-fall timescale in
Oppenheimer-Snyder
collapse

A universal behaviour?

- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal**?
- 3. Express measured values in terms of dimensionless collapse time.

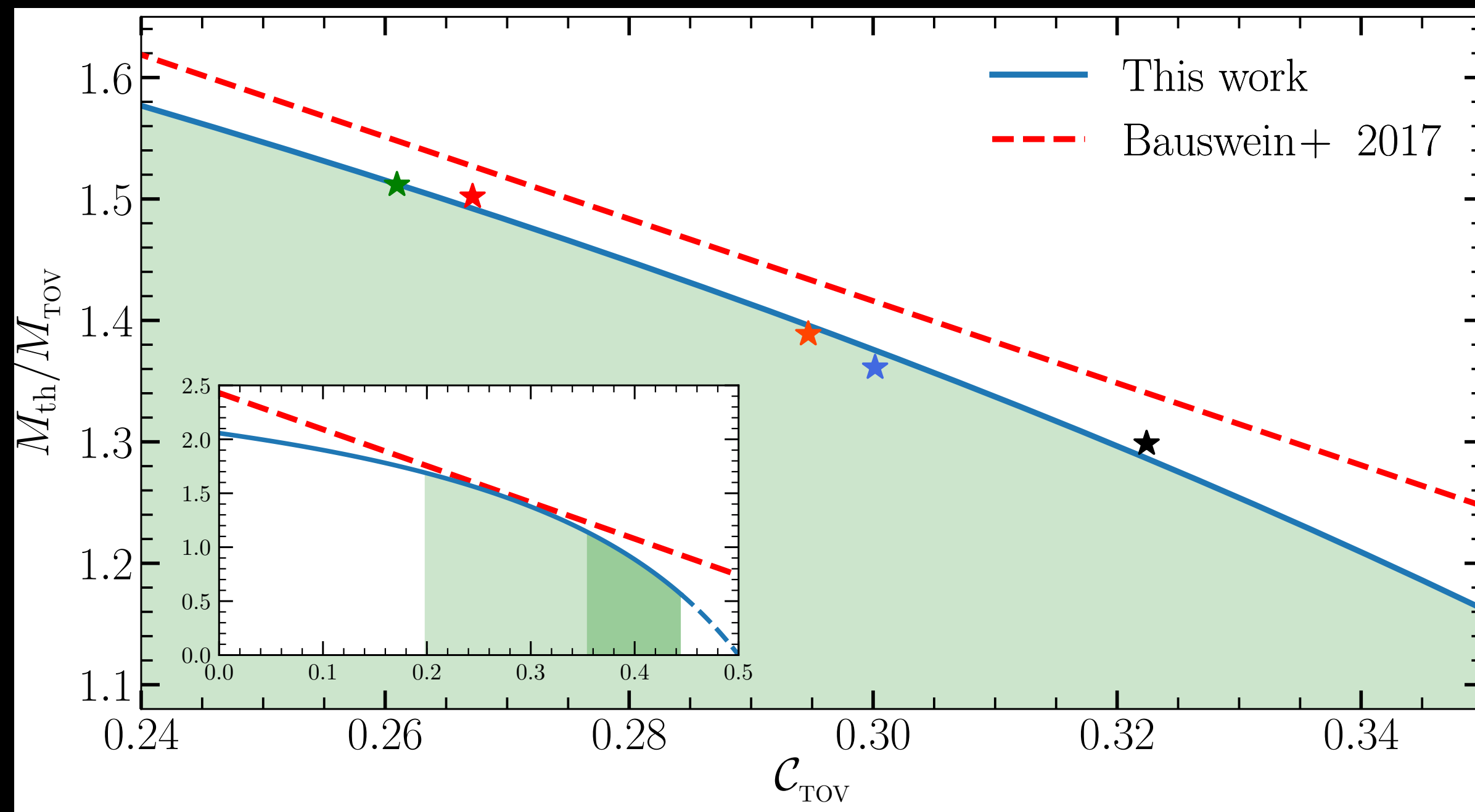


$$\frac{M_{\text{th}}}{M_{\text{TOV}}} \approx 1.415$$

first rough estimate

A universal behaviour?

- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal**?
- 4. Seek universal behaviour via **maximum compactness**.
 $\mathcal{C}_{\text{TOV}} := (M/R)_{\text{TOV}}$. A **linear** fit is possible but not satisfactory. A **nonlinear** fit obtained by requiring that



$$M_{\text{th}}/M_{\text{TOV}} \rightarrow 0$$

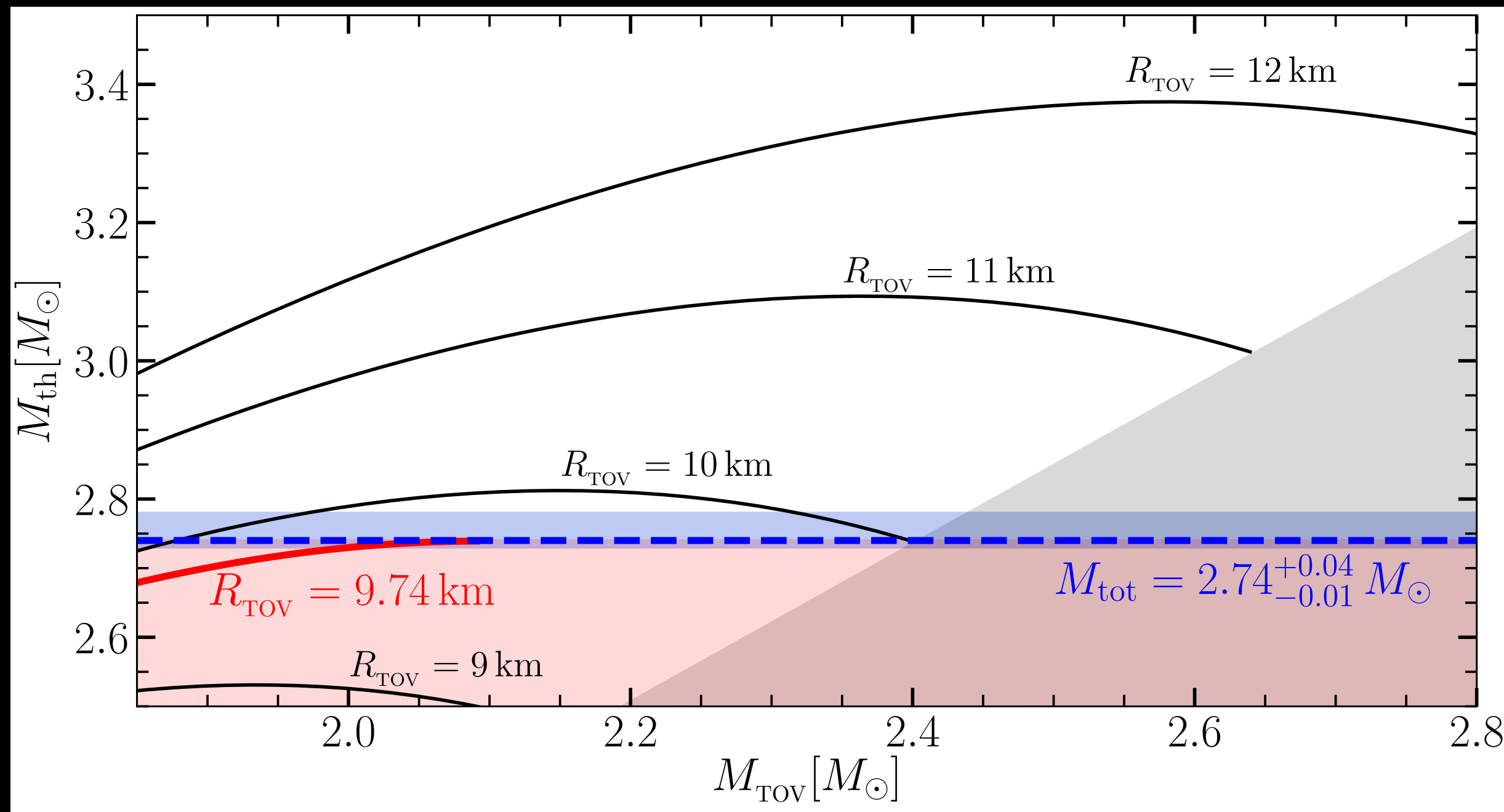
for

$$\mathcal{C}_{\text{TOV}} \rightarrow 1/2$$

$$\frac{M_{\text{th}}}{M_{\text{TOV}}} = a - \frac{b}{1 - c\mathcal{C}_{\text{TOV}}}$$

Another universal behaviour

- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal**?
5. The detection of a merger not leading to prompt collapse **constraints the radius from below**



GW170817

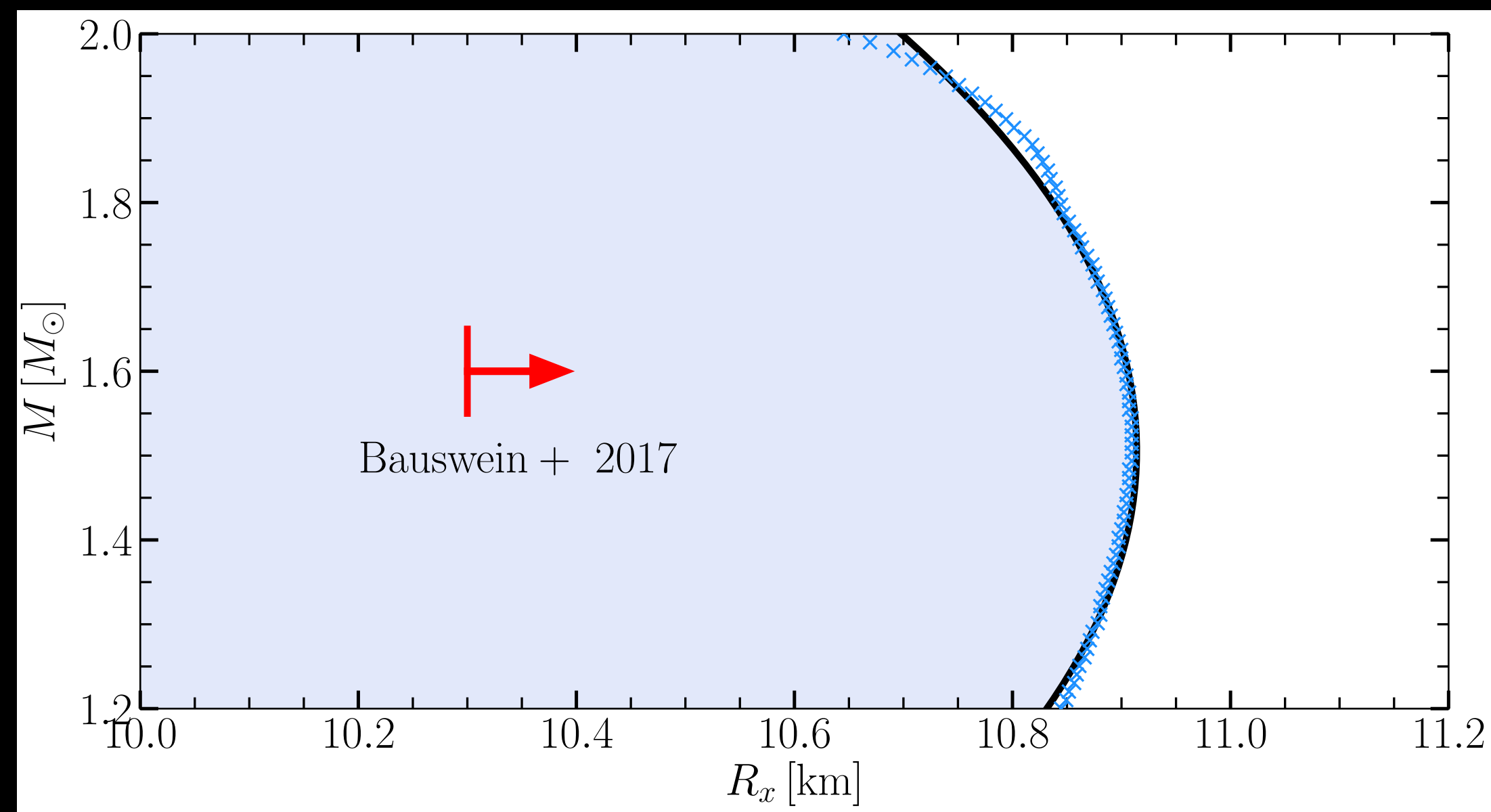
$$M_{\text{tot}} = 2.74^{+0.04}_{-0.01} M_{\odot}$$

so that

$$R_{\text{TOV}} \geq 9.74^{+0.14}_{-0.04} \text{ km}$$

Another universal behaviour

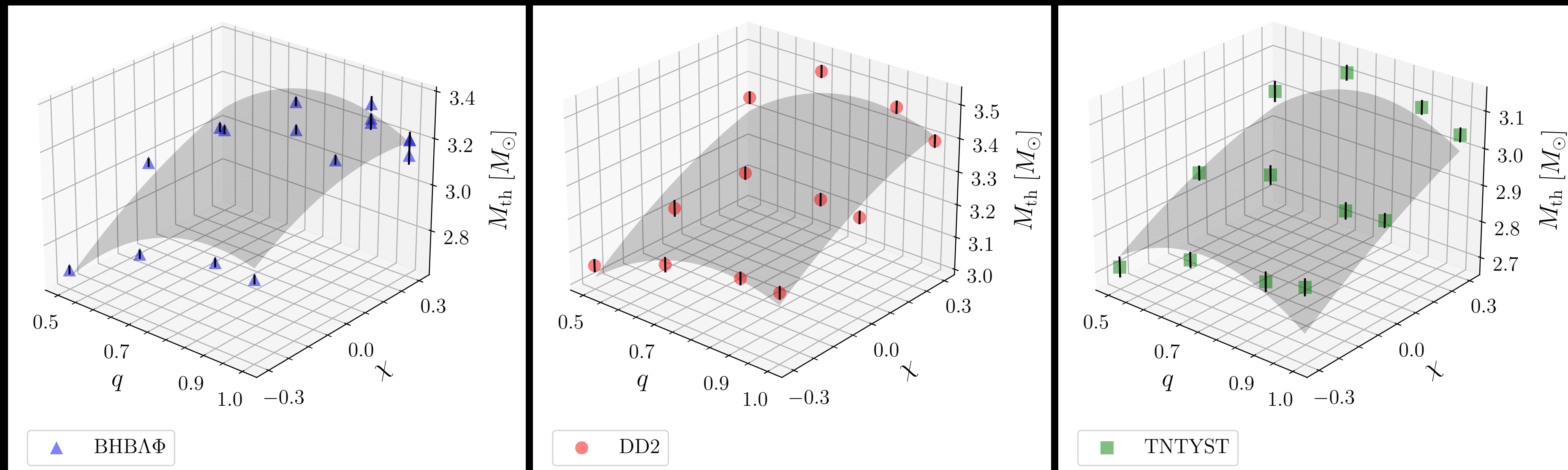
- Given an EOS, a **threshold mass** exists that marks the prompt collapse. Is this **universal**?
- 5. The detection of a merger not leading to prompt collapse **constraints the radius from below**



$$R_x = -0.88 M^2 + 2.66 M + 8.91$$

A more general behaviour

- All results so far true for **irrotational equal-mass** binaries
- M_{th} will depend also on **mass ratio** and **spin**
- Intuitively, M_{th} increases with **positive spin** and **mass ratio**
- We have considered **40** configurations, **360** simulations



Clearly, $M_{\text{th}} = M_{\text{th}}(\text{EOS}, q, \chi)$

A more general behaviour

Is this behaviour **universal**?

Assume **separable ansatz**

$$M_{\text{th}} = M_{\text{th}}(\text{EOS}, q, \chi) = \kappa(\text{EOS}) f(q, \chi)$$

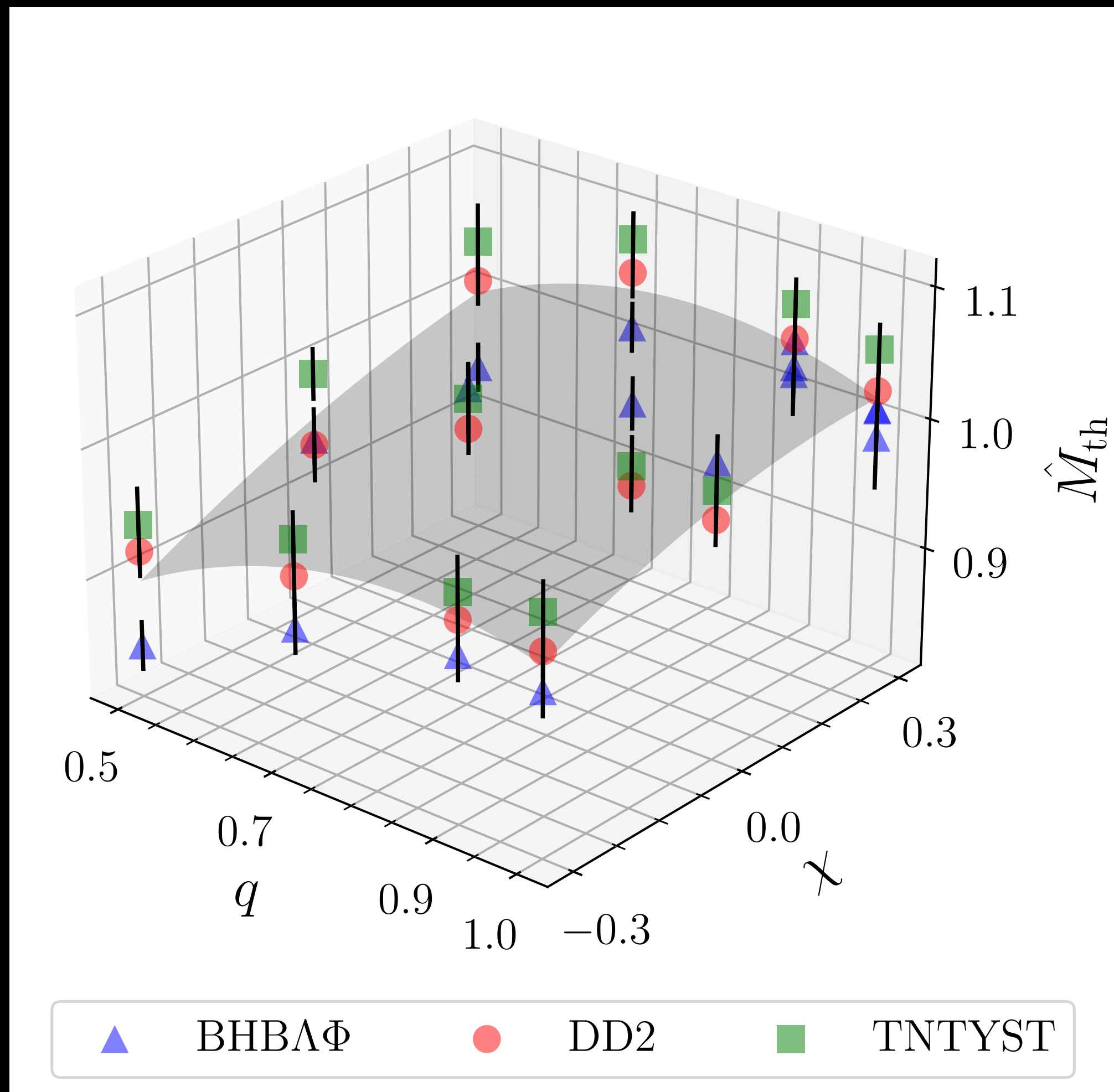
where $\kappa(\text{EOS})$ comes from $q = 1, \chi = 0$ (Köppel+ 2019)

$$\kappa(\text{EOS}) := \left(a - \frac{b}{1 - c\mathcal{C}_{\text{TOV}}} \right) M_{\text{TOV}}$$

and $f(q, \chi)$ is a quadratic function of q and χ

$$f(q, \chi) := a_1 + a_2(1 - q) + a_3\chi + a_4(1 - q)\chi + a_5(1 - q)^2 + a_6\chi^2$$

Does this work?



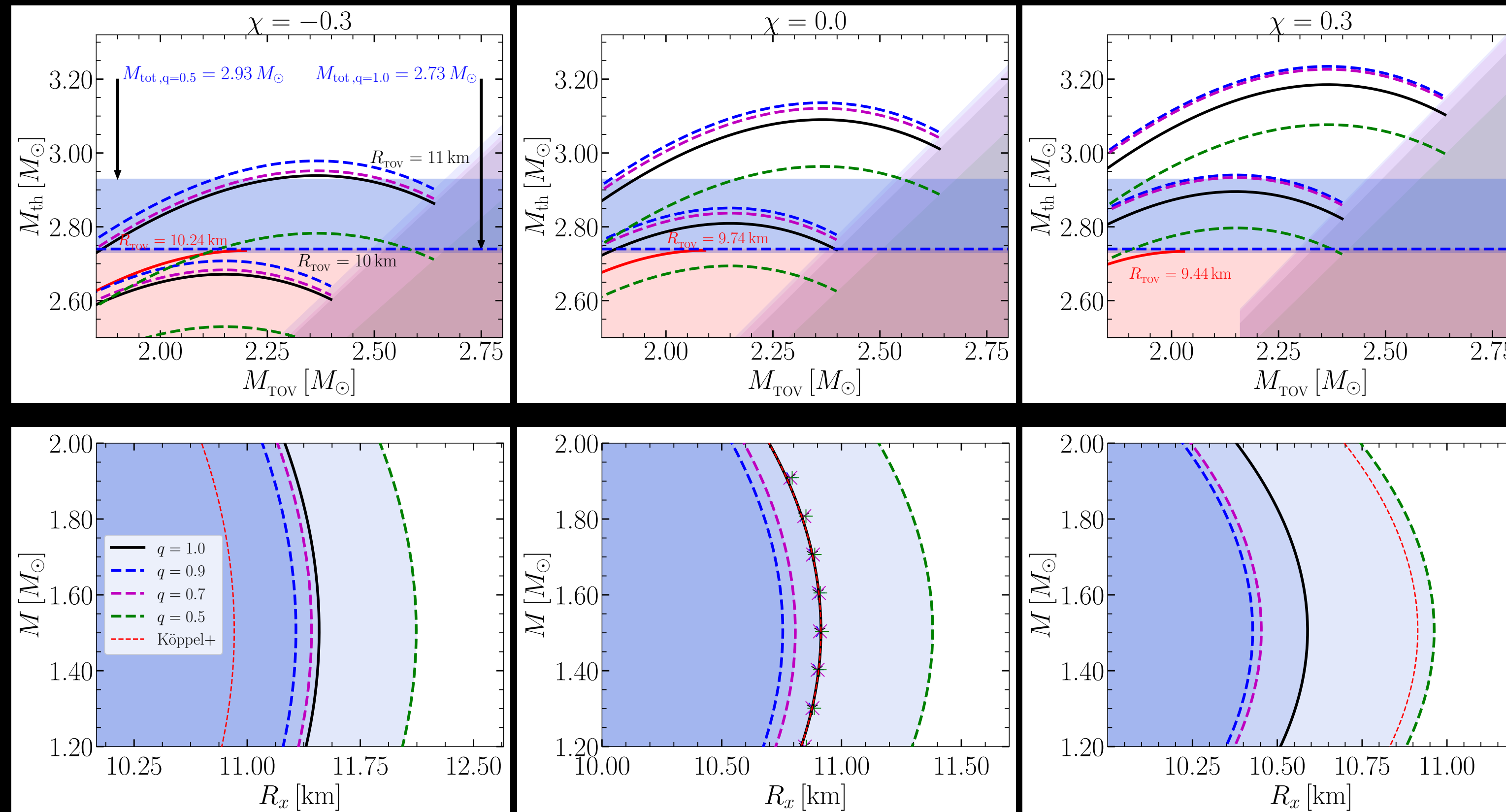
Indeed a **universal relation** exists and yields:

- **average deviation** from fit of $\sim 2\%$, and **largest deviation** below $\sim 6\%$.
- M_{th} **increases** by $\sim 10\%$ for **aligned** spins
- M_{th} **decreases** by $\sim 5\%$ for **antialigned** spins

Note: dependence on q **not monotonic**: balance between larger “discs” for small q and increased stability for large q yields **local maximum**

Possible to extend logic for lower limit on radius:

$$R_x(M, q, \chi) = \frac{R_x(M)}{f(q, \chi)} \quad \text{where } R_x(M) \text{ is from Köppel+ 2019 and } f(q, \chi) \text{ is the same as for } M_{\text{th}}$$



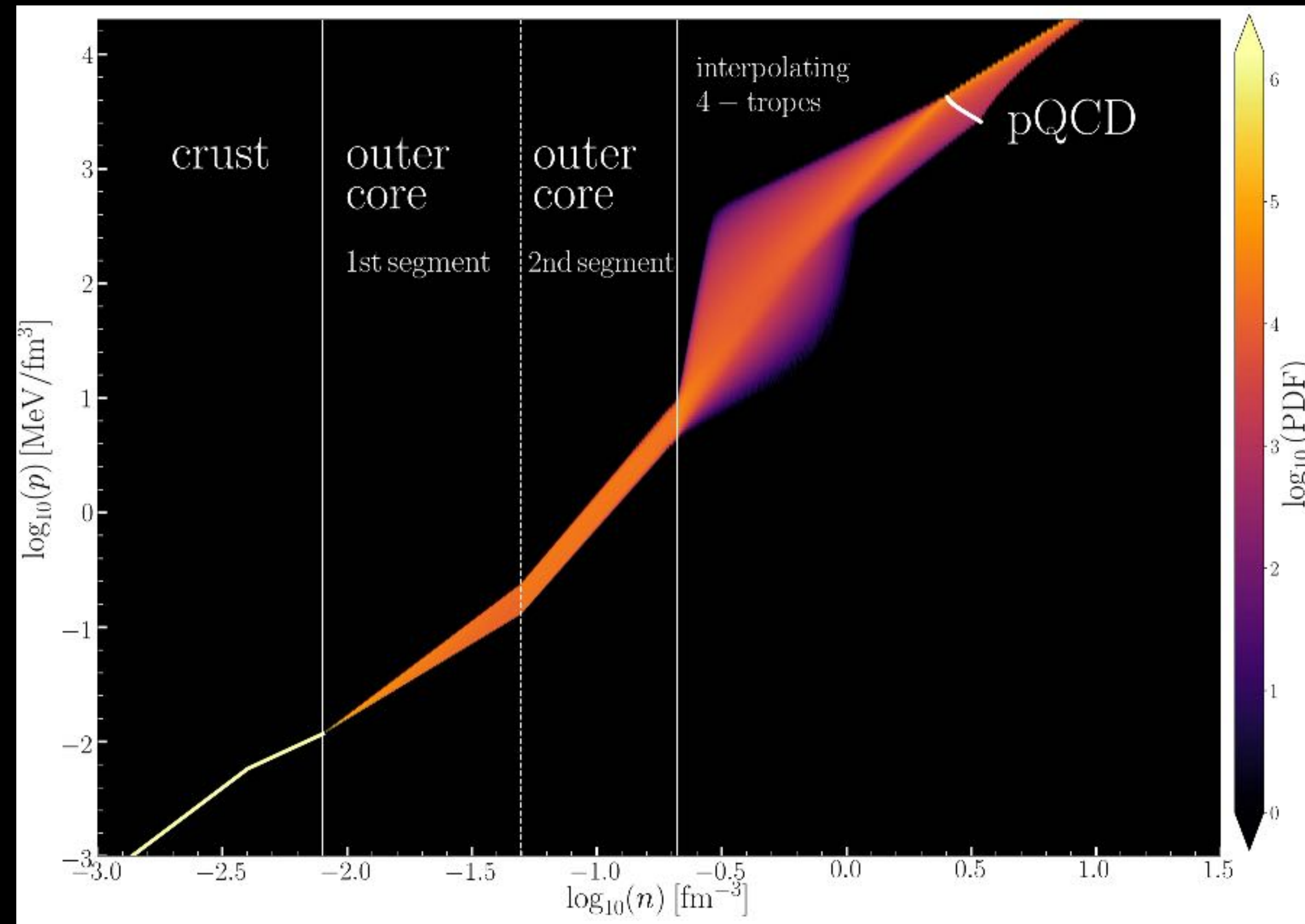
Antialigned binaries provide significantly tighter constraints:

$$R_{\text{TOV}} \geq 10.24 \text{ km for } \chi = -0.3$$

vs

$$R_{\text{TOV}} \geq 9.44 \text{ km for } \chi = 0.3$$

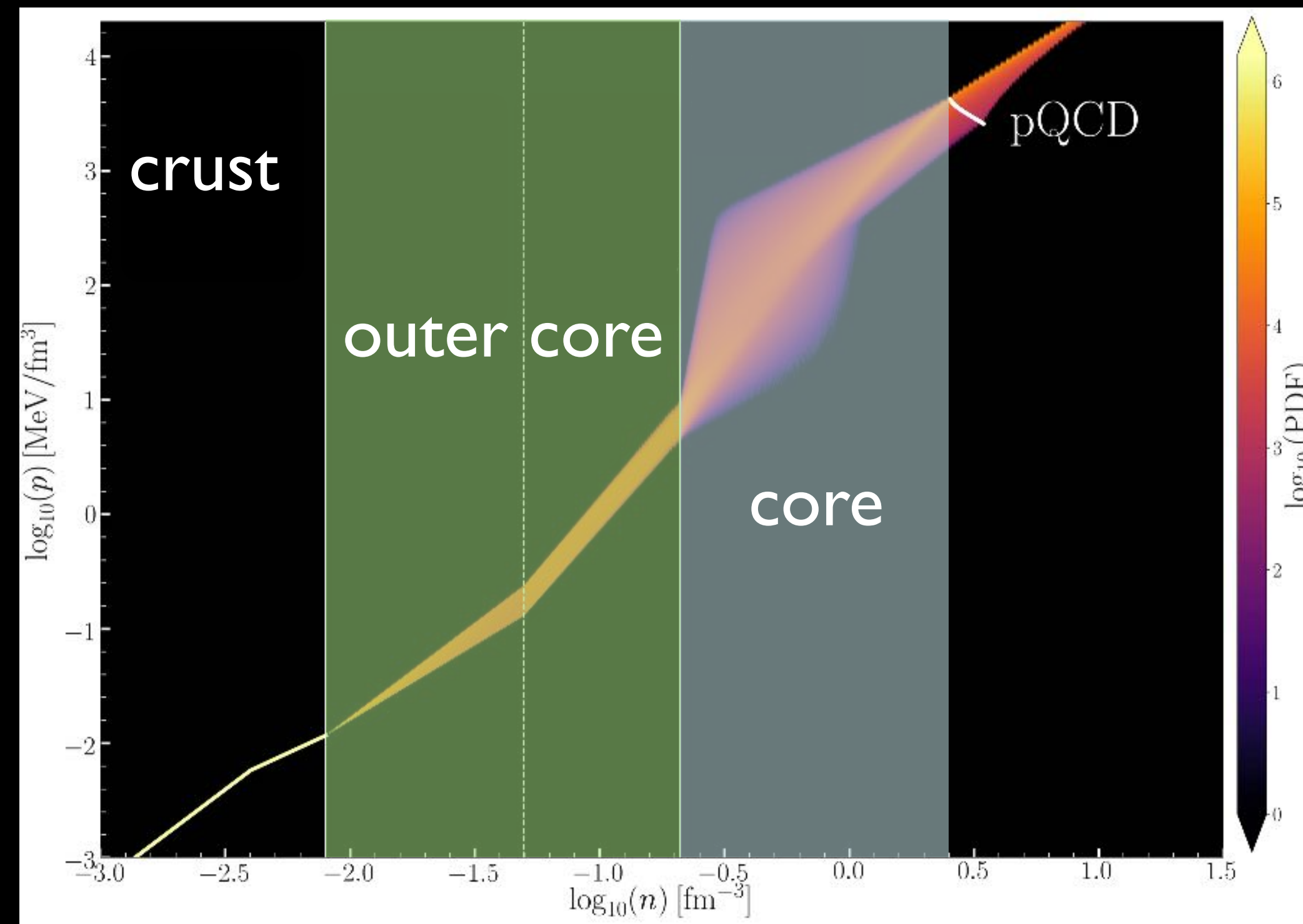
Limits on radii and deformabilities



Limits on radii and deformabilities

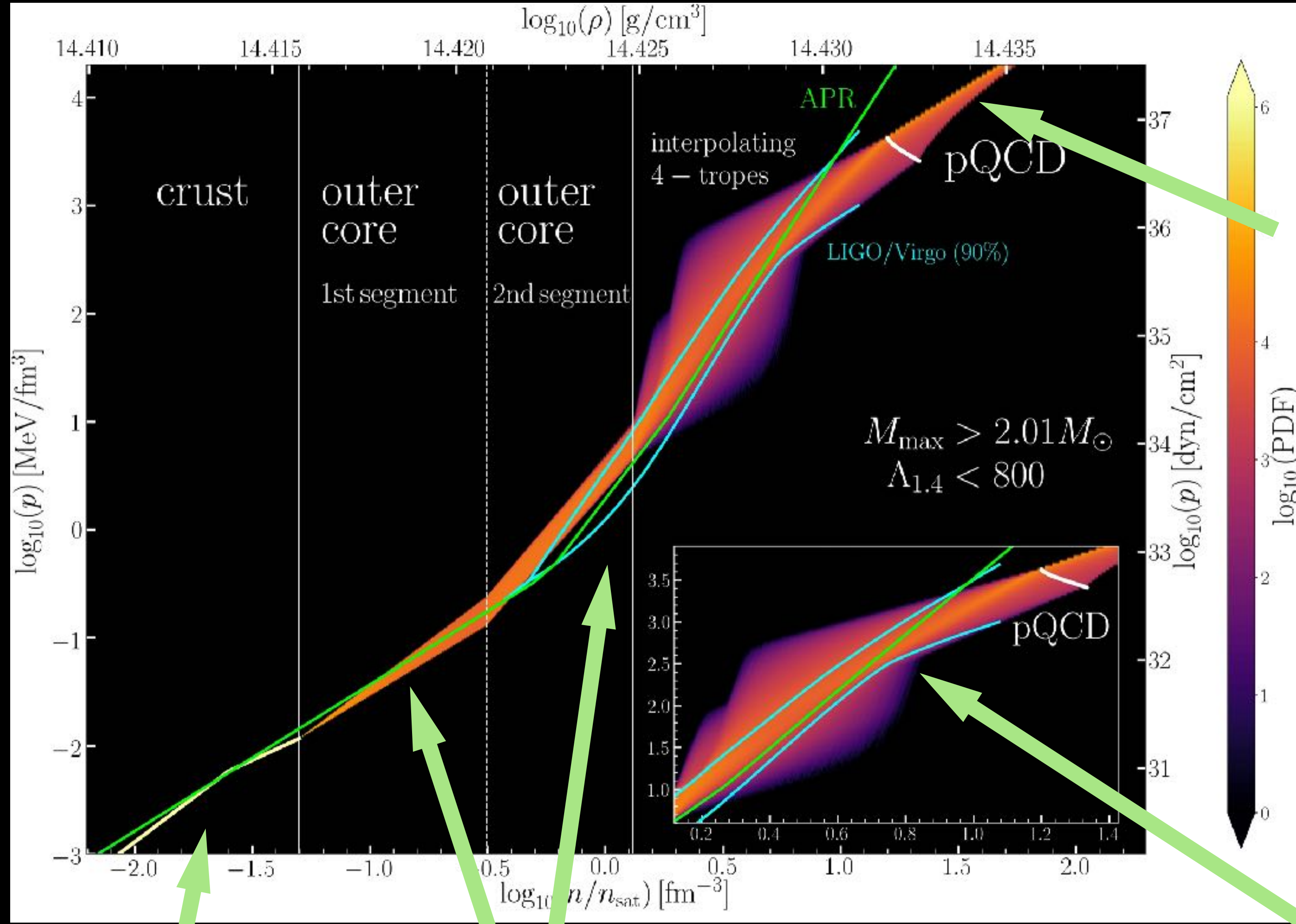
- Can new constraints be set on typical radius and tidal deformability by using GW170817?

- **Ignorance** can be parameterised and EOSs can be built arbitrarily as long as they satisfy specific **constraints** on **low** and **high** densities.



parametrising our ignorance

- Construct most generic family of NS-matter EOs



from $\mu_b=2.6\text{GeV}$
NNLO pQCD
Kurkela+ (2014)
Fraga+ (2014)

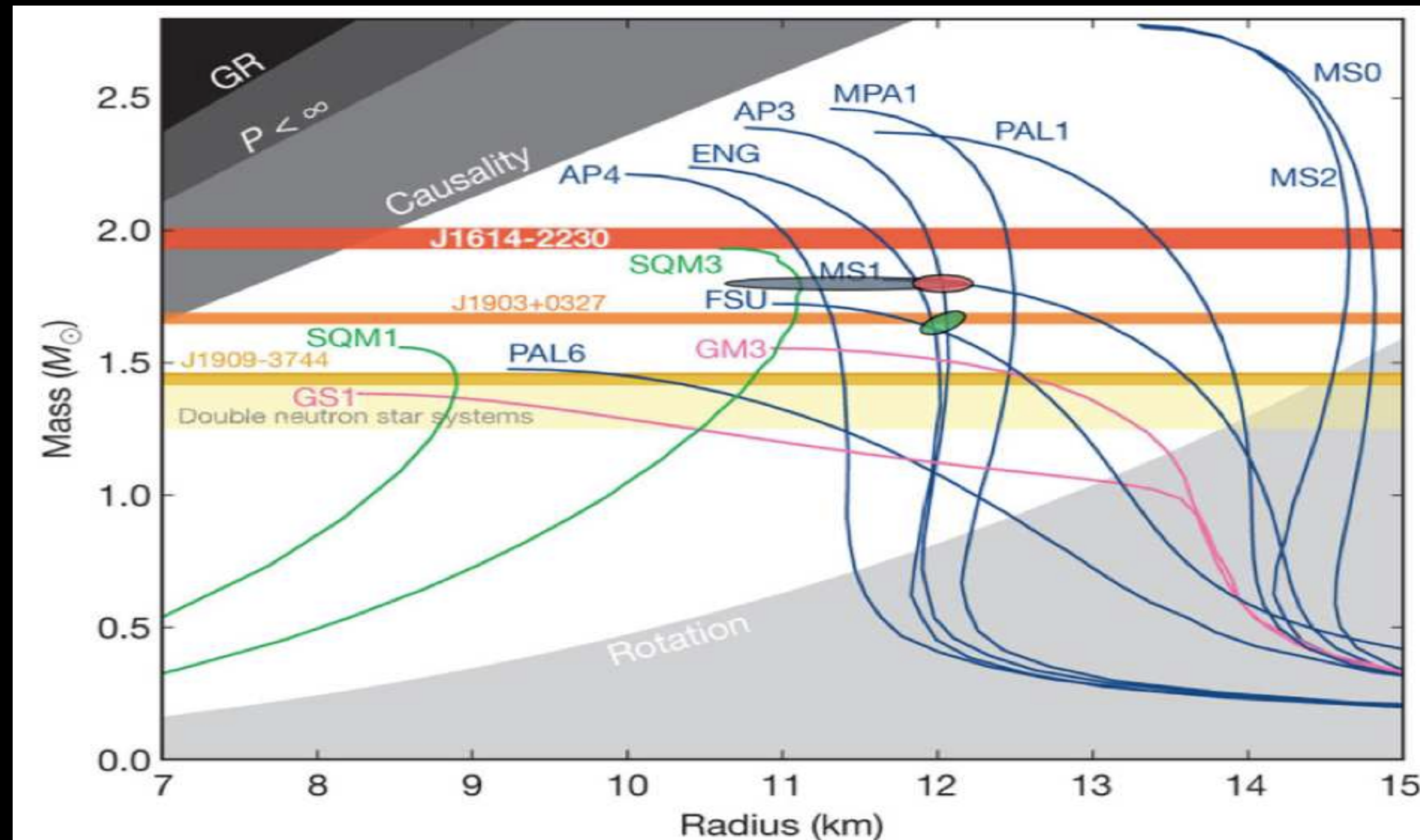
BPS

polytropic fit of Drischler+ (2016)
(large impact on results)

interpolation
by matching 4
polytropes

Mass-radius relations

- We have produced 10^6 EOSs with about 10^9 stellar models.
- Can impose differential constraints from the **maximum mass** and from the **tidal deformability** from **GW170817**

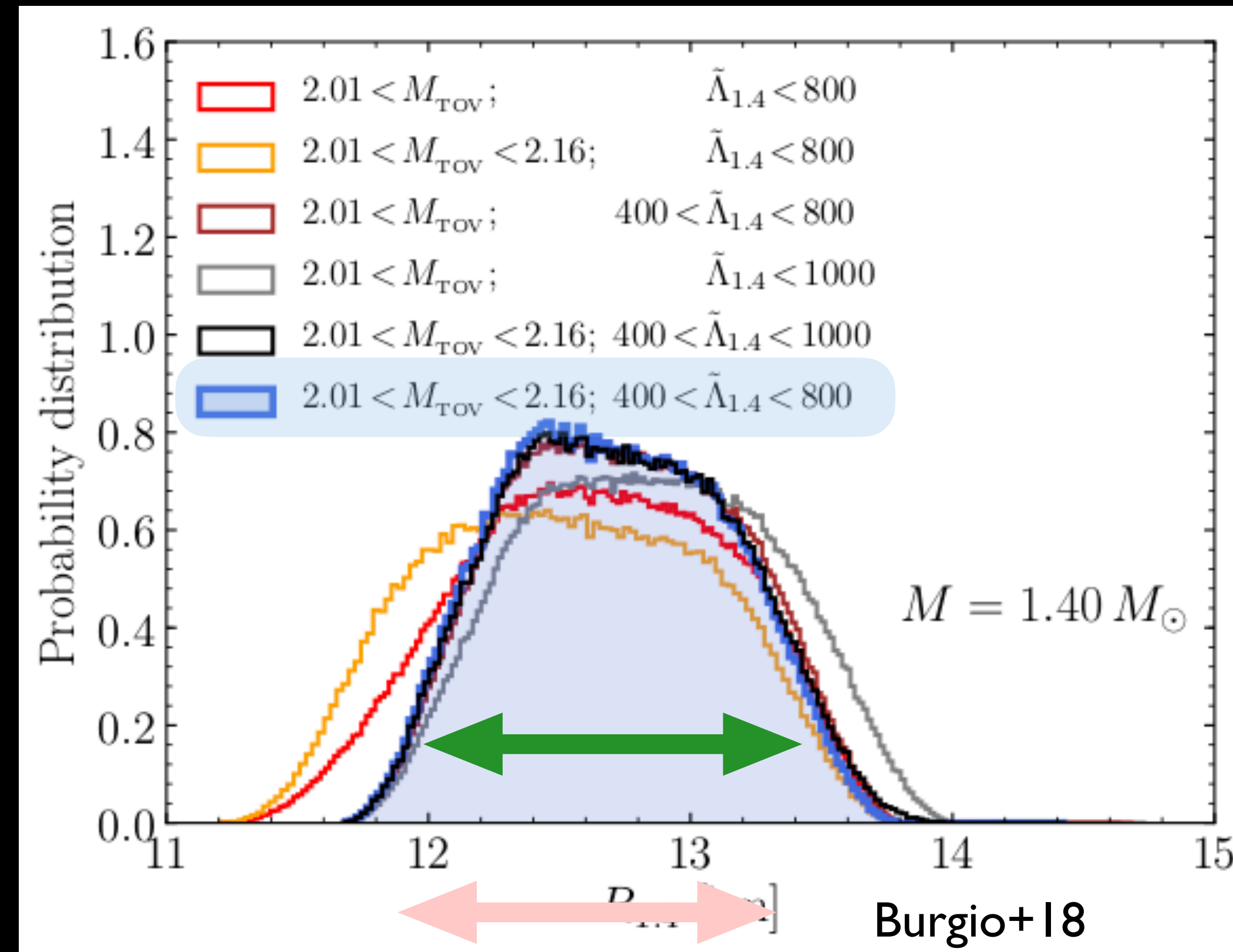


one-dimensional cuts

- Closer look at a mass of $M = 1.40 M_{\odot}$
- Can play with different constraints on maximum mass and tidal deformability.
- Overall distribution is very robust

$$12.00 < R_{1.4}/\text{km} < 13.45$$

$$\langle R_{1.4} \rangle = 12.45 \text{ km}$$



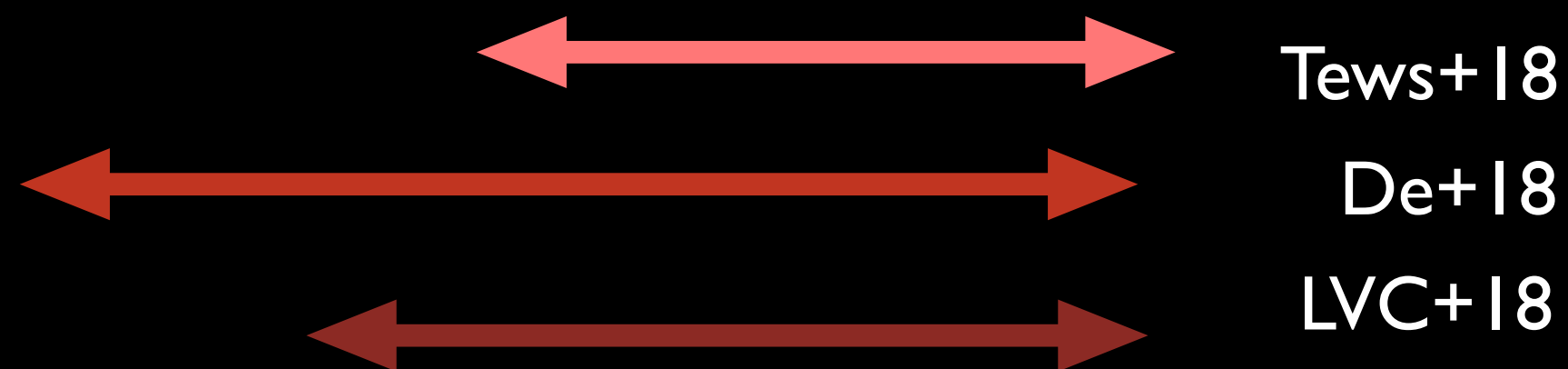
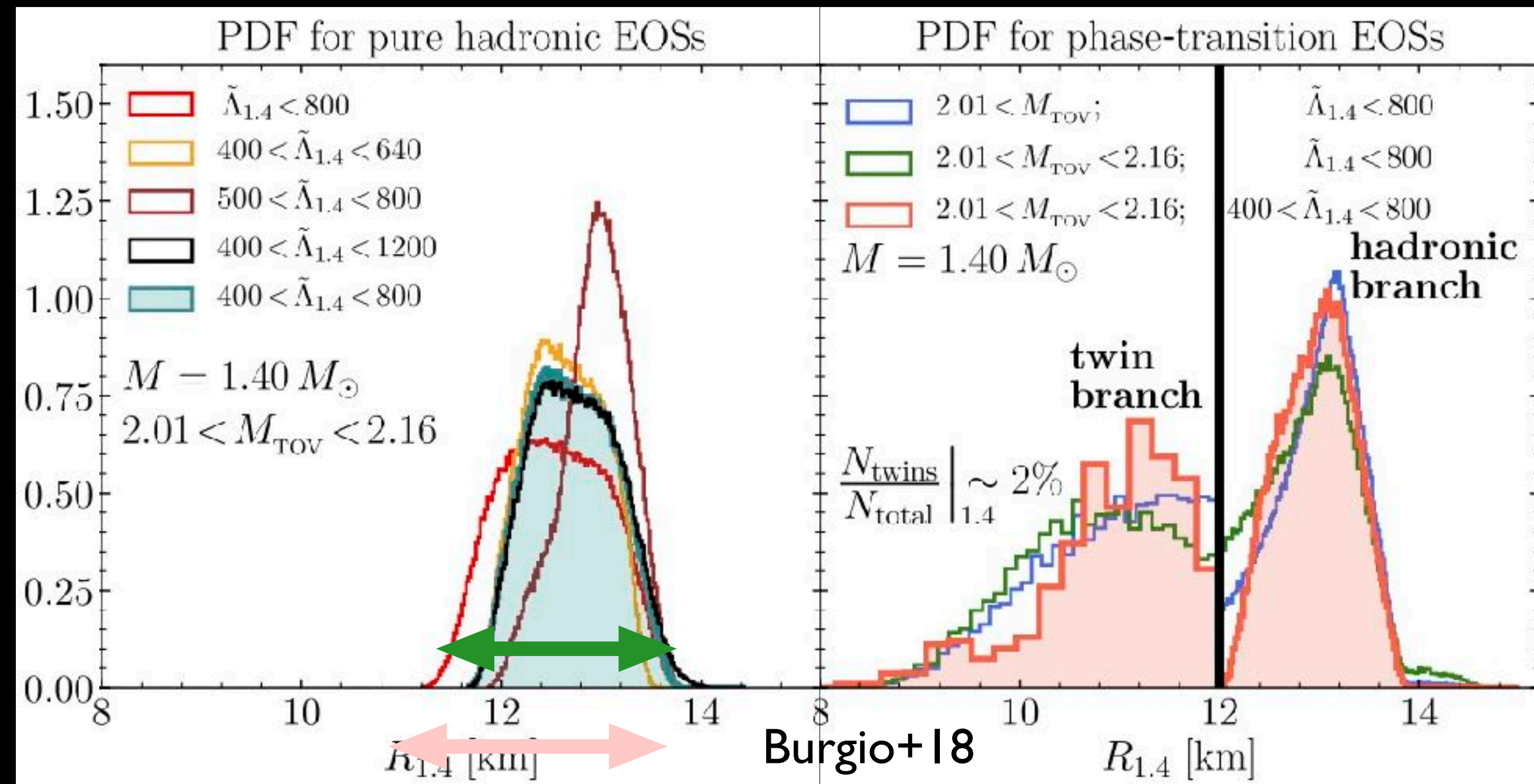
Tews+18

De+18

LVC+18

one-dimensional cuts

- Closer look at a mass of $M = 1.40 M_{\odot}$
- Play with different constraints on M_{TOV} and tidal deformability
- Overall distribution is very robust



$12.00 < R_{1.4}/\text{km} < 13.45$
 $\langle R_{1.4} \rangle = 12.45 \text{ km}$

Constraining tidal deformability

- Can explore statistics of all properties of our 10^9 models.
- In particular can study PDF of tidal deformability:

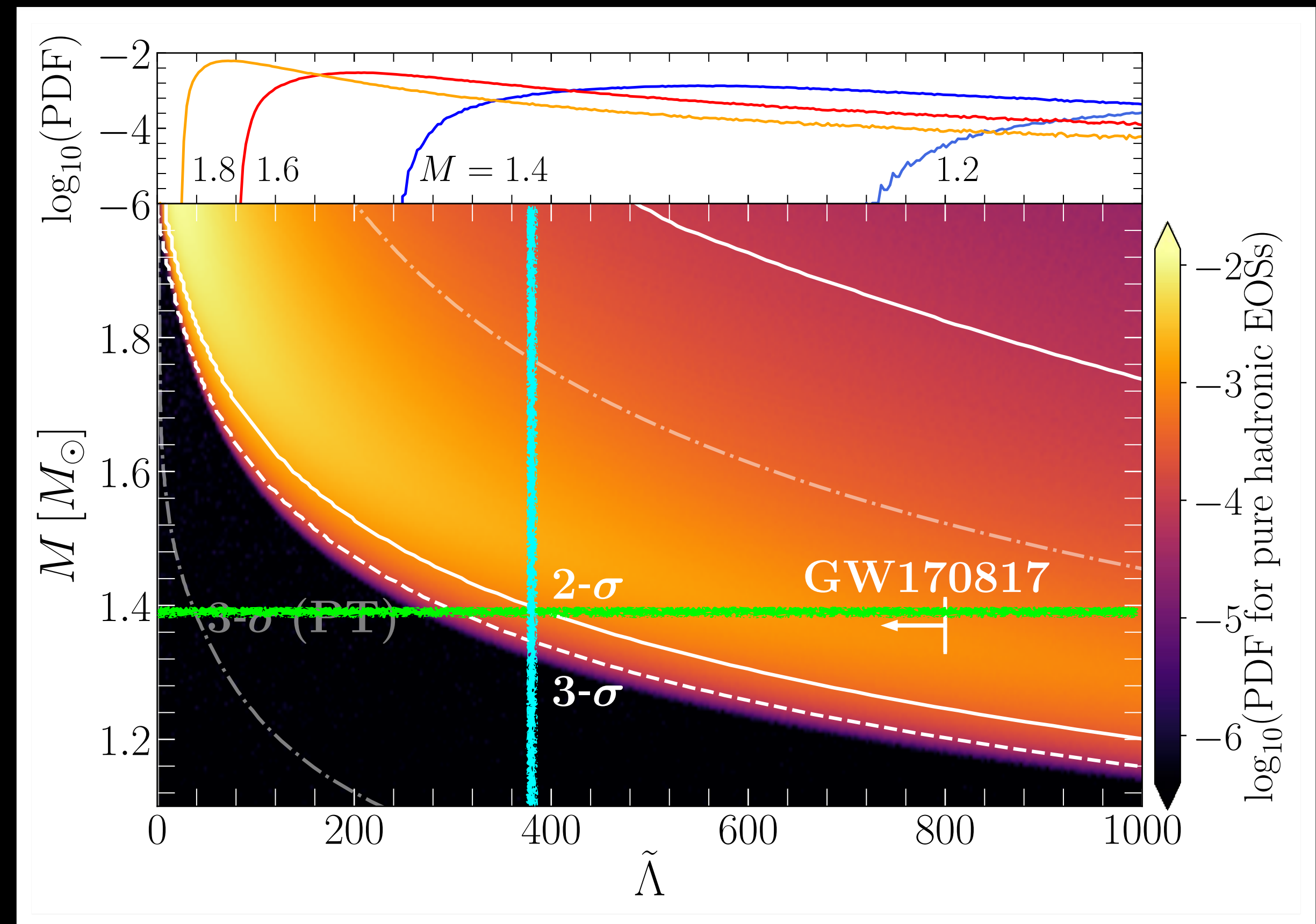
- LIGO has already set upper limit:

$$70 < \tilde{\Lambda}_{1.4} < 720$$

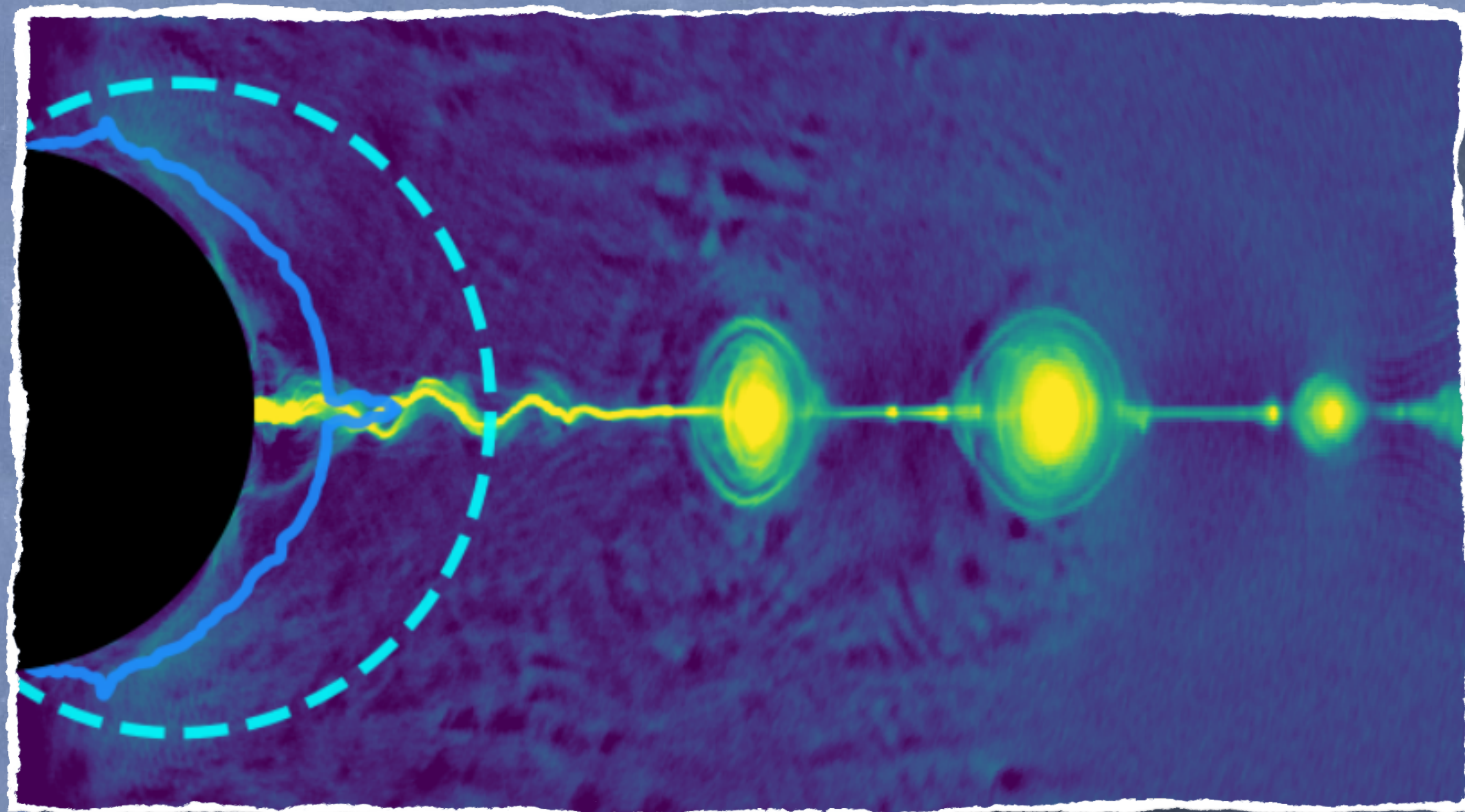
- Our sample sets a lower limit:

$$\tilde{\Lambda}_{1.4} > 375$$

the largest so far.

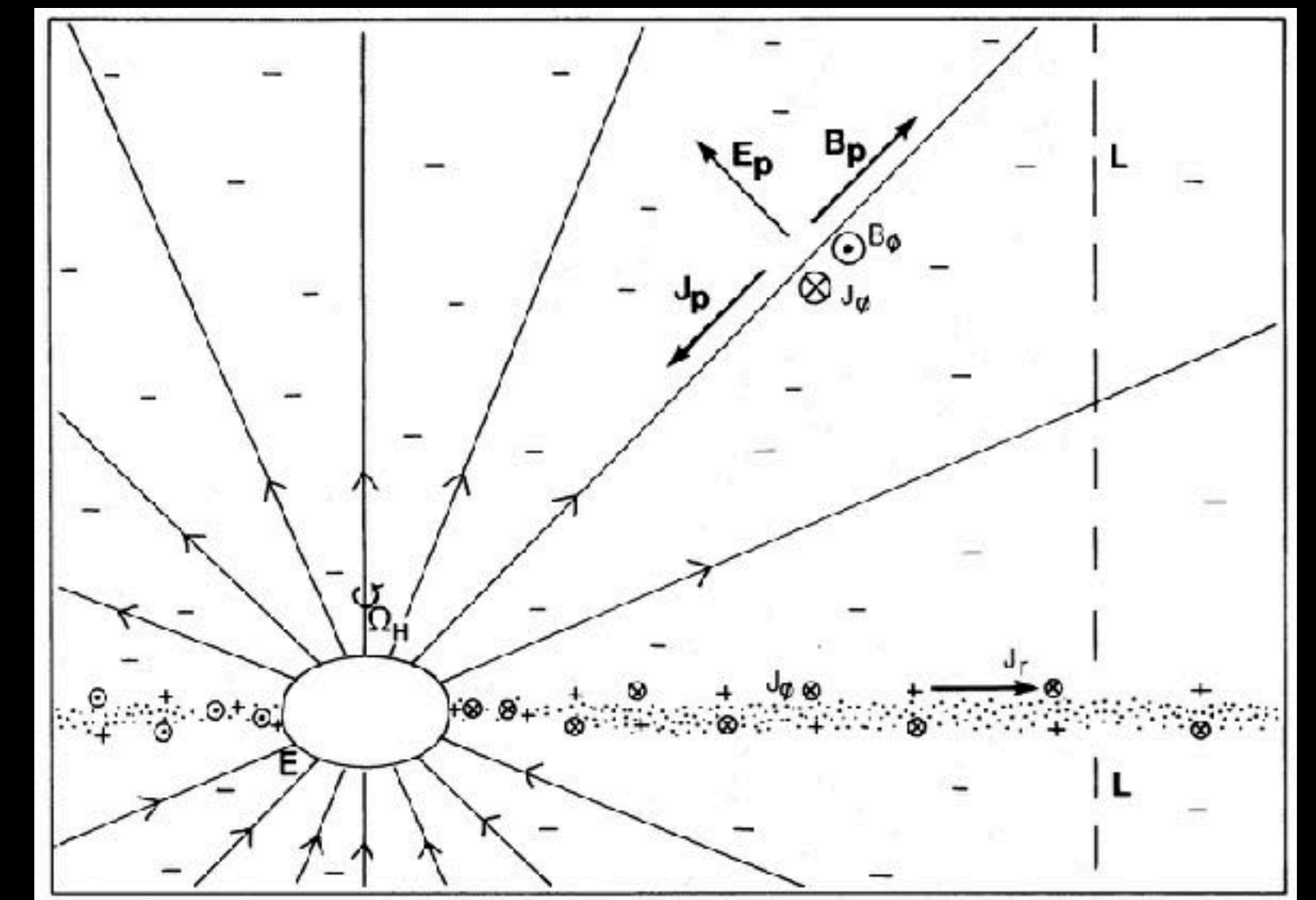
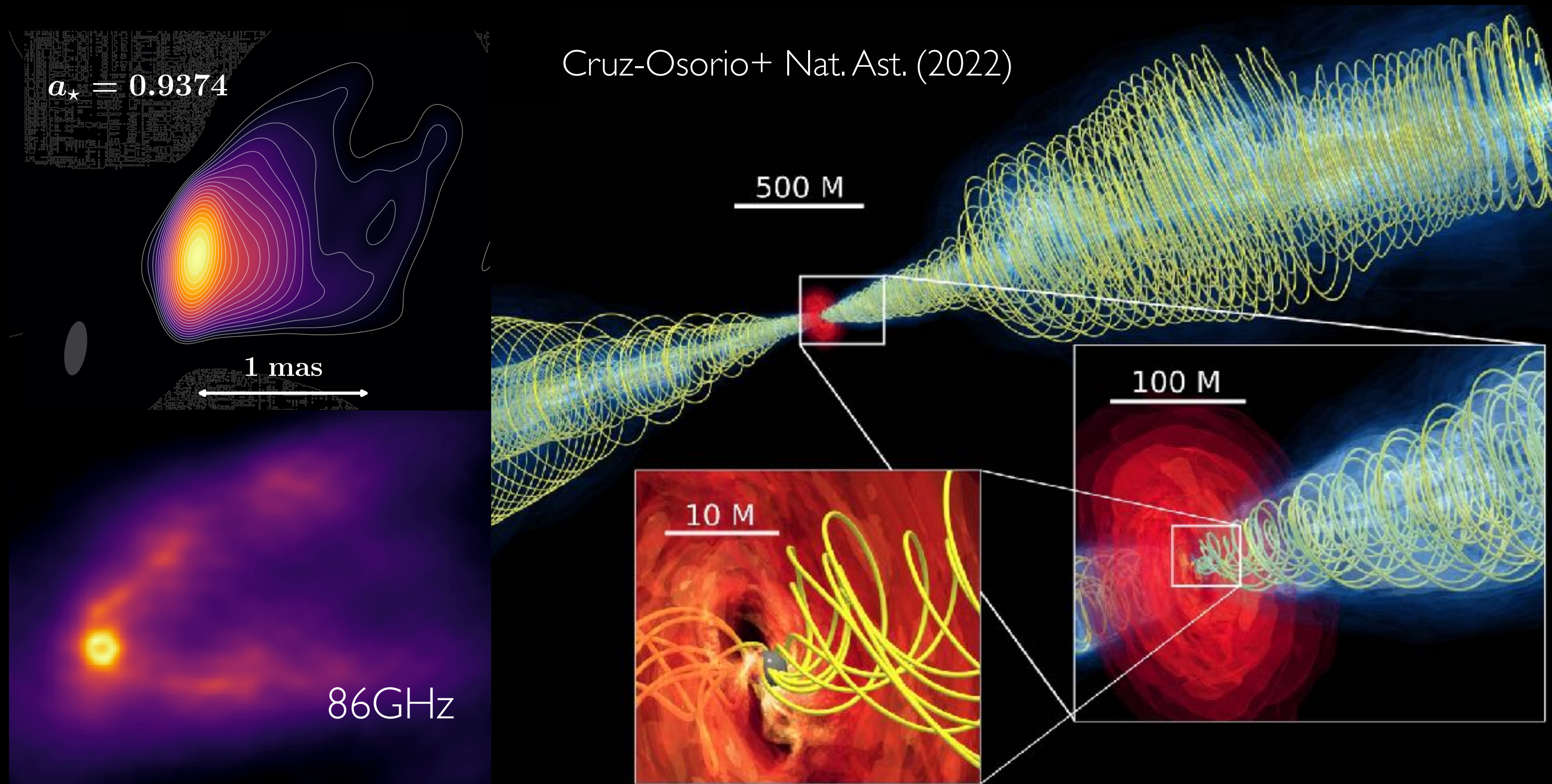


Energy extraction from rotating BHs



A collisional description on BH scales: GRMHD simulations

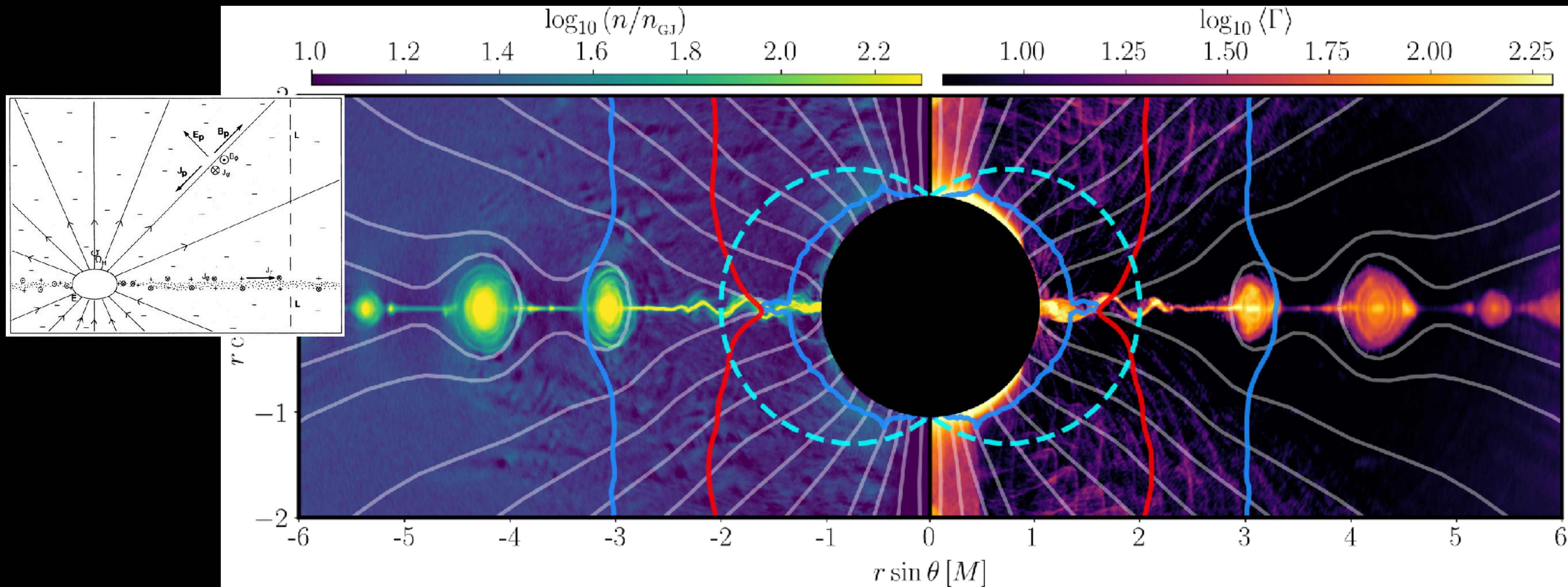
- GRMHD simulations of accretion onto supermassive BHs have reached high level of sophistication and are able to reproduce morphology and energy spectrum of M87 jet
- The Blandford-Znajek (BZ) mechanism offers most natural route to extract the rotational energy from rotating BHs and power relativistic jets. However, it assumes a FF regime



Blandford and Znajek MNRAS (1977)

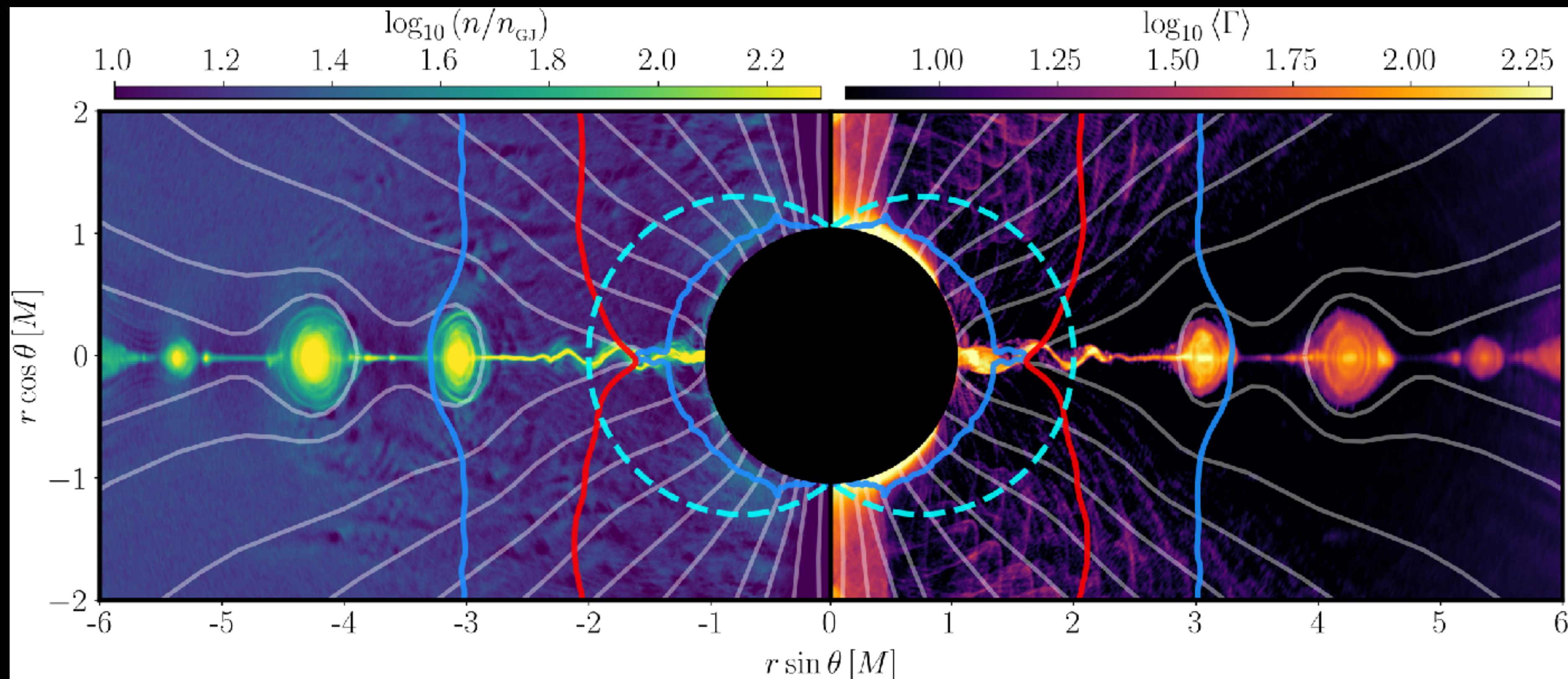
A collisionless description on BH scales: PIC simulations

- Particle-in-cell simulations provide ab-initio description of FF conditions near BH
- Extension to GR not easy but provides first-principle dynamics near BHs
- Carried out extensive campaign of e_+/e_- pair plasma in 2D with new code **FPIC** and “classic” split-monopole of BZ solution



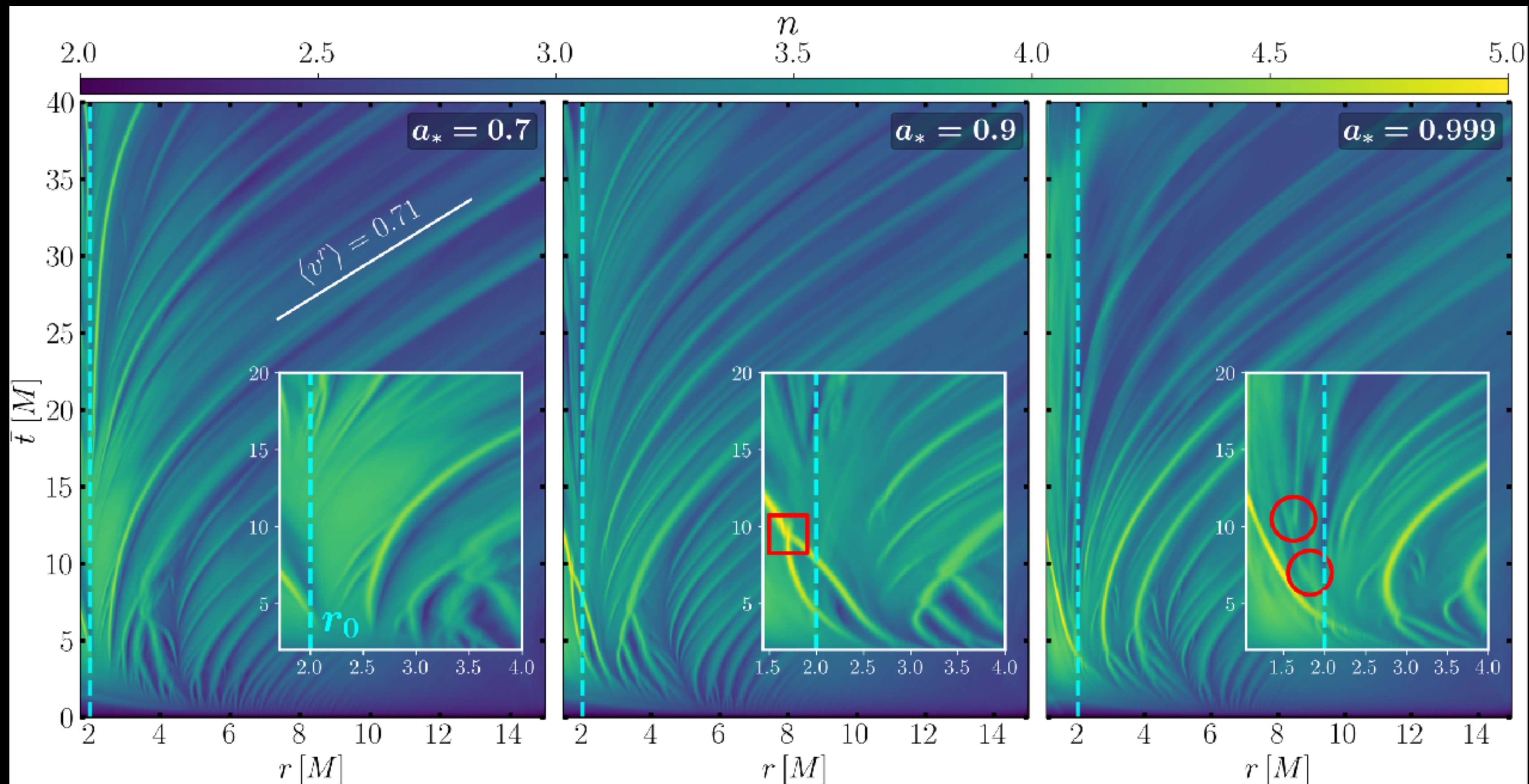
Microphysics on BH scales

- SR-PIC simulations provide important input for large-scale jet emission
- Extension to GR not easy but provides first-principle dynamics near BHs
- Carried out extensive campaign of e_+/e_- pair plasma in 2D with new code and “classic” split-monopole of Blandford-Znajek (BZ) solution



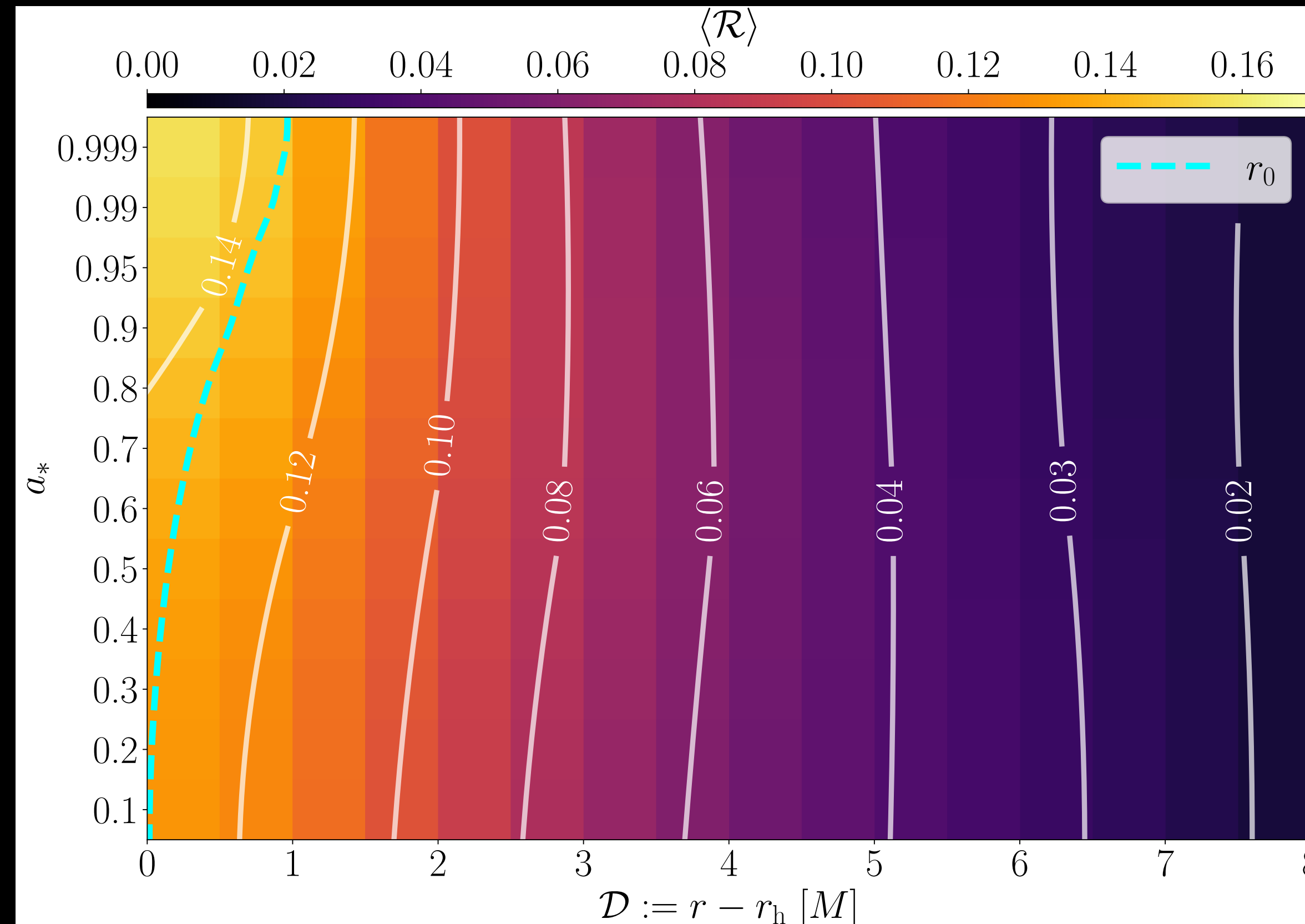
Among the new results...

- evidence plasmoids can **collide** and **merge** inside and outside **ergosphere**
- evidence plasmoids can also **split** inside **ergosphere** and reach **infinity**
- outgoing plasmoids have radial velocity $v \simeq 0.7$ independent of BH spin



Reconnection rate

- reconnection rate \mathcal{R} essential for all considerations of EM emission
- simulations allow to compute $\mathcal{R} = \mathcal{R}(r, a_*)$
- reconnection grows with BH spin and reaches maximum $\mathcal{R} \simeq 0.14$ inside ergosphere of maximally rotating BH



Blandford-Znajek luminosity

The BZ luminosity can be expressed very generically as

$$P_{\text{BZ}} = \frac{\kappa}{4\pi} \Phi_h^2 F(\Omega_h)$$

where (Camilloni+ JCAP 2022)

κ depends uniquely on the B-field topology ($\kappa_{sm} = 1/(6\pi)$ for split monopole)

Φ_h is the magnetic flux across the event horizon

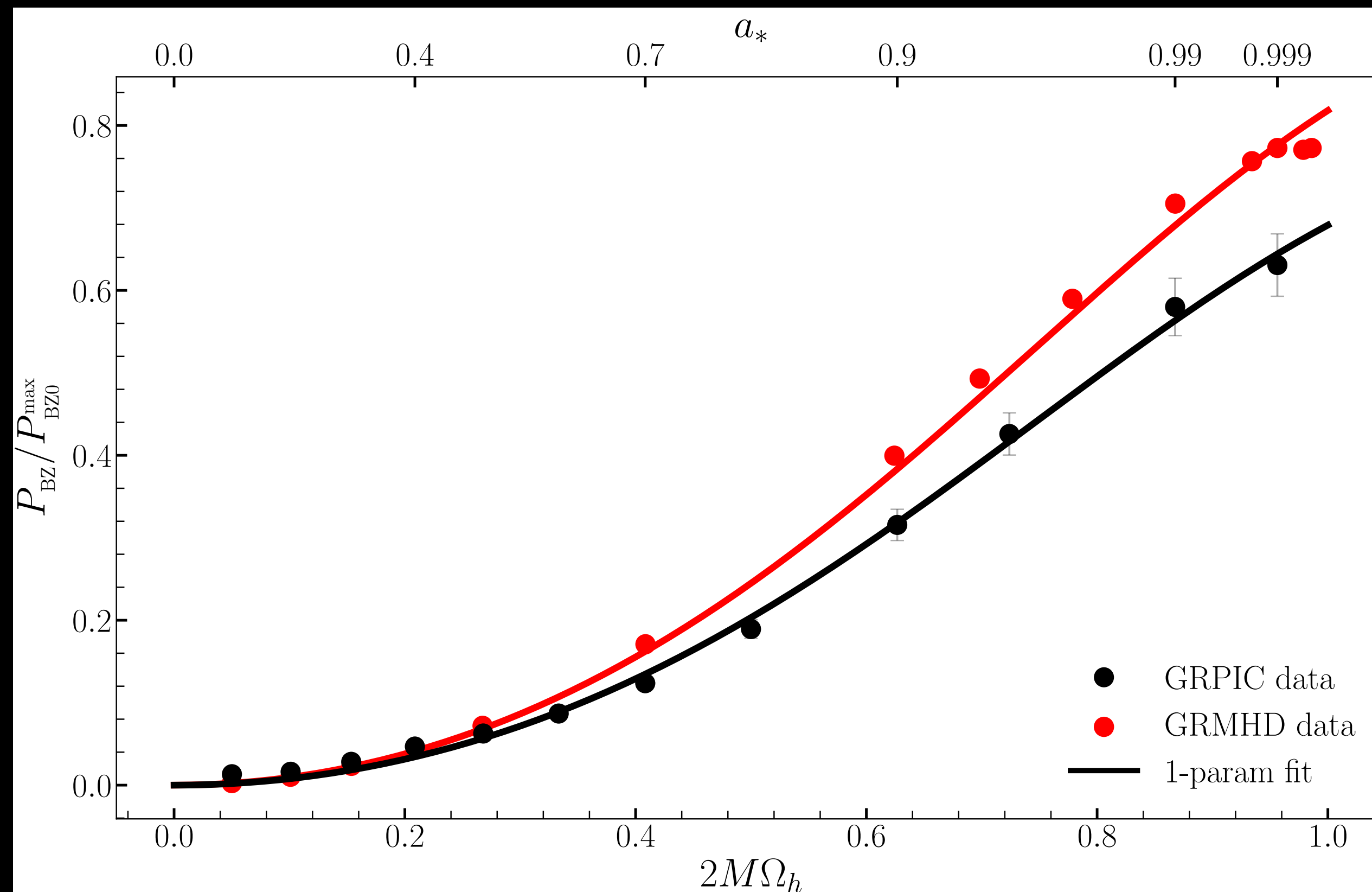
$F_{\text{an}}(\Omega_h)$ is a nonlinear function of the event-horizon velocity Ω_h :

$$F_{\text{an}}(\Omega_h) = \Omega_h^2 \left[1 + \tilde{\alpha}(M\Omega_h)^2 + \tilde{\beta}(M\Omega_h)^4 + \tilde{\gamma}|M\Omega_h|^5 + (\tilde{\delta} + \tilde{\epsilon} \log |M\Omega_h|)(M\Omega_h)^6 \right]$$

Blandford-Znajek luminosity

The BZ can be measured from the simulations

$$P_{\text{BZ}} = \frac{\kappa}{4\pi} \Phi_h^2 F(\Omega_h)$$

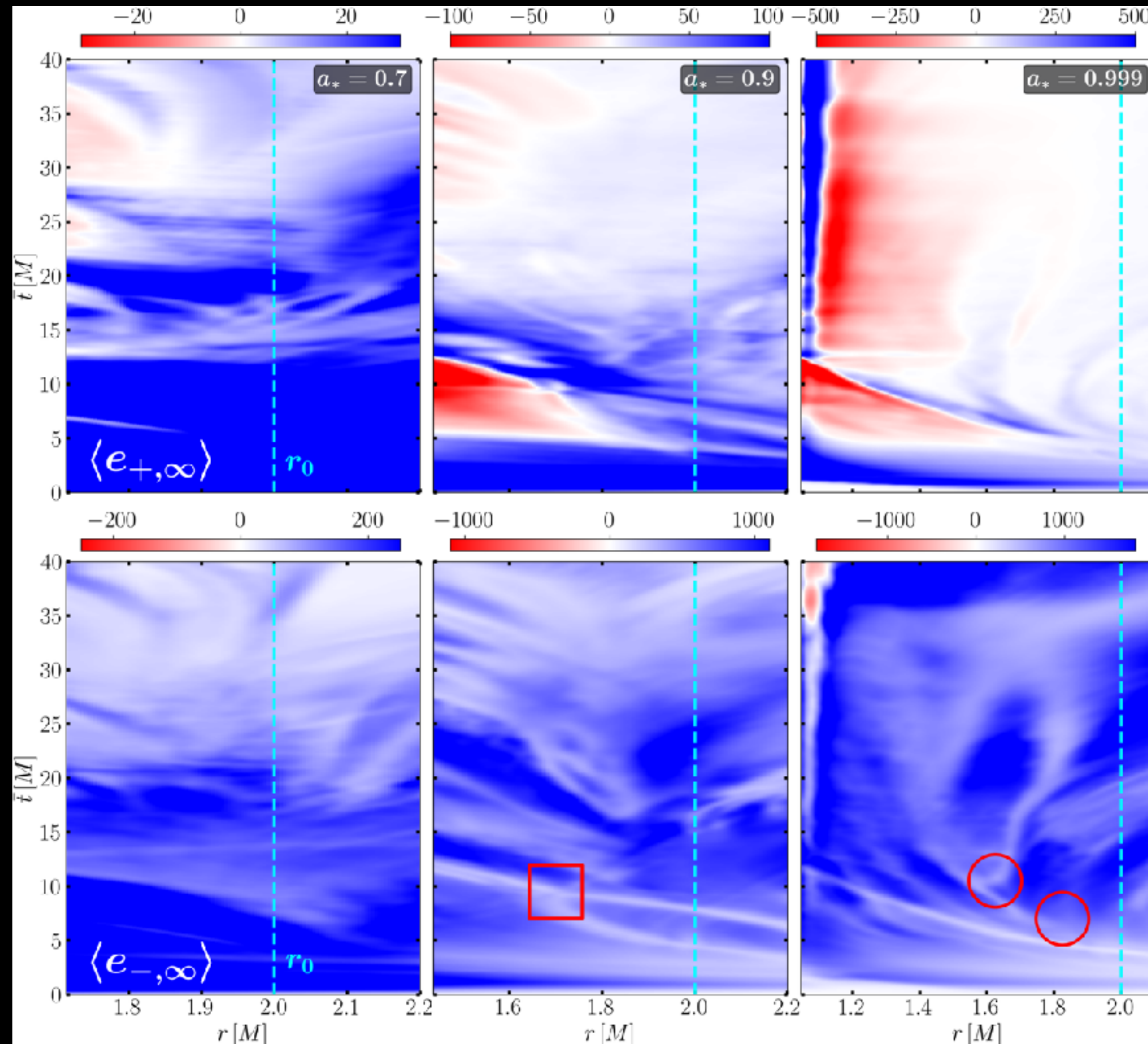


The measured BZ power matches very well analytic expression at $\mathcal{O}(\Omega_h^8)$

Good match is present also for GRMHD simulations; only difference is value of κ

Behaviour for extremal BHs can be captured with fit of quartic term

Evidence of Penrose process (PP)



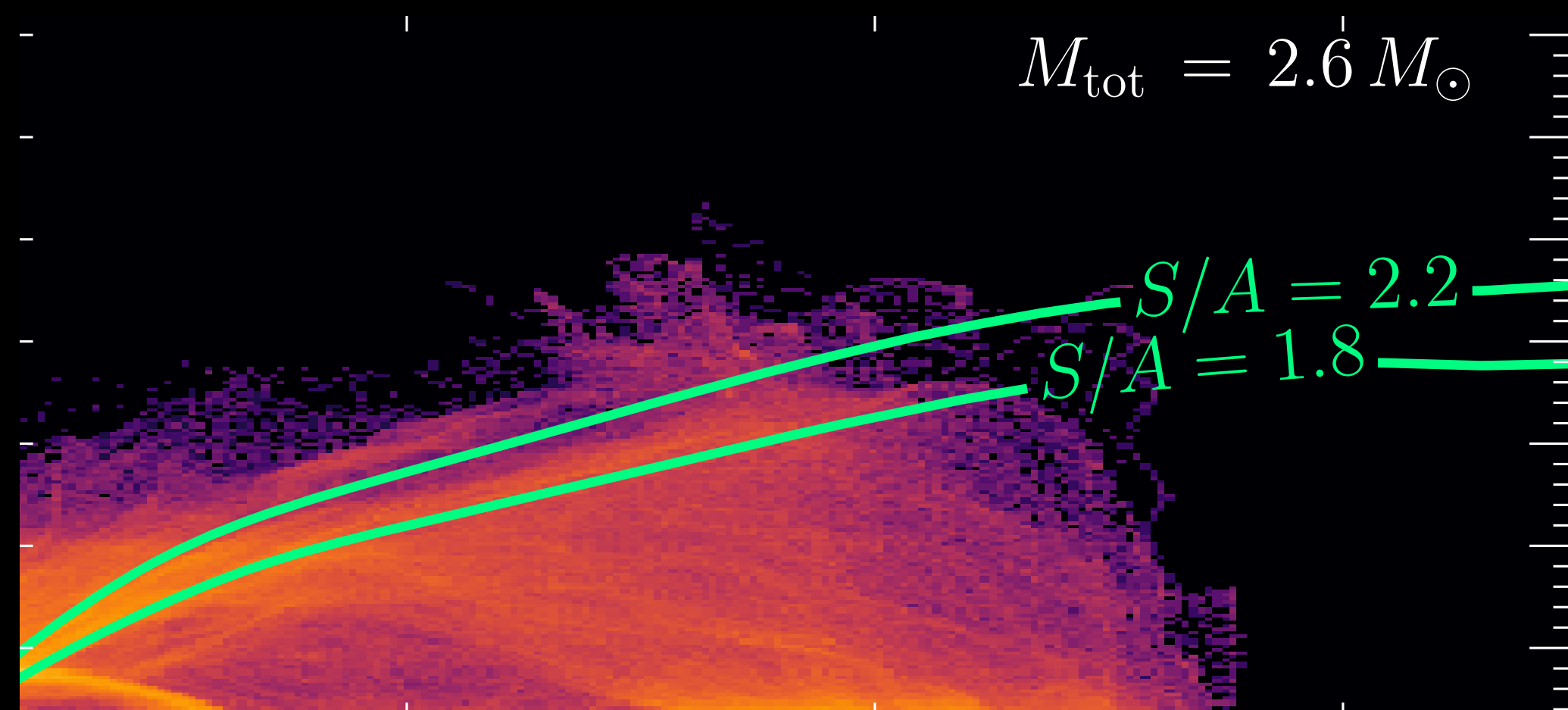
Evidence of negative-energy positrons inside ergosphere and accreting

Process is not steady and accretion rate increases with BH spin

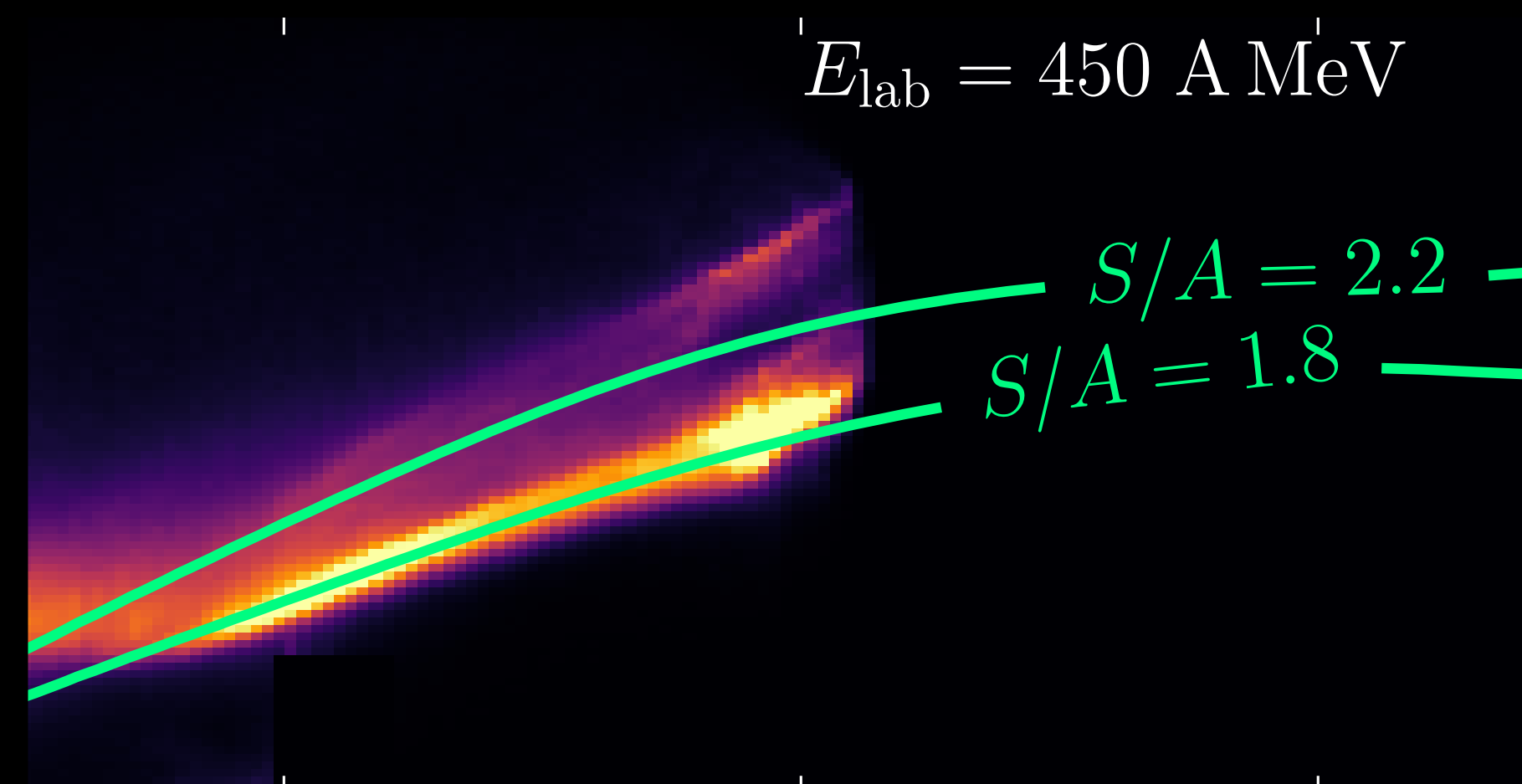
Accretion of negative-energy particles also for electrons but with smaller rates

Results suggest that **both BZ and PP** are present in force-free magnetospheres of rotating BHs: extraction is combination of effects.

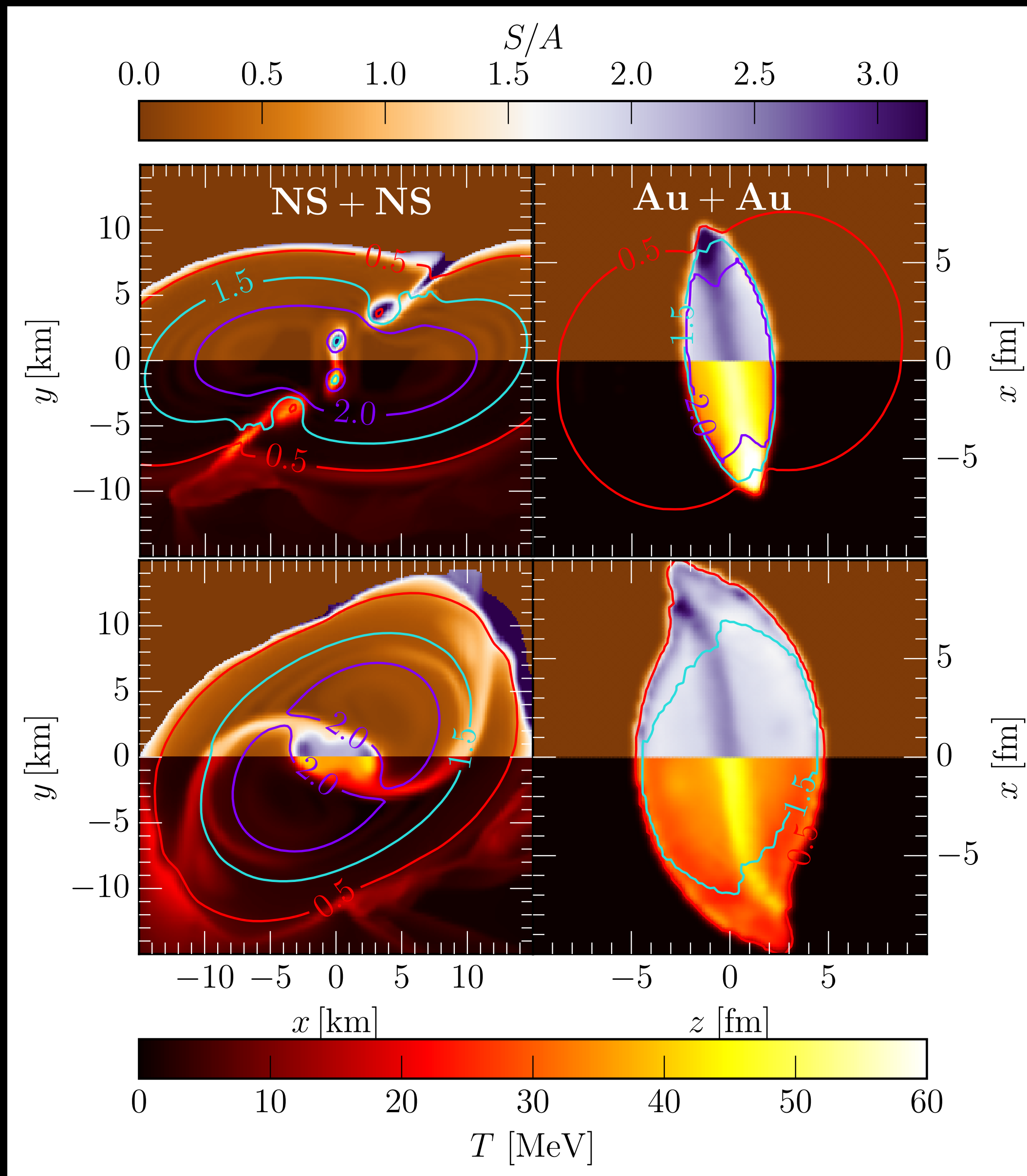
Probing neutron-star matter in the lab



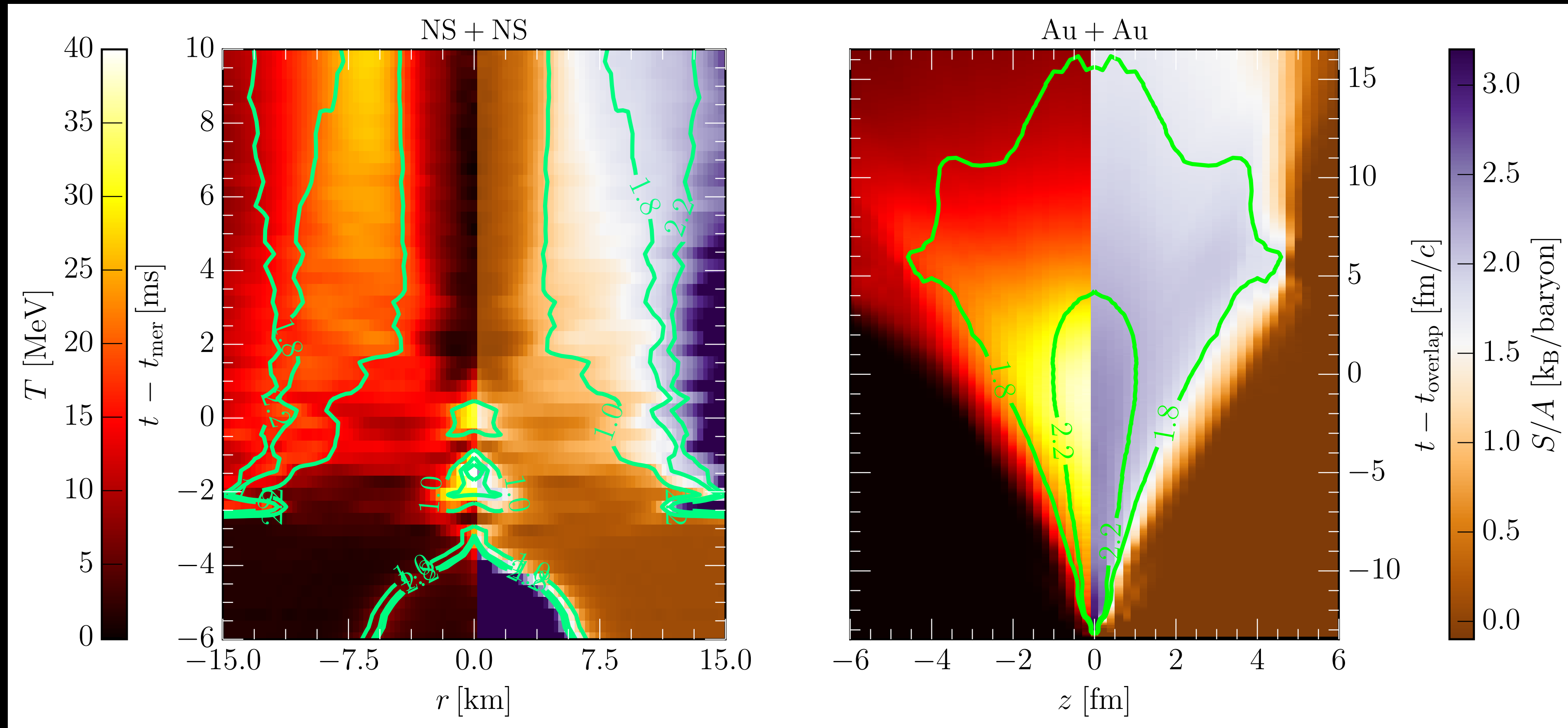
freeze - out



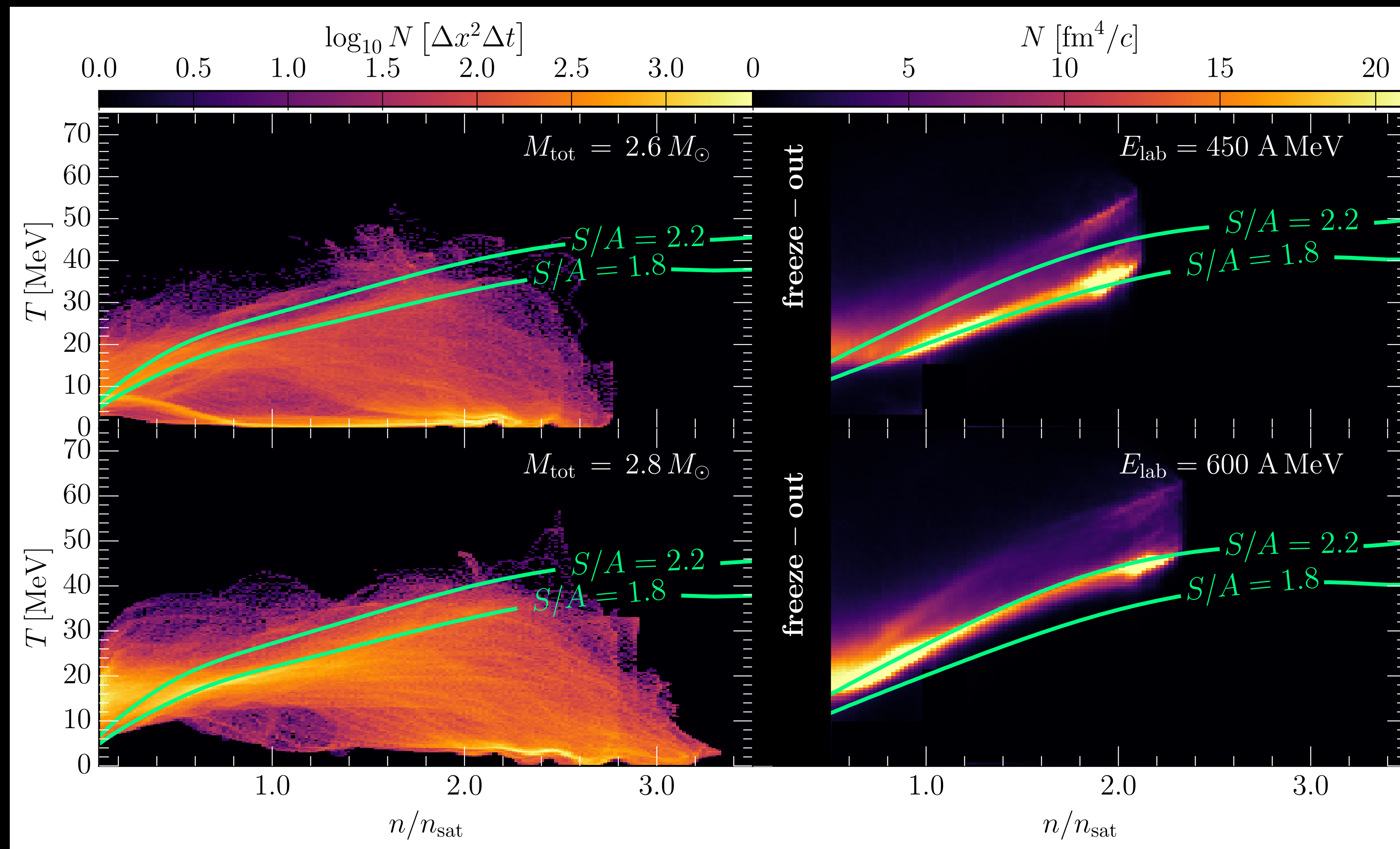
BNS mergers vs HICs



- We have explored the dynamics of BNS mergers and HIC using the same EOS.
- Chiral Mean Field model, based on the three-flavor chiral Lagrangian for hadronic matter.
- Crossover transition for deconfinement occurs at both, finite and zero temperature



- **BNSs:** core is hot and with high entropy; hot and high entropy ring is formed. Remnant is gravitationally bound.
- **HICs:** collision product is hot and with high entropy but expands rapidly cooling isentropically.



- **BNSs:** core is hot and with high entropy; hot and high entropy ring is formed. Remnant is gravitationally bound.
- **HICs:** collision product is hot and with high entropy but expands rapidly cooling isentropically.